

"QUIZ" for Lecture 9

NAME: (print!) Krithika Patrachari Section: 22

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q9FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 5, 8:00pm

1. Find $\frac{\partial f}{\partial r}$ and $\frac{\partial f}{\partial s}$ as functions of r and s , if

$$f(x, y) = x^2 + 2xy^2 + 2y^3,$$

and the variables are related by $x = r + 2s$ and $y = 3r + 2s$. You do not need to simplify!

$$\frac{\partial f}{\partial r} = \frac{\partial f}{\partial x} \left(\frac{\partial x}{\partial r} \right) + \frac{\partial f}{\partial y} \left(\frac{\partial y}{\partial r} \right)$$

$$\frac{\partial f}{\partial x} = 2x + 2y^2 \quad \frac{\partial x}{\partial r} = 1$$

$$\frac{\partial f}{\partial y} = 4x + 6y^2 \quad \frac{\partial y}{\partial r} = 3$$

$$\begin{aligned} \frac{\partial f}{\partial r} &= (2x + 2y^2)(1) + (4x + 6y^2)(3) \\ &= (2x + 2y^2) + (12x + 18y^2) \\ &= 14x + 20y^2 \end{aligned}$$

$$\frac{\partial f}{\partial s} = \frac{\partial f}{\partial x} \left(\frac{\partial x}{\partial s} \right) + \frac{\partial f}{\partial y} \left(\frac{\partial y}{\partial s} \right)$$

$$\frac{\partial f}{\partial x} = 2x + 2y^2 \quad \frac{\partial x}{\partial s} = 2$$

$$\frac{\partial f}{\partial y} = 4x + 6y^2 \quad \frac{\partial y}{\partial s} = 2$$

$$\begin{aligned} \frac{\partial f}{\partial s} &= (2x + 2y^2)(2) + (4x + 6y^2)(2) \\ &= 4x + 4y^2 + 8x + 12y^2 \\ &= 12x + 16y^2 \end{aligned}$$

2. Find $\frac{\partial z}{\partial x}$ and $\frac{\partial z}{\partial y}$ if

$$x^2 + y^2 + z^2 = 5xyz + 1 \quad \cdot \quad x^2 + y^2 + z^2 - 5xyz - 1 = 0$$

$$\frac{\partial}{\partial x} = 2x + 2z \frac{\partial z}{\partial x} - 5yz - 5xy \frac{\partial z}{\partial x} - 1 = 0$$

$$\frac{\partial z}{\partial x} (2z - 5xy) = 5xz - 2x + 1$$

$$\frac{\partial z}{\partial x} = \frac{5xz - 2x + 1}{2z - 5xy}$$

$$\frac{\partial}{\partial y} = 2y + 2z \frac{\partial z}{\partial y} - 5xz - 5xy \frac{\partial z}{\partial y} - 1 = 0$$

$$\frac{\partial z}{\partial y} (2z - 5xy) = 5xz - 2y + 1$$

$$\frac{\partial z}{\partial y} = \frac{5xz - 2y + 1}{2z - 5xy}$$