

"QUIZ" for Lecture 8

NAME: (print!) Yeram Sarah Jung Section: 23

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: qXFfirstLast.pdf) ASAP BUT NO LATER THAN Oct. 1, 2020, 8:00pm

1. Find the directional derivative of the function $f(x, y, z) = xy^2z^3$ at the point $(2, 1, 1)$ in the direction $\langle 2, -1, -1 \rangle$.

$$f_x = y^2 z^3 \quad f_y = 2xy z^3 \quad f_z = 3xy^2 z^2$$

$$\nabla f = \langle y^2 z^3, 2xy z^3, 3xy^2 z^2 \rangle$$

$$|\langle 2, -1, -1 \rangle| = \sqrt{2^2 + (-1)^2 + (-1)^2} = \sqrt{6}$$

$$u = \frac{1}{\sqrt{6}} \langle 2, -1, -1 \rangle = \left\langle \frac{2}{\sqrt{6}}, \frac{-1}{\sqrt{6}}, \frac{-1}{\sqrt{6}} \right\rangle$$

$$\nabla f(2, 1, 1) = \langle 1, 4, 6 \rangle$$

$$\langle 1, 4, 6 \rangle \cdot \left\langle \frac{2}{\sqrt{6}}, \frac{-1}{\sqrt{6}}, \frac{-1}{\sqrt{6}} \right\rangle = \frac{2}{\sqrt{6}} + \left(\frac{-4}{\sqrt{6}} \right) + \left(\frac{-6}{\sqrt{6}} \right) = \boxed{\frac{-8}{\sqrt{6}}}$$

2. Find the maximum rate of change of $f(x, y) = x^2 + y^3$ at the point $(2, 1)$ and the direction in which it occurs.

$$f_x = 2x \quad f_y = 3y^2$$

$$\nabla f = \langle 2x, 3y^2 \rangle$$

$$\nabla f(2, 1) = \langle 4, 3 \rangle$$

$$|\langle 4, 3 \rangle| = \sqrt{4^2 + 3^2} = 5$$

maximum rate of change is 5 in the direction $\langle 4, 3 \rangle$