

"QUIZ" for Lecture 8

NAME: (print!) Niharika Kamella Section: 23

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: qXFIRSTLAST.pdf) ASAP BUT NO LATER THAN Oct. 1, 2020, 8:00pm

1. Find the directional derivative of the function $f(x,y,z) = xy^2z^3$ at the point $(2,1,1)$ in the direction $\langle 2, -1, -1 \rangle$.

$$f_x = 1 \cdot y^2 z^3, \quad f_y = 2y x z^3, \quad f_z = 3z^2 x y^2$$

$$v = \left\langle \frac{2}{\sqrt{2^2+(-1)^2+(-1)^2}}, \frac{-1}{\sqrt{2^2+(-1)^2+(-1)^2}}, \frac{-1}{\sqrt{2^2+(-1)^2+(-1)^2}} \right\rangle = \left\langle \frac{2}{2}, \frac{-1}{2}, \frac{-1}{2} \right\rangle \rightarrow a=1, b=-\frac{1}{2}, c=-\frac{1}{2}$$

$$D_v f = (2, 1, 1) = 1(1-1) + -\frac{1}{2}(2-1) + -\frac{1}{2}(2-1) = -\frac{1}{2} - \frac{1}{2} = \boxed{-1}$$

2. Find the maximum rate of change of $f(x,y) = x^2 + y^3$ at the point $(2,1)$ and the direction in which it occurs.

$$f(x,y) = x^2 + y^3$$

$$\nabla f(x,y) = \left\langle \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right\rangle = \langle 2xy^3, 3y^2x^2 \rangle$$

$$\nabla f(2,1) = \langle 2(2)(1)^3, 3(1)^2(2)^2 \rangle$$

$$\nabla f(2,1) = \boxed{\langle 4, 12 \rangle} \rightarrow \text{max rate of change in direction}$$

$$|\nabla f(2,1)| = \sqrt{4^2 + 12^2} = \sqrt{16 + 144} = \sqrt{160} \rightarrow \text{magnitude of max r.o.c.}$$