

You can share answers

"QUIZ" for Lecture 8

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: qXFirstLast.pdf) ASAP BUT NO LATER THAN Oct. 1, 2020, 8:00pm

1. Find the directional derivative of the function $f(x, y, z) = xy^2z^3$ at the point $(2, 1, 1)$ in the direction $\langle 2, -1, -1 \rangle$.

$$D_{\vec{u}} f(P) = \nabla f_P \cdot \vec{u} = \langle 1, 4, 6 \rangle \cdot \langle 2, -1, -1 \rangle = 2 - 4 + 6 = -8$$

$$\begin{aligned} \nabla f_P &= \left\langle \frac{d}{dx} f(xyz), \frac{d}{dy} f(xyz), \frac{d}{dz} xy^2z^3 \right\rangle \\ &= \langle y^2z^3, 2xy^2z^3, 3xy^2z^2 \rangle \\ &= \langle 1, 4, 6 \rangle \end{aligned}$$

2. Find the maximum rate of change of $f(x, y) = x^2 + y^3$ at the point $(2, 1)$ and the direction in which it occurs.

$$\nabla f(x, y) = \langle 2x, 3y^2 \rangle$$

$$\nabla f_{(2,1)} = \langle 4, 3 \rangle$$

$$\vec{u} = \frac{\langle 4, 3 \rangle}{5}$$

direction

$$\|\nabla f_{(2,1)}\| = \sqrt{4^2 + 3^2} = 5$$

max rate
of change