

"QUIZ" for Lecture 8

NAME: (print!) Fayed Raza Section: 24

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: qXFirstLast.pdf) ASAP BUT NO LATER THAN Oct. 1, 2020, 8:00pm

1. Find the directional derivative of the function $f(x, y, z) = xy^2z^3$ at the point $(2, 4, 6)$ in the direction $\langle 2, -1, -1 \rangle$.

$$f(x, y, z) = x y^2 z^3 \quad \langle 1, 4, 6 \rangle, \langle 2, -1, -1 \rangle$$

$$\begin{matrix} 2 & -4 & -6 \\ & & -8 \end{matrix}$$

$$\left\langle \frac{d}{dx} (x y^2 z^3), \frac{d}{dy} (x y^2 z^3), \frac{d}{dz} (x y^2 z^3) \right\rangle$$

$$\langle y^2 z^3, 2 y x z^3, 3 z^2 x y^2 \rangle$$

$$\langle (1)(1), 2(2)(1)(1), 3(1)(2)(1) \rangle \rightarrow \langle 1, 4, 6 \rangle$$

2. Find the maximum rate of change of $f(x, y) = x^2 + y^3$ at the point $(2, 1)$ and the direction in which it occurs.

$$f'(x, y) = 2x + 3y^2 \quad \tan^{-1}\left(\frac{4}{3}\right) = 53^\circ$$

$$f'(2, 1) = 4 + 3 = 7 @ 53^\circ$$