

"QUIZ" for Lecture 8

NAME: (print!) Aditya Sivakumar Section: 24

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: qXFirstLast.pdf) ASAP BUT NO LATER THAN Oct. 1, 2020, 8:00pm

1. Find the directional derivative of the function $f(x, y, z) = xy^2z^3$ at the point $(2, 1, 1)$ in the direction $\langle 2, -1, 1 \rangle$.

$$u = \langle 2, -1, 1 \rangle$$

$$D_u f = \nabla f \cdot u$$

$$\nabla f = \langle y^2z^3, 2xyz^3, 3xy^2z^2 \rangle = \langle 1, 4, 6 \rangle$$

$$\nabla f \cdot u = \langle 1, 4, 6 \rangle \cdot \langle 2, -1, 1 \rangle = 4$$

2. Find the maximum rate of change of $f(x, y) = x^2 + y^3$ at the point $(2, 1)$ and the direction in which it occurs.

$$\nabla f = \langle 2x, 3y^2 \rangle = \langle 4, 3 \rangle$$

$$|\langle 4, 3 \rangle| = 5$$

$$\langle 4/5, 3/5 \rangle$$

Max rate of change is 5 at

direction $\langle 4/5, 3/5 \rangle$