

"QUIZ" for Lecture 7

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q7FirstLast.pdf) ASAP BUT NO LATER THAN Sept. 28, 8:00pm

1. Compute the partial derivatives with respect to  $x$  and  $y$ .

$$z = \ln(x^2 + y^3)$$

w/ respect to:

$$\begin{aligned} \frac{x}{z} &= \ln(x^2 + y^3) = \\ \frac{1}{x^2 + y^3} \cdot \frac{\partial}{\partial x} (\ln(x^2 + y^3)) &= \\ \frac{1}{x^2 + y^3} \cdot 2x &= 0 \\ \boxed{z' = \frac{2x}{x^2 + y^3}} \end{aligned}$$

$$\begin{aligned} \frac{y}{z} &= \ln(x^2 + y^3) = \\ \frac{1}{x^2 + y^3} \cdot \frac{\partial}{\partial y} (\ln(x^2 + y^3)) &= \\ \frac{1}{x^2 + y^3} \cdot 3y &= 0 \\ \boxed{z' = \frac{3y}{x^2 + y^3}} \end{aligned}$$

2. Find an equation of the tangent plane to the given surface at the specified point.

B  $z = x^2 + y^2 + 2$  ,  $(1, 1, 4)$  .

$$f(x, y) = x^2 + y^2 + 2$$

$$\left. \begin{aligned} f_x &= 2x \rightarrow f(1) = 2 \\ f_y &= 2y \rightarrow f(1) = 2 \end{aligned} \right\} \rightarrow \begin{aligned} z - z_0 &= f_x(x_0) \cdot (x - x_0) + f_y(x_0) \cdot (y - y_0) = \\ &= 2 \cdot (x - 1) + 2 \cdot (y - 1) = z \\ 2x - 2 + 2y - 2 &= z \end{aligned}$$

$$\boxed{2x + 2y - z - 2 = 0}$$