

“QUIZ” for Lecture 6

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q6FirstLast.pdf) ASAP BUT NO LATER THAN Sept. 24, 8:00pm

1. Find the limit if it exists, or show that the limit does not exist.

$$\lim_{(x,y) \rightarrow (0,0)} \frac{2x}{2x + 3y} .$$

Both top and bottom vanish when we plug-in $(x, y) = (0, 0)$ so we must go on.

Plug in $y=cx$
 $\lim_{x \rightarrow 0} \frac{2x}{2x+3cx}$
 $= \lim_{x \rightarrow 0} \frac{2x}{x(2+3c)}$
 $= \lim_{x \rightarrow 0} \frac{2}{2+3c}$
 $= \frac{2}{2+3c}$

The limit does not exist since you get different limits when you approach the point $(0, 0)$ on different lines.

2. Find the limit if it exists, or show that the limit does not exist.

$$\lim_{(x,y) \rightarrow (0,0)} \frac{x^5}{x^2 + y^2} .$$

Both top and bottom vanish when we plug-in $(x, y) = (0, 0)$ so we must go on.

Plug in $y=cx$
 $\lim_{x \rightarrow 0} \frac{x^5}{x^2+c^2x^2}$
 $= \lim_{x \rightarrow 0} \frac{x^5}{x^2(1+c^2)}$
 $= \lim_{x \rightarrow 0} \frac{x^3}{1+c^2}$
 $= 0$

: The limit exists and equals 0.