

“QUIZ” for Lecture 5

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22, 23, 24

NAME: (print!) \_\_\_\_\_

Section: \_\_\_\_\_

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q5FirstLast.pdf) ASAP BUT NO LATER THAN Sept. 21, 8:00pm

1, Find the curvature for

$$\mathbf{r}(t) = \sin t \mathbf{i} + \cos t \mathbf{j} + t \mathbf{k} \quad .$$

$$\begin{aligned} \mathbf{r}'(t) &= \cos t \mathbf{i} - \sin t \mathbf{j} + \mathbf{k} \\ \mathbf{r}''(t) &= -\sin t \mathbf{i} - \cos t \mathbf{j} + 0 \end{aligned}$$

$$\begin{aligned} \mathbf{r}'(t) \cdot \mathbf{r}''(t) &= \langle \cos t, \sin t, -\cos^2 t - \sin^2 t \rangle \\ |\mathbf{r}'(t) \cdot \mathbf{r}''(t)| &= \sqrt{(\cos^2 t + \sin^2 t + (-\cos^2 t - \sin^2 t)^2)} \\ |\mathbf{r}'(t)| &= \sqrt{\cos^2 t + (-\sin t)^2 + 1^2} \\ \kappa(t) &= \frac{\sqrt{\cos^2 t + \sin^2 t + (-\cos^2 t - \sin^2 t)^2}}{(\sqrt{\cos^2 t + (-\sin t)^2 + 1^2})^3} \end{aligned}$$

2.: Find the velocity, acceleration, and speed of a particle with the given position function.

$$\mathbf{r}(t) = t \mathbf{i} + t^2 \mathbf{j} + 5 \mathbf{k} \quad .$$

$$\begin{aligned} \mathbf{v}(t) = \mathbf{r}'(t) &= 1 \mathbf{i} + 2t \mathbf{j} + 0 \mathbf{k} \\ \mathbf{a}(t) = \mathbf{v}'(t) &= 0 \mathbf{i} + 2 \mathbf{j} + 0 \mathbf{k} \\ \text{speed } |\mathbf{v}(t)| &= \sqrt{1^2 + 2t^2 + 0} = \sqrt{1 + 4t^2} \end{aligned}$$