

“QUIZ” for Lecture 4

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E-MAILSCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q4FirstLast.pdf) ASAP BUT NO LATER THAN Sept. 17, 8:00pm

1. Find a parametric equation for the tangent line to the curve with the given parametric equation at the specified point

$$x = \cos t, \quad y = \sin t, \quad z = t^2 + 1; \quad (1, 0, 1)$$

$$\begin{aligned} \cos t_0 &= 1, \quad \sin t_0 = 0, \quad t_0^2 + 1 = 1 \\ t_0 &= 0 \\ \mathbf{r}(t) &= \langle \cos t, \sin t, t^2 + 1 \rangle \\ \mathbf{r}'(t) &= \langle -\sin t, \cos t, 2t \rangle \\ (1, 0, 1) + t \langle 0, 1, 0 \rangle \\ &= \langle 1, t, 1 \rangle \\ x &= 1, \quad y = t, \quad z = 1 \end{aligned}$$

2. Find $\mathbf{r}(t)$ if

$$\mathbf{r}'(t) = t\mathbf{i} + 2\mathbf{j} + (t+1)\mathbf{k}$$

and

$$\mathbf{r}(0) = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k}.$$

$$\begin{aligned} \mathbf{r}(t) &= \int (t\mathbf{i} + 2\mathbf{j} + (t+1)\mathbf{k}) dt \\ &= \left(\frac{t^2}{2}\right)\mathbf{i} + 2t\mathbf{j} + \left(\frac{(t+1)^2}{2}\right)\mathbf{k} + \mathbf{C} \\ \mathbf{r}(0) &= 0\mathbf{i} + 0\mathbf{j} + \frac{1}{2}\mathbf{k} + \mathbf{C} = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k} \\ \mathbf{C} &= \mathbf{i} + 2\mathbf{j} + \frac{5}{2}\mathbf{k} \\ \mathbf{r}(t) &= \left(\frac{t^2}{2}\right)\mathbf{i} + 2t\mathbf{j} + \left(\frac{(t+1)^2}{2}\right)\mathbf{k} + \mathbf{i} + 2\mathbf{j} + \frac{5}{2}\mathbf{k} \\ &= \left(\frac{t^2}{2} + 1\right)\mathbf{i} + (2t + 2)\mathbf{j} + \left(\frac{(t+1)^2}{2} + \frac{5}{2}\right)\mathbf{k} \end{aligned}$$