

q4 Rahul Paleja

section 22

- ① Find a parametric equation for the tangent line to the curve with the given parametric equation at the specified point

$$x = \cos t, y = \sin t, z = t^2 + 1; (1, 0, 1)$$

$$1 = \cos t$$

$$0 = \sin t$$

$$1 = t^2 + 1$$

$$0 = t$$

$$0 = t$$

$$0 = t$$

$$r(t) = \langle \cos t, \sin t, t^2 + 1 \rangle$$

$$r'(t) = \langle -\sin t, \cos t, 2t \rangle$$

$$r'(0) = \langle 0, 1, 0 \rangle$$

Equation of Tangent line in vector form:

$$\langle 1, 0, 1 \rangle + t \langle 0, 1, 0 \rangle = \langle 1, t, 1 \rangle$$

$$x = 1 \quad y = t \quad z = 1$$

②

$$r(t) = \int (t\mathbf{i} + 2\mathbf{j} + (t+1)\mathbf{k}) dt$$

$$= \int (t\mathbf{i} + 2\mathbf{j} + \mathbf{k} + t\mathbf{k}) dt$$

$$= \frac{t^2}{2} \mathbf{i} + 2t \mathbf{j} + \frac{t^2}{2} \mathbf{k} + t \mathbf{k} + C$$

$$= \frac{t^2}{2} \mathbf{i} + 2t \mathbf{j} + \left(\frac{t^2}{2} + t \right) \mathbf{k} + C$$

$$r(0) = 0 + 0 + 0 + C = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$$

$$r(t) = \frac{t^2}{2} \mathbf{i} + 2t \mathbf{j} + \left(\frac{t^2}{2} + t \right) \mathbf{k} + \mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$$

$$r(t) = \left(\frac{t^2}{2} + 1 \right) \mathbf{i} + (2t + 2) \mathbf{j} + \left(\frac{t^2}{2} + t + 3 \right) \mathbf{k}$$