

“QUIZ” for Lecture 4

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Section:24

E-MAILSCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q4FirstLast.pdf) ASAP BUT NO LATER THAN Sept. 17, 8:00pm

1. Find a parametric equation for the tangent line to the curve with the given parametric equation at the specified point

$$x = \cos t, \quad y = \sin t, \quad z = t^2 + 1; \quad (1, 0, 1)$$

$$x' = -\sin t \quad y' = \cos t \quad z' = 2t$$

$$\begin{cases} \cos t = 1 \\ \sin t = 0 \\ t^2 + 1 = 1 \end{cases} \rightarrow t = 0 \rightarrow \begin{cases} x' = 0 \\ y' = 1 \\ z' = 2 \end{cases}$$

$$\text{The tangent line is } f(t) = \begin{cases} 1 \\ t \\ 1 + 2 * t \end{cases}$$

2. Find $\mathbf{r}(t)$ if

$$\mathbf{r}'(t) = t \mathbf{i} + 2\mathbf{j} + (t + 1) \mathbf{k}$$

$$\mathbf{r}(0) = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k} \quad .$$

and

$$r(t) = \frac{t^2}{2} \mathbf{i} + 2t\mathbf{j} + \frac{t^2 + 2}{2} \mathbf{k} + c$$

$$r(t) = \frac{t^2 + 2}{2} \mathbf{i} + 2 * (t + 1)\mathbf{j} + \frac{t^2 + 6}{2} \mathbf{k}$$