

"QUIZ" for Lecture 3

E-MAILSCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q3FirstLast.pdf) ASAP BUT NO LATER THAN Sept. 15, 8:00pm

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P Q R

1. Find an equation of the plane that passes through the points (0, 1, 1), (1, 0, 1), (1, 1, 0).

$$\vec{PQ} = \langle 1, 0, 1 \rangle - \langle 0, 1, 1 \rangle = \langle 1, -1, 0 \rangle$$

$$\vec{PR} = \langle 1, 1, 0 \rangle - \langle 0, 1, 1 \rangle = \langle 1, 0, -1 \rangle$$

$$\begin{aligned} \vec{PQ} \times \vec{PR} &= \begin{vmatrix} i & j & k \\ 1 & -1 & 0 \\ 1 & 0 & -1 \end{vmatrix} = i((-1)(-1) - (0)(0)) - j((1)(-1) - (1)(0)) + k(1(0) - 1(-1)) \\ &= i(1-0) - j(-1-0) + k(0-(-1)) \\ &= i + j + k \implies \langle 1, 1, 1 \rangle \end{aligned}$$

$$(x-0) + (y-1) + (z-1) = 0$$

$$\boxed{x + (y-1) + (z-1) = 0}$$

2. Find the intersection of the line

$$\mathbf{r}(t) = \langle 1, 1, 0 \rangle + t\langle 0, 2, 4 \rangle$$

and the plane

$$x + y + z = 14$$

$$\begin{aligned} \mathbf{r}(t) &= \langle 1, 1, 0 \rangle + t\langle 0, 2, 4 \rangle \\ &= \langle 1, 1, 0 \rangle + \langle 0, 2t, 4t \rangle \\ &= \langle 1, 1+2t, 4t \rangle \end{aligned}$$

$$x=1 \quad y=2t \quad z=4t$$

$$1 + 2t + 4t = 14$$

$$6t = 13$$

$$t = \frac{13}{6}$$

$$\begin{array}{r} 1 + \frac{26}{6} + \frac{52}{6} \\ \frac{13}{3} + \frac{52}{6} \\ \frac{13}{3} + \frac{52}{6} \end{array}$$

$$\boxed{\langle 1, \frac{13}{3}, \frac{26}{3} \rangle}$$