

"QUIZ" for Lecture 3

E-MAILSCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q3FirstLast.pdf) ASAP BUT NO LATER THAN Sept. 15, 8:00pm

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1. Find an equation of the plane that passes through the points $(0, 1, 1)$, $(1, 0, 1)$, $(1, 1, 0)$.

$$u = \vec{PQ} = Q - P = (1, 0, 1) - (0, 1, 1) = \langle 1, -1, 0 \rangle$$

$$v = \vec{PR} = R - P = (1, 1, 0) - (0, 1, 1) = \langle 1, 0, -1 \rangle$$

$$u \times v = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -1 & 0 \\ 1 & 0 & -1 \end{vmatrix} = ((-1)(-1) - (0))\hat{i} - ((1)(-1) - (0))\hat{j} + (0 - (1)(-1))\hat{k} = \hat{i} + \hat{j} + \hat{k}$$

Point: $P = (0, 1, 1)$: $1(x-0) + 1(y-1) + 1(z-1) = 0$

$$x + y - 1 + z - 1 = 0$$

$$\boxed{x + y + z = 2}$$

2. Find the intersection of the line

$$\mathbf{r}(t) = \langle 1, 1, 0 \rangle + t\langle 0, 2, 4 \rangle$$

and the plane

$$x + y + z = 14$$

$$\mathbf{r}(t) = \langle 1, 1, 0 \rangle + \langle 0, 2t, 4t \rangle$$

$$\mathbf{r}(t) = \langle 1, 1+2t, 4t \rangle$$

$$x = 1$$

$$y = 1 + 2t$$

$$z = 4t$$

$$1 + (1+2t) + (4t) = 14$$

$$2 + 6t = 14$$

$$6t = 12$$

$$t = 2$$

$$\mathbf{r}(2) = \langle 1, 1, 0 \rangle + \langle 0, 4, 8 \rangle$$

$$= \boxed{\langle 1, 5, 8 \rangle}$$