

"QUIZ" for Lecture 3

E-MAILSCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q3FirstLast.pdf) ASAP BUT NO LATER THAN Sept. 15, 8:00pm

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1. Find an equation of the plane that passes through the points $\overset{P}{(0, 1, 1)}$, $\overset{Q}{(1, 0, 1)}$, $\overset{R}{(1, 1, 0)}$.

$$u = \overrightarrow{PQ} = [1-0, 0-1, 1-1] = [1, -1, 0]$$

$$v = \overrightarrow{PR} = [1-0, 1-1, 0-1] = [1, 0, -1]$$

$$\begin{aligned} u \times v &= [u_2v_3 - v_2u_3, v_1u_3 - u_1v_3, u_1v_2 - v_1u_2] \\ &= [(-1)(-1) - (0)(0), (1)(0) - (1)(-1), (1)(0) - (1)(-1)] \\ &= [1-0, 0+1, 1+1] = [1, 1, 2] \quad (\text{pick point P}) \end{aligned}$$

$$1(x-0) + 1(y-1) + 2(z-1) = 0$$

$$x + y + 2z = 3$$

2. Find the intersection of the line

$$r(t) = \langle 1, 1, 0 \rangle + t\langle 0, 2, 4 \rangle$$

and the plane

$$x + y + z = 14$$

$$r(t) = \langle 1+0, 1+2t, 0+4t \rangle = \langle 1, 1+2t, 4t \rangle$$

$$(1) + (1+2t) + (4t) = 14$$

$$2 + 6t = 14$$

$$t = 6$$

$$r(6) = \langle 1, 1, 0 \rangle + 6\langle 0, 2, 4 \rangle$$

$$= \langle 1, 1, 0 \rangle + \langle 0, 12, 24 \rangle$$

$$= \langle 1, 13, 24 \rangle$$