

Quiz 3 Sammy (Zixin Qu)

Q1. Let P be $(0, 1, 1)$, Q be $(1, 0, 1)$, R be $(1, 1, 0)$

$$U = \vec{PQ} = Q - P = (1, 0, 1) - (0, 1, 1) = (1, -1, 0)$$

$$V = \vec{PR} = R - P = (1, 1, 0) - (0, 1, 1) = (1, 0, -1)$$

$$\therefore CR = (1, -1, 0) \times (1, 0, -1) = \begin{vmatrix} i & j & k \\ 1 & -1 & 0 \\ 1 & 0 & -1 \end{vmatrix}$$

$$= (-1)i + (-1+0)j + (0+1)k$$

$$= i + j + k = (1, 1, 1)$$

Let point Q be the favorite point.

$$(x-1)i + (y-0)j + (z-1)k = 0$$

$$x-1 + y + z - 1 = 0$$

$$x + y + z = 2$$

Q2. Find the intersect of the line $r(t) = (1, 1, 0) + t(0, 2, 4)$

and the plane $x + y + z = 14$

$$r(t) = (1, 1, 0) + (0, 2t, 4t)$$

$$= (1, 1+2t, 4t)$$

$$\therefore x + y + z = 14$$

$$\therefore 1 + 1 + 2t + 4t = 14$$

$$6t = 12$$

$$t = 2$$

$$\text{so } r(t) = (1, 5, 8)$$

