

# Jessimo Kulu calc homework

16.2

8)  $F = \langle y^2, x^2 \rangle$ ;  $C: y = x^{-1}$  for  $1 \leq x \leq 2$

from left to right

a)  $F(r(t)), dr = r'(t) dt$  for  $r(t) = \langle t, t^{-1} \rangle$

$x = t \quad y = t^{-1}$

$F(r(t)) = \langle t, t^{-1} \rangle \quad dr = \langle dt, -t^{-2} dt \rangle$

$F(r(t)) \cdot dr = (t^{-2} - 1) dt$

$\int_1^2 (t^{-2} - 1) dt = -1/2$

9)  $F(x, y) = \sqrt{1+9xy}$   $y = x^3$  for  $0 \leq x \leq 1$

$r(t) = \langle t, t^3 \rangle \rightarrow \|r'(t)\| = \sqrt{1+9t^4}$

$\int_0^1 \sqrt{1+9t^4} \cdot \sqrt{1+9t^4} dt = 2.8$  with Maple

11)  $f(x, y, z) = z^2$   $r(t) = \langle 2t, 3t, 4t \rangle$   $0 \leq t \leq 1$

$x = 2t \quad y = 3t \quad z = 4t \quad f(r(t)) = 16t^2$

$ds = \|r'(t)\| dt = \sqrt{29} dt \rightarrow \int_0^1 16t^2 \sqrt{29} dt$

$= \frac{128\sqrt{29}}{3}$  with Maple

13)  $F(x, y, z) = xe^{2z}$ , point  $(0, 0, 1)$  to  $(0, 2, 0)$

$\int F(r(t)) ds \quad \left\{ \begin{array}{l} r(t) = \langle 0, 0, 1 \rangle + t \langle 0, 2, 0 \rangle = \langle 0, 2t, 1 \rangle \\ x = 0 \quad y = 2t \quad y' = 2 \quad dt \quad z = 1 \quad dz = 0 \end{array} \right.$

$\int \frac{1}{\sqrt{3}} t e^{2z} dt = \frac{\sqrt{3}}{2} e^{2z} \Big|_0^1 = \frac{\sqrt{3}e}{2} - \frac{\sqrt{3}}{2} =$

$u = t^2 \rightarrow [0, 1]$

$$\frac{dy}{y} = \frac{1}{y} dy$$

$$17) \int_C \frac{1}{\sqrt{y^2 + z^2}} ds : r(t) = \langle 4t, -3t, t \rangle \quad t=0 \text{ and } t=2$$

$$\|r'(t)\| = \sqrt{4^2 + 3^2 + 1^2} = \sqrt{26}$$

$\int_0^2 \frac{1}{\sqrt{26}} dt = \frac{2}{\sqrt{26}}$  the integral represents the distance between the points  $(0, -6, 0)$  and  $(8, 9, 2)$

$$27) \int_C 4dx - xdy \quad \text{parabola } y = x^2 \text{ for } 0 \leq x \leq 2$$

$$r(t) = \langle t, t^2 \rangle$$

$$x = t \quad y = t^2 \quad dx = dt \quad dy = 2t dt$$

$$\int_0^2 t^2 dt - t(2t dt) = -\frac{8}{3}$$

$$29) \int_C (x-y) dx + (y-2) dy + z dz$$

the segment  $(0, 0, 0)$  to  $(1, 4, 4)$

$$r(t) = t \langle 1, 4, 4 \rangle = \langle t, 4t, 4t \rangle$$

$$x = t \quad dx = dt \quad y = 4t \quad dy = 4 dt \quad z = 4t \quad dz = 4 dt$$

$$31) \int_C \frac{-y dx + x dy}{x^2 + y^2} \quad \text{line segment } (0, 0, 0) \text{ to } (2, 4, 4)$$

$$r(t) = t \langle 2, 4, 4 \rangle = \langle 2t, 4t, 4t \rangle$$

$$x = 2t \quad dx = 2 dt \quad y = 4t \quad dy = 4 dt \quad z = 4t$$

$$2.5) \int_{S_A} F(x,y,z) ds + \int_{S_B} F(x,y,z) ds \downarrow$$

$$\int_{S_B} F(x,y,z) ds \quad F(x,y,z) = e^z, e^{x^2}, e^y$$

$$\textcircled{1} \int_{S_A} \langle e, 1, 1 \rangle \cdot \langle 0, 0, 1 \rangle dt = 1$$

$$r_{pA}(t) = \langle 0, 0, t \rangle$$

$$\|r_{pA}'\| = 1$$

$$\textcircled{2} \int_{S_B} \langle e^t, e^{-t}, e^t \rangle \cdot \langle 0, 1, 1 \rangle dt = \int_0^1 e^{-t} + e^t dt \checkmark$$

# Teste me BME 163 Calculo Vectorial

1)  $F(x,y,z) = xy \sin(2z)$

$F(1,1,0) - F(0,0,0) = 0$  C:  $(0,0,0)$  to  $(1,1,0)$

means  $F$  is conservative

3)  $F(x,y) = (3, 6y)$   $F(x,y) = 3x + 3y^2$

$\nabla F \cdot R$   $\nabla F = (3, 6y)$

$F(9,1) - F(1,1) = -9/4$

$r(t) = \langle t, t^2 \rangle$   $r(0) = \langle 1, 1 \rangle$   $r(1) = \langle 4, 16 \rangle$

5)  $F(x,y) = y e^{2x} i + x e^{2y} j + x y e^{2z} k$

$F(x,y,z) = x y e^z$   $r(t) = \langle t^2, t^3, t \rangle$

$\nabla F = \langle y e^z, x e^z, x y e^z \rangle$

$F(4,2,1) - F(1,1,0) = 3e^{-1}$

9)  $F = y^2 i + (2xy + e^z) j + y e^{2x} k$

$\int y^2 dx = xy^2 + g(y,z)$

$\int (2xy + e^z) dy = xy^2 + y e^z + g(x,z)$

$\int y e^{2x} dz = y e^{2x} + g(x,y)$

13)  $r = \langle 2s \cos^2 t, z, y \ln t \rangle$

curl  $P = \langle \frac{d}{dx}, \frac{d}{dy}, \frac{d}{dz} \rangle \cdot \langle 2x e^{2x}, z, y \ln t \rangle$

$\int 2x e^{2x} dx = 2 \ln(x) + g(y, z)$

$yz + 2kx$

$\int z dy = yz + g(x, z)$

$\int y \ln t dz = yz + 2kx + g(x, y)$

10)  $\int (2xy^2 dx + x^2 z dy + x^2 y dz)$

over the path  $r(t) = \langle t^2, \sin(t), t \rangle e^{t-z}$

for  $0 \leq t \leq 2$

$r(t) = \langle t^2, \sin(t), t \rangle e^{t-z}$

$$r(t) = C_0 + \int_0^t \omega \left( \frac{r}{\omega} \right) e^{-\omega(t-\tau)} d\tau \quad \checkmark$$

19)  $f = x^2 y - z$   $r_1 = (t, t, 1)$  for  $0 \leq t \leq 1$   
and  $r_2 = (t, t^2, 0)$  for  $0 \leq t \leq 1$

$$\int_C F \cdot dr = F(r_1(1)) - F(r_1(0)) \quad \checkmark$$