

"QUIZ" for Lecture 24

NAME: (print!) Gillian Mulvay Section: _____

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q24FirstLast.pdf) ASAP BUT NO LATER THAN Dec. 4, 2020, 8:00pm

By using Stokes' Theorem, or otherwise, evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$, where

$$\mathbf{F}(x, y, z) = (yz + 2y + 3z)\mathbf{i} + (xz + 2x + 4z)\mathbf{j} + (xy + 3x + 4y)\mathbf{k}$$

where C is the curve of intersection of the plane $x + y + z = 1$ and the cylinder $x^2 + y^2 = 1$, oriented counterclockwise as viewed from above. Be sure to explain everything.

$F_{\text{curl}}(F) =$

$$\begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ yz + 2y + 3z & xz + 2x + 4z & xy + 3x + 4y \end{vmatrix} =$$

$$(x + 4 - x - 4)\mathbf{i} - (y + 3 - y - 3)\mathbf{j} + (z + 2 - z - 2)\mathbf{k}$$

$$0\mathbf{i} + 0\mathbf{j} + 0\mathbf{k} \quad \langle 0, 0, 0 \rangle$$

$$\int_C \mathbf{F} \cdot d\mathbf{r} = \int \text{curl}(\mathbf{F})$$

$$= \int \langle 0, 0, 0 \rangle$$

$$= 0$$

Since $\int_C \mathbf{F} \cdot d\mathbf{r} = \int \text{curl}(\mathbf{F})$ by the Stokes's Theorem, the first step is to find the curl. Since the curl gives a zero vector, the $\int \mathbf{F} \cdot d\mathbf{r}$ is 0.