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Question #1:

$$F(x, y, z) = \left\langle \underbrace{\cos(\sqrt{1-x^2} + zy^4)}_A, \underbrace{\tan(x^7 + y^2 + \frac{1}{z})}_B, \underbrace{\tan^{-1}(e^{xyz} + \cos^6(x^2 - y + 3z))}_C \right\rangle$$

$\langle P, Q, R \rangle = \text{curl } \vec{F}$

$$\text{curl } \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{d}{dx} & \frac{d}{dy} & \frac{d}{dz} \\ A & B & C \end{vmatrix}$$

$\text{div}(\text{curl } \vec{F}) = 0$  because from theorems we know that the divergence of a curl is 0.

Question #2:

$$F(x, y, z) = \langle 2x + y + z, x + 2y + z, x + y + 2z \rangle$$

$$\text{curl } \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{d}{dx} & \frac{d}{dy} & \frac{d}{dz} \\ \wedge \quad \begin{matrix} x+2y+z \\ 2x+y+z \end{matrix} & \wedge \quad \begin{matrix} x+2y+z \\ x+y+2z \end{matrix} & \wedge \quad \begin{matrix} x+2y+z \\ x+y+2z \end{matrix} \end{vmatrix}$$

$$= (x+2z - \cancel{2}x - 2y) \hat{i} - (y+2z - 2x - y) \hat{j} + (1+2y+z - 2x - 1 - z) \hat{k}$$

vector field is not conservative.