

"QUIZ" for Lecture 20

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Section: 23

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q20FirstLast.pdf) ASAP BUT NO LATER THAN Nov. 16, 8:00pm

1. Find an equation for the tangent plane to the parametric surface

$$x = v^2, \quad y = u + v, \quad z = u^2,$$

at the point (1, 2, 1). Simplify as much as you can!

$$r(t) = \langle v^2, u+v, u^2 \rangle$$

$$r_u = \langle 0, 1, 2u \rangle$$

$$r_v = \langle 2v, 1, 0 \rangle$$

$$1 = v^2, \quad 2 = u + v, \quad 1 = u^2$$

$v = -1$  or  $1$ ,  $u = -1$  or  $1$ , but only  $u=1$  and  $v=1$  work.

$$r_u = \langle 0, 1, 2 \rangle$$

$$r_v = \langle 2, 1, 0 \rangle$$

$$n = \langle 0, 1, 2 \rangle \times \langle 2, 1, 0 \rangle = \langle -2, 4, -2 \rangle$$

$$\langle x-1, y-2, z-1 \rangle \cdot \langle -2, 4, -2 \rangle = 0$$

$$\boxed{x - 2y + z = -2}$$

2. Evaluate the surface integral

$$\iint_S z \, dS,$$

where  $S$  is the triangular region with vertices (2, 0, 0), (0, 2, 0), (0, 0, 2).

$$x + y + z = 2$$

$$z = 2 - x - y$$

$$g(x, y) = 2 - x - y, \quad g_x = -1, \quad g_y = -1 \quad \text{and} \quad \sqrt{1 + 9x^2 + 9y^2} = \sqrt{3}$$

$$\iint_S z \, dS = \iint_D (2 - x - y) \sqrt{3}$$

$$D = \{ (x, y) \mid x \geq 0, y \geq 0, x + y \leq 2 \}$$

$$\int_0^2 \int_0^{2-x} \sqrt{3} \, dy \, dx$$

$$= \int_0^2 \sqrt{3} (2 - x) \, dx = \sqrt{3} \left( 2x - \frac{x^2}{2} \right) \Big|_0^2 = \boxed{2\sqrt{3}}$$