

"QUIZ" for Lecture 2

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E-MAIL ADDRESS SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com  
(Attachment: q2FirstLast.pdf) ASAP BUT NO LATER THAN FRIDAY Sept. 11,  
8:00pm \_\_\_\_\_

1. Determine whether the two vectors are orthogonal and if not, whether the angle between them is acute or obtuse. a.  $\langle 1, 1, 1 \rangle$  ,  $\langle 3, -2, -1 \rangle$  .

b.  $\langle 4, 3 \rangle$  ,  $\langle 2, -4 \rangle$  .

Two vectors are orthogonal if their dot product is equal to 0

$$\begin{aligned} \text{a) } \langle 1, 1, 1 \rangle \cdot \langle 3, -2, -1 \rangle &= (1 \cdot 3) + (1 \cdot -2) + (1 \cdot -1) = \\ &= 3 - 2 - 1 = 0 \rightarrow \text{Orthogonal} \end{aligned}$$

$$\theta = \cos^{-1} \left( \frac{\langle 1, 1, 1 \rangle \cdot \langle 3, -2, -1 \rangle}{\| \langle 1, 1, 1 \rangle \| \| \langle 3, -2, -1 \rangle \|} \right) = \cos^{-1} \left( \frac{0}{\sqrt{3} \cdot \sqrt{14}} \right) = \cos^{-1}(0) = 90^\circ$$

The angle between those vectors is a right angle.

$$\text{b) } \langle 4, 3 \rangle \cdot \langle 2, -4 \rangle = (4 \cdot 2) + (3 \cdot -4) = 8 - 12 = -4 \rightarrow \text{Not orthogonal}$$

$$\begin{aligned} \theta &= \cos^{-1} \left( \frac{\langle 4, 3 \rangle \cdot \langle 2, -4 \rangle}{\| \langle 4, 3 \rangle \| \| \langle 2, -4 \rangle \|} \right) = \cos^{-1} \left( \frac{-4}{\sqrt{16+9} \cdot \sqrt{4+16}} \right) = \cos^{-1} \left( \frac{-4}{\sqrt{25} \cdot \sqrt{20}} \right) = \\ &= \cos^{-1} \left( \frac{-4}{10\sqrt{5}} \right) \approx 100.3^\circ \rightarrow \text{The angle between those vectors is an} \\ &\text{obtuse angle.} \end{aligned}$$

2. Calculate  $\mathbf{v} \times \mathbf{w}$ , if

$$\mathbf{v} = \langle 0, 1, -1 \rangle \quad , \quad \mathbf{w} = \langle 1, -1, 0 \rangle .$$

$$\begin{aligned} \vec{v} \times \vec{w} &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 1 & -1 \\ 1 & -1 & 0 \end{vmatrix} = \hat{i} (1 \cdot 0 - (-1) \cdot (-1)) - \hat{j} (0 \cdot 0 - 1 \cdot (-1)) + \\ &\quad + \hat{k} (0 \cdot (-1) - 1 \cdot 1) = \\ &= -\hat{i} - \hat{j} - \hat{k} \rightarrow \langle -1, -1, -1 \rangle . \end{aligned}$$