

"QUIZ" for Lecture 16

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q16FirstLast.pdf) ASAP BUT NO LATER THAN Nov. 2, 8:00pm

1. Compute the Jacobian of the transformation

$$\Phi(r, s) = (rs, r + s) \quad x = rs \quad y = r + s$$

$$J = (x_r)(y_s) - (x_s)(y_r) = s - r$$

$$J = s - r$$

2. Let $D = \Phi(R)$ where $\Phi(u, v) = (u + v, v^2)$ and $R = [0, 6] \times [1, 2]$. Calculate

$$\iint_D y \, dA \quad J = x_u y_v - x_v y_u = (1)(2v) - (1)(0) = 2v$$

(Note: it is not necessary to compute D).

$$\iint_R y J \, dA = \iint_R (v^2)(2v) \, dA = \iint_R 2v^3 \, dA$$

$$\int_0^6 \int_1^2 2v^3 \, dv \, du = 45$$