

"QUIZ" for Lecture 15

NAME: (print!) _____ Section: _____

E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: qXFirstLast.pdf) ASAP BUT NO LATER THAN Oct. 29, 8:00pm

1. Use polar coordinates to compute the double integral

$$\iint_D xy \, dA \quad ,$$

where

$$D = \{(x, y) \mid x^2 + y^2 \leq 1, x \geq 0, y \geq 0\} \quad .$$

$$\iint_D r \cos \theta \, r \sin \theta \, dA$$

$$r^2 \leq 1$$

$$r \cos \theta \geq 0$$

$$r \sin \theta \geq 0$$

$$\int_0^1 r \cos \theta \sin \theta \, dr = r \cos(\theta) r \sin(\theta) =$$

$$\int_0^1 (\cos(\theta) \sin(\theta)) \, r^2 \, dr = \boxed{.4546}$$

2. Evaluate the iterated integral by converting it to polar coordinates

$$\int_0^1 \int_0^{\sqrt{1-y^2}} e^{x^2+y^2} \, dx \, dy \quad .$$

Note: The previous version had a typo ($dy \, dx$ instead of $dx \, dy$, that made it nonsense). I thank Yidi "Wendy" Weng for pointing it out (and see won a dollar).

$$f(r, \theta) = e^{(r \cos \theta)^2 + (r \sin \theta)^2} = e^{r^2 \cos^2 \theta + r^2 \sin^2 \theta} = e^{r^2 (\cos^2 \theta + \sin^2 \theta)} = e^{r^2}$$

$$= e^{r^2 \cos^2 \theta + r^2 \sin^2 \theta}$$

$$= e^{r(r \cos^2 \theta + r \sin^2 \theta)}$$

$$\int_0^1 \int_0^{\sqrt{1-y^2}} e^{r^2} \, d\theta \, dr$$

$$= \int_0^1 e^{r^2} \cdot \sqrt{1-r^2 \sin^2 \theta} \, dr = \cos \theta$$