

"QUIZ" for Lecture 14

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q14FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 26, 8:00pm

1. Evaluate the iterated integral

$$\int_0^1 \int_x^{3x} \int_0^y x^2 yz \, dz \, dy \, dx .$$

$$\int_0^y x^2 yz \, dz \rightarrow \frac{x^2 y z^2}{2} \Big|_0^y$$

$$\int_x^{3x} \frac{x^2 y^3}{2} \, dy \rightarrow \frac{x^2 y^4}{4} \Big|_x^{3x}$$

$$\int_0^1 20x^4 \, dx \rightarrow \frac{20x^5}{5} \Big|_0^1 = \boxed{\frac{20}{5}}$$

2. Evaluate the triple integral

$$\iiint_E yz \ln(x^5) \, dV ,$$

where

$$E = \{(x,y,z) | 0 \leq x \leq 1, 0 \leq y \leq x, 2x \leq z \leq 3x\}$$

$$\int_{2x}^{3x} yz \ln(x^5) \, dz \rightarrow \frac{5 \ln(x) y z^2}{2} \Big|_{2x}^{3x}$$

$$\int_0^x \frac{25x^2 \ln(x) y}{2} \, dy \rightarrow \frac{25x^2 \ln(x) y^2}{4} \Big|_0^x$$

$$\int_0^1 \frac{25x^4 \ln(x)}{4} \, dx \rightarrow \frac{x^5(5 \ln(x) - 1)}{4} \Big|_0^1 = \boxed{-\frac{1}{4}}$$