

“QUIZ” for Lecture 13

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q13FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 22, 8:00pm

1. Change the order of integration in

$$\int_1^4 \int_0^{\ln y} f(x, y) dx dy .$$

$x=0 \dots \ln y \quad y=1 \dots 4$
 $0 \leq x \leq \ln y \quad 1 \leq y \leq 4$
 $x = \ln y \quad y = e^x$
 $0 \leq x \leq \ln 4 \quad e^x \leq y \leq 4$
 $\int_1^4 \int_0^{\ln y} f(x, y) dy dx \quad y = e^x \dots 4 \quad x = 0 \dots \ln 4$

2. Evaluate

$$\int_0^2 \int_{y/2}^1 \frac{1}{(x^2 + 1)^2} dx dy ,$$

by inverting the order of integration and evaluating the new iterated integral.

$x=y/2 \dots 1 \quad y=0 \dots 2$
 $y/2 \leq x \leq 1 \quad 0 \leq y \leq 2$
 $y/2 = x \quad y = 2x$
 $0 \leq x \leq 1 \quad 0 \leq y \leq 2x$
 $\int_0^1 \int_0^{2x} \frac{1}{(x^2 + 1)^2} dy dx \quad y = 0 \dots 2x \quad x = 0 \dots 1$
 $= 1/2$