

Quiz 13

Q1. Change the order of integration in

$$\int_1^4 \int_0^{\ln y} f(x, y) dx dy$$

$$D = \{(x, y) \mid 1 \leq y \leq 4, 0 \leq x \leq \ln y\}$$

$$x = \ln y \quad y = e^x$$

$$\therefore \text{when } y=1 \quad x=0 \quad 0 \leq x \leq \ln 4$$

$$y=4 \quad x=\ln 4 \quad 1 \leq y \leq 4$$

~~$$\int_1^4 \int_0^{\ln y} f(x, y) dx dy$$~~

$$\int_0^{\ln 4} \int_{e^x}^4 f(x, y) dy dx$$

Q2. $\int_0^2 \int_{\frac{y}{2}}^1 \frac{1}{(x^2+1)^2} dx dy$

$$0 \leq y \leq 2$$

$$\frac{y}{2} \leq x \leq 1$$

$$x = \frac{y}{2}$$

$$y = 2x$$

$$\therefore 0 \leq y \leq 2x$$

$$0 \leq x \leq 1$$

$$\therefore \int_0^1 \int_0^{2x} \frac{1}{(x^2+1)^2} dy dx$$

$$= \frac{1}{2}$$

