

**“QUIZ” for Lecture 12**

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**E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q12FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 19 8:00pm**

1. Calculate the iterated integral

$$\int_1^2 \int_{-1}^1 (x + y^2) dx dy \quad .$$

$$\begin{aligned} \int (x + y^2) dx \quad x=-1..1 \\ =x^2/2+xy^2=2y^2 \end{aligned}$$

$$\begin{aligned} \int (2y^2) dy \quad y=1..2 \\ =2y^3/3=2*2^3/3-2*1^3/3=14/3 \end{aligned}$$

Ans: 14/3

2. Calculate the double integral

$$\int \int_R \frac{x^2 y}{x^3 + 1} dA \quad ,$$
$$R = \{(x, y) \mid 0 \leq x \leq 1, -1 \leq y \leq 1\} \quad .$$

$$\int \left( \int x^2 y / x^3 + 1 dy \right) dx \quad x=0..1 \quad y=-1..1$$

$$\begin{aligned} \int x^2 y / x^3 + 1 dy \quad y=-1..1 \\ =x^2 / x^3 + 1 * \int y dy \quad y=-1..1 \\ = (x^2 / x^3 + 1) * y^2 / 2 \\ = (x^2 / x^3 + 1) * 0 = 0 \end{aligned}$$

$$\begin{aligned} \int 0 dx \quad x=0..1 \\ 0x=0 \end{aligned}$$