

“QUIZ” for Lecture 11

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q11FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 12, 8:00pm Deadline extended to Oct. 17

1. Use Lagrange multipliers (no credit for other methods) to find the **smallest** value that $x + y + z$ can be, given that $xyz = 125$

$f_x=1$ $f_y=1$ $f_z=1$
 $\text{grad}f = \langle 1, 1, 1 \rangle$
 $g_x=yz$ $g_y=xz$ $g_z=xy$
 $\text{grad}g = \langle yz, xz, xy \rangle$
 $\text{grad}f = L \text{grad}g$
 $\langle 1, 1, 1 \rangle = L \langle yz, xz, xy \rangle$
 $1 = L yz$ $1 = L xz$ $1 = L xy$
 $xyz = 125$
 $1 = L^3 (xyz)^2$

$x=5$ $y=5$ $z=5$
which means the point $(5, 5, 5)$
plug in
 $5+5+5=15$
The smallest value is 15.

$1 = L^3 (x \cdot (1/L))^2$
 $x = \sqrt{1/L}$
 $1 = L^3 (y \cdot (1/L))^2$
 $y = \sqrt{1/L}$
 $1 = L^3 (z \cdot (1/L))^2$
 $z = \sqrt{1/L}$

$\sqrt{1/L} \cdot \sqrt{1/L} \cdot \sqrt{1/L} = 125$
 $L = 1/25$

2. Use Lagrange multipliers (no credit for other methods) to find the **largest** value that xyz can be, given that $x + y + z = 15$

$f_x=yz$ $f_y=xz$ $f_z=xy$
 $\text{grad}f = \langle yz, xz, xy \rangle$
 $g_x=1$ $g_y=1$ $g_z=1$
 $\text{grad}g = \langle 1, 1, 1 \rangle$
 $\text{grad}f = L \text{grad}g$
 $\langle yz, xz, xy \rangle = L \langle 1, 1, 1 \rangle$
 $yz=L$ $xz=L$ $xy=L$ $x + y + z = 15$
 $(xyz)^2 = L^3$

$(xL)^2 = L^3$
 $x = \sqrt{L}$
 $(yL)^2 = L^3$
 $y = \sqrt{L}$
 $(zL)^2 = L^3$
 $z = \sqrt{L}$
 $\sqrt{L} + \sqrt{L} + \sqrt{L} = 15$
 $L = 25$
 $x=5$ $y=5$ $z=5$
which means the point $(5, 5, 5)$
plug in $5 \cdot 5 \cdot 5 = 125$
the largest value is 125.