

"QUIZ" for Lecture 11

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q11FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 12, 8:00pm Deadline extended to Oct. 17

1. Use Lagrange multipliers (no credit for other methods) to find the **smallest** value that $x + y + z$ can be, given that $xyz = 125$

$$f(x, y, z) = x + y + z$$

$$\nabla f = \langle 1, 1, 1 \rangle$$

$$1 = \lambda yz \quad 1 = \lambda xz$$

$$1 = \lambda xy \quad 125 = xyz$$

$$g(x, y, z) = xyz = 125$$

$$\nabla g = \langle yz, xz, xy \rangle$$

Solved using MATLAB:

$$\lambda = \frac{1}{25} \text{ (and some imaginary sol'ns)}$$

$$x = y = z = 5$$

Ans: Smallest Value is $f(5, 5, 5) = 15$

2. Use Lagrange multipliers (no credit for other methods) to find the **largest** value that xyz can be, given that $x + y + z = 15$

$$f(x, y, z) = xyz$$

$$\nabla f = \langle yz, xz, xy \rangle$$

$$yz = \lambda \quad xz = \lambda$$

$$xy = \lambda \quad x + y + z = 15$$

$$g(x, y, z) = x + y + z = 15$$

$$\nabla g = \langle 1, 1, 1 \rangle$$

Solved in MATLAB:

When $\lambda = 25,$

$$x = 5, y = 5, z = 5$$

When $\lambda = 0,$
 $xyz = 0$

Ans: Largest value is $f(5, 5, 5) = 5^3 = 125$

(Am I allowed to use MATLAB in this way?)