

"QUIZ" for Lecture 11

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q11FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 12, 8:00pm Deadline extended to Oct. 17

1. Use Lagrange multipliers (no credit for other methods) to find the **smallest** value that  $x + y + z$  can be, given that  $xyz = 125$

$$\begin{aligned} \nabla f &= \langle 1, 1, 1 \rangle & \lambda \nabla f &= \nabla g \\ \nabla g &= \langle yz, xz, xy \rangle & \lambda \langle 1, 1, 1 \rangle &= \langle yz, xz, xy \rangle \\ & & \lambda &= yz \quad \lambda = xz \quad \lambda = xy \\ & & y &= \frac{\lambda}{z} \quad z = \frac{\lambda}{x} \quad x = \frac{\lambda}{y} \\ xyz &= \frac{\lambda^3}{xyz} & \lambda^3 &= 1 \quad \lambda = 1 \\ y &= \frac{1}{z} \quad z = \frac{1}{x} \quad x = \frac{1}{y} & f(5, 5, 5) &= 5 + 5 + 5 = \boxed{15} \\ y &= x \quad z = y \quad x = z \\ x &= y = z & \rightarrow x &= y = z = 5 \\ x^3 &= 125 \\ x &= 5 \end{aligned}$$

2. Use Lagrange multipliers (no credit for other methods) to find the **largest** value that  $xyz$  can be, given that  $x + y + z = 15$

$$\begin{aligned} \nabla f &= \langle yz, xz, xy \rangle & \nabla f &= \lambda \nabla g \\ \nabla g &= \langle 1, 1, 1 \rangle & \langle yz, xz, xy \rangle &= \lambda \langle 1, 1, 1 \rangle \\ & & yz &= \lambda \quad xz = \lambda \quad xy = \lambda \\ & & y &= \frac{\lambda}{z} \quad z = \frac{\lambda}{x} \quad x = \frac{\lambda}{y} \\ xyz &= \frac{\lambda^3}{xyz} \\ 1 &= \lambda^3 \\ \lambda &= 1 \\ y &= \frac{1}{z} \quad z = \frac{1}{x} \quad x = \frac{1}{y} & f(5, 5, 5) &= \boxed{125} \\ x &= y = z \\ 3x &= 15 \\ x &= 5 \end{aligned}$$