

Quiz for lecture 11.

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Section: 8:40-10:00 A.M.

1. Use Lagrange multipliers to find the smallest value that $x+y+z$ can be, given that $xyz=125$

$$f(x, y, z) = x+y+z$$

$$g(x, y, z) = xyz = 125.$$

$$\nabla f = \langle 1, 1, 1 \rangle, \nabla g = \langle yz, xz, xy \rangle.$$

$$\langle 1, 1, 1 \rangle = \lambda \langle yz, xz, xy \rangle.$$

$$\begin{cases} \lambda yz = 1 \\ \lambda xz = 1 \\ \lambda xy = 1. \end{cases}$$

$$\lambda^3 (xyz)^2 = 1$$

$$\lambda^3 = \frac{1}{125}$$

$$\lambda = \frac{1}{25}$$

$$x = y = z = \frac{125}{25} = 5$$

$$f(5, 5, 5) = 15$$

\therefore The minimum of $(x+y+z)$ is 15.



2. Use Lagrange multipliers to find the largest value that xyz can be, given that $x+y+z=15$.

$$f(x, y, z) = xyz$$

$$g(x, y, z) = x+y+z=15.$$

$$\nabla f = \langle yz, xz, xy \rangle.$$

$$\nabla g = \langle 1, 1, 1 \rangle$$

$$\langle yz, xz, xy \rangle = \lambda \langle 1, 1, 1 \rangle$$

$$\begin{cases} yz = \lambda \\ xz = \lambda \\ xy = \lambda \end{cases}$$

$$(xyz)^2 = \lambda^3$$

$$xyz = \lambda^{\frac{3}{2}}$$

$$yz = \frac{\lambda^{\frac{3}{2}}}{x} = \lambda$$

$$x = y = z = \lambda^{\frac{1}{2}}$$

$$3\lambda^{\frac{1}{2}} = 15$$

$$\lambda^{\frac{1}{2}} = 5.$$

$$\cancel{\lambda} \\ x = y = z = 5.$$

$$f(5, 5, 5) = 125.$$

\therefore The maximum of xyz is 125.

