

"QUIZ" for Lecture 10

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q10FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 8, 8:00pm

1. Find the local maximum and minimum point(s), the local maximum and minimum values, and saddle point(s) of the function

$$f(x, y) = 12x^2 - 4x^3 + 6y^2 + 12xy$$

$$f_x = 24x - 12x^2 + 12y$$

$$f_y = 12y + 12x$$

$$f_{xx} = 24 - 24x$$

$$f_{xy} = 12$$

$$f_{yy} = 12$$

$$24x - 12x^2 + 12y = 0, \quad 12y + 12x = 0$$

$$\begin{array}{r} 24x - 12x^2 + 12y = 0 \\ - \quad 12x + 12y = 0 \\ \hline \end{array}$$

$$12x - 12x^2 = 0$$

$$12x(1-x) = 0$$

$$x = 0, 1$$

$$y = 0, -1$$

critical points: $(0, 0), (1, -1)$

$$f_{xx}(0, 0) = 24$$

$$f_{xy}(0, 0) = 12$$

$$f_{yy}(0, 0) = 12$$

$$D = (24)(12) - 12^2 = 144$$

$$f_{xx}(1, -1) = 0$$

$$f_{xy}(1, -1) = 12$$

$$f_{yy}(1, -1) = 12$$

$$D = (0)(12) - 12^2 = -144$$

$(1, -1)$ saddle point

$(0, 0)$ local minimum

no local maximum