

LJ: 12.1, 12.2 Pdf Quiz

10/3/20

1. Show that the Δ w/ vertices $P = (1, 0, 0)$, $Q = (0, 1, 0)$, & $R = (0, 0, 1)$ is an equilateral Δ .

$$\text{dist}(P, Q) = \sqrt{(1-0)^2 + (0-1)^2 + (0-0)^2} = \sqrt{2}$$

$$\text{dist}(P, R) = \sqrt{(1-0)^2 + (0-0)^2 + (0-1)^2} = \sqrt{2}$$

$$\text{dist}(Q, R) = \sqrt{(0-0)^2 + (0-1)^2 + (1-0)^2} = \sqrt{2}$$

All 3 sides of ΔPQR have the same length ($\sqrt{2}$).
 $\Rightarrow \Delta$ is equilateral

2. Determine whether the following 2 lines ever meet. If they do meet, where?

$$r_1(t) = \langle 1, 0, 0 \rangle + t \langle 1, 2, 3 \rangle, \quad r_2(s) = \langle 0, 1, 0 \rangle + s \langle 2, 1, 3 \rangle$$

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$$r_1(t) = \langle 1+t, 2t, 3t \rangle, \quad r_2(s) = \langle 2s, 1+s, 3s \rangle$$

$$r_1(t) = r_2(s)$$

$$1+t = 2s$$

$$2t = 1+s$$

$$3t = 3s$$

$$2(1) = 1+1$$

$t=1, s=1$ (LINES MEET)

To find where lines meet, plug-in $t=1$ into $r_1(t)$

$$r_1(1) = \langle 1+1, 2 \cdot 1, 3 \cdot 1 \rangle = \langle 2, 2, 3 \rangle$$

To be safe, plug-in $s=1$ into $r_2(s)$

$$r_2(1) = \langle 2, 2, 3 \rangle$$

BEWARE: convert vector into a point

The 2 lines do intersect each other, & the intersection pt. is:
 $(2, 2, 3)$