

Dr. Z.'s Math 250(2), (Fall 2010, RU) REAL Quiz #2 (Sept. 23, 2010)

NAME: (print!) \_\_\_\_\_

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1. (4 pts.) Determine the value of  $r$ , if any, for which the given system of linear equations is **inconsistent**.

$$\begin{aligned}x_1 - x_2 + 2x_3 &= 4 \\3x_1 + rx_2 - x_3 &= 2 \quad .\end{aligned}$$

2. (4 pts.) Find a subset of the following set  $\mathcal{S}$  of vectors in  $\mathbb{R}^3$  with the same span as  $\mathcal{S}$  that is as small as possible.

$$\mathcal{S} = \left\{ \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 2 \\ 3 \\ 4 \end{bmatrix}, \begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix} \right\} .$$

3. True or False (Explain!, unexplained answered get no credit)

(a) (1 pt.) The number of rows in a matrix equals its rank.

(b) (1 pt.) If  $\mathbf{u}$  and  $\mathbf{v}$  are any two vectors in  $\mathbb{R}^2$ , then their span is the whole of  $\mathbb{R}^2$ .