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a)

(i) continuous

$$(ii) \frac{dx}{dt} = -2x$$

$$(iii) F(x) = -2x$$

$$(iv) -2x = 0$$

$\Rightarrow x=0$ is an eq. pt.

(v) $F'(0) = -2 < 0$, so it is stable.

b) (i) discrete

$$(ii) x(n) = \frac{1}{2} x(n-1)$$

$$(iii) f(x) = \frac{1}{2}x$$

$$(iv) x = \frac{1}{2}x$$

$\Rightarrow x = 0$ is a fixed pt.

(v) $f'(0) = \frac{1}{2} < 1$, so it is stable.

c) i) discrete

$$ii) x(n) = 2x(n-1) \cdot (1 - x(n-1))$$

$$(iii) f(x) = 2x(1-x)$$

$$(iv) x = 2x(1-x)$$

$$x = 0$$

$$1 = 2(1-x)$$

$$\frac{1}{2} = 1-x$$

$$x = 1 - \frac{1}{2} = \frac{1}{2}$$

so fixed pts are $x=0, \frac{1}{2}$

$$(v) f(x) = 2x - 2x^2$$

$$f'(x) = 2 - 4x$$

$$f'(0) = 2 > 1, \text{ so } x=0 \text{ is not stable}$$

$$f'(\frac{1}{2}) = 2 - 2 = 0 < 1, \text{ so } x=\frac{1}{2} \text{ is stable}$$

d) (i) continuous

$$(ii) \frac{dx}{dt} = 2x(1-x)$$

$$(iii) F(x) = 2x(1-x)$$

$$(iv) 2x(1-x) = 0$$

$\Rightarrow x=0, 1$ are the eq. pts

$$(v) F(x) = 2x - 2x^2$$

$$F'(x) = 2 - 4x$$

$$F'(0) = 2 > 0, \text{ so } 0 \text{ is not stable}$$

$$F'(1) = 2 - 4 = -2 < 0, \text{ so } 1 \text{ is stable}$$