

- > $SFP(f, x)$ [8.123105626] (4)
=> #Yes there is a steady state at 8.123105625 and it is stable.

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#2)
> f := x · (1 - x)                                f := x (1 - x)          (5)
=
> Orb(f, x, 0.5, 1, 1000)                         [0.25, 0.1875, 0.15234375, 0.1291351318, 0.1124592495, 0.09981216670, 0.08984969808,
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                                                0.04371482382, 0.04180383800, 0.04005627713, 0.03845177179, 0.03697323304, (6)

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► $SFP(f, x)$ [] (7)

$$\textcolor{red}{\triangleright} \quad f := 2x \cdot (1-x) \quad \quad \quad f := 2x(1-x) \quad \quad \quad (8)$$

> $Orb(f, x, 0.5, 1, 1000)$
 $[0.50, 0.5000, 0.50000000, 0.5000000000, 0.5000000000, 0.5000000000, 0.5000000000, \dots]$, (9)

> $SFP(f, x)$ [0.5000000000] (10)

$$\Rightarrow f := 2.5 x \cdot (1 - x) \quad (11)$$

$$SFP(f, x)$$

[0.6000000000] (13)

$$\textcolor{red}{\triangleright} \quad f := 3.1 x \cdot (1 - x) \quad \quad \quad f := 3.1 x (1 - x) \quad \quad \quad (14)$$

> $Orb(f, x, 0.5, 1, 1000)$

➤ $SFP(f, x)$ [] (16)

> $f := 3.5 x \cdot (1 - x)$ (17)

> $Orb(f, x, 0.5, 1, 1000)$
[0.875, 0.3828125, 0.8269348143, 0.5008976952, 0.8749971794, 0.3828199039, (18)

> $SFP(f, x)$

[]

(19)

- #Only when $k=2$ and $k=2.5$ will there be a stable fixed point

#3)

$$f := \text{rsolve}\left(\left\{x(n) - \frac{x(n-1) + 9x(n-2)}{x(n-1) + 6x(n-2)} = 0, x(0) = 0.5, x(1) = 0.7\right\}, x(n)\right)$$

$$f := \text{rsolve}\left(\left\{x(n) - \frac{x(n-1) + 9x(n-2)}{x(n-1) + 6x(n-2)} = 0, x(0) = 0.5, x(1) = 0.7\right\}, x(n)\right)$$

$$> Orb\left(\frac{1x - 9(x-1)}{1 + 6(x-1)}, x, 0.5, 1, 1000\right)$$

$$[-2.500000000, -1.450000000, -1.503649635, -1.499739719, -1.500018594, \dots]$$

#The steady state is at -1.5 .