

OK to post

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Homework 3

#3

$$a(n) = 3a(n-1) - 2a(n-2); \quad a(0) = 2 \quad a(1) = 3$$

$$a(2) = 3(3) - 2(2) = 5^{+2}$$

$$a(3) = 3(5) - 2(3) = 9^{+4}$$

$$a(4) = 3(9) - 2(5) = 17^{+8}$$

$$a(5) = 3(17) - 2(9) = 33^{+16}$$

$$a(n) = 2^n + 1 \quad \text{for } n \geq 0$$

#4

$$a(n) = 2a(n-1) + 2a(n-2) - 2a(n-3); \quad a(0) = 3 \quad a(1) = 2 \quad a(2) = 6$$

$$a(3) = 10$$

$$a(4) = 28$$

$$a(5) = 64$$

No discernable pattern, made didn't solve realistically either

$$\#5 \quad a(n) = a(n-4); \quad a(0) = 1 \quad a(1) = 0 \quad a(2) = 0 \quad a(3) = 0$$

$$a(4) = 1$$

$$a(5) = 0$$

$$a(6) = 0$$

$$a(7) = 0$$

$$a(8) = 1$$

Since a alternates every k where $k/4 = \text{an integer}$
the first thing that comes to mind is imaginary numbers

Since it alternates from 1 & 0 we need a function of i
that equals 1 when $n=4k$, & 0 everywhere else

$$a(n) = \frac{1}{4} + \frac{(i)^n}{4} + \frac{(-i)^n}{4} + \frac{(-1)^n}{4}$$