

OK to post

Anne Somalwar, hw25, 12/2/21

$$P1) \quad z^3 + 3(z)^2 - 11(z) + 2$$

$$= 8 + 12 - 22 + 2 = 0$$

so  $z=2$  is a solution.

$$z^3 + 3(z)^2 - 11(z) + 2$$

$$= 27 + 27 - 33 + 2 \neq 0$$

so  $z=3$  is not a solution.

$$P2) \quad \sin \pi = 0$$

so  $\pi$  is a solution.

$$\sin \frac{\pi}{2} = 1$$

so  $\frac{\pi}{2}$  is not a solution.

P3)  $\forall r \in \mathbb{R} \quad \sin^2 r + \cos^2 r = 1,$

so both are solutions.

P4)  $\mathbb{R}$

P5)  $x(t) = t^4$

$$x'(t) = 4t^3 \Rightarrow x'(2) = 32$$

$$x''(t) = 12t^2 \Rightarrow x''(2) = 48$$

$$P6) \quad f(1) = 0 + 1 = 1, \quad \boxed{\text{so } 1 \text{ is fixed.}}$$

$$f(2) = 0 + 2 = 2 \quad \boxed{\text{so } 2 \text{ is fixed}}$$

$$f(3) = 0 + 3 = 3 \quad \boxed{\text{so } 3 \text{ is fixed}}$$

$$f(-1) = (-2)(-3)(-4) - 1 \neq -1$$

$$\boxed{\text{so } -1 \text{ is not fixed}}$$

$$P7) \quad f(0, 1) = (0 - 1 + 1, 0 + 1 - 2)$$

$$= (0, -1) \quad \boxed{\text{so } (0, -1) \text{ is a fixed pt.}}$$

$$P8) \quad f(x) = \frac{1}{x+1}$$

$$(i) \quad x(0) = 0.5$$

$$x(1) = \frac{1}{3/2} = \frac{2}{3}$$

$$x(2) = \frac{1}{1 + \frac{2}{3}} = \frac{1}{\frac{5}{3}} = \frac{3}{5}$$

$$(ii) \quad \text{Orb}([1/(x+1)], [x], [0.5], 0, 2)$$

$$(iii) \quad \text{Orb}([1/(x+1)], [x], [0.5], 1000, 1000) [1]$$

0.61803...

$$p9) \quad f(x, y, z) = \left( \frac{x}{1+y+z}, \frac{y}{1+x+z}, \frac{z}{1+x+y} \right)$$

$$f(0, 0, 0) = (1, 1, 1)$$

$$f(1, 1, 1) = \left( \frac{1}{1+1+1}, \frac{1}{1+1+1}, \frac{1}{1+1+1} \right)$$

$$= \left( \frac{1}{3}, \frac{1}{3}, \frac{1}{3} \right)$$

$$f\left(\frac{1}{3}, \frac{1}{3}, \frac{1}{3}\right) = \left( \frac{\frac{1}{3}}{1+\frac{1}{3}+\frac{1}{3}}, \frac{\frac{1}{3}}{1+\frac{1}{3}+\frac{1}{3}}, \frac{\frac{1}{3}}{1+\frac{1}{3}+\frac{1}{3}} \right)$$

$$= \left( \frac{1}{5}, \frac{1}{5}, \frac{1}{5} \right)$$

(ii)  $\text{Orb}([x/(1+y+z), y/(1+x+z), z/(1+x+y)],$   
 $[x, y, z], [1.0, 1.0, 1.0], 0, 2)$

(iii)  $\text{Orb}([x/(1+y+z), y/(1+x+z), z/(1+x+y)],$   
 $[x, y, z], [1.0, 1.0, 1.0], 1000, 1000)[1]$

$$\Rightarrow [0.0004997\dots, 0.0004997\dots, 0.0004997\dots]$$

$$P(1) \quad x = x^2 - 2x + 2$$

$$x^2 - 3x + 2 = 0$$

$$(x-2)(x-1) = 0$$

$$x = 1, 2$$

$$P(2) \quad x = \frac{5}{2}x(1-x)$$

$$x=0$$

$$1 = \frac{5}{2}(1-x)$$

$$\frac{2}{5} = 1-x$$

$$x = \frac{3}{5}$$

$$x = 0, \frac{3}{5}$$

$$P(3) \quad x = kx(1-x)$$

$$x=0$$

$$1 = k(1-x)$$

$$1/k = 1-x$$

$$x = 1 - 1/k$$

$$\boxed{x=0, 1-1/k}$$

$$P(11'') \quad f(x) = x^2 - 2x + 2$$

$$f'(x) = 2x - 2$$

$$f'(1) = 2 - 2 = 0 < 1 \quad \boxed{\text{so 1 is stable}}$$

$$f'(2) = 4 - 2 = 2 > 1 \quad \text{so } \boxed{2 \text{ is not stable}}$$

$$P12'') \quad f(x) = \frac{5}{2}x(1-x) = \frac{5}{2}x - \frac{5}{2}x^2$$

$$f'(x) = \frac{5}{2} - 5x$$

$$f'(0) = \frac{5}{2} > 1 \quad \boxed{\text{so } 0 \text{ is not stable}}$$

$$f'(3/5) = \frac{5}{2} - 3 = -\frac{1}{2}$$

$$|-\frac{1}{2}| < 1 \quad \boxed{\text{so } 3/5 \text{ is stable}}$$