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> #OK to post
>
>
> #Anne Somalwar, hw19, 11.7.2021
>
>
>
> read "C:/Users/aks238/OneDrive - Rutgers University/Documents/M19.txt"
>
>
>
>
> #I
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> #(i)
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>
> SIRSDemo(1000, 200, 3, 1, 0.01, 10)

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*This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, 10*

*with population size, 1000, and fixed parameters nu=, 1, and gamma=, 3  
where we change beta from 0.2\*nu/N to 4\*nu/N*

*Recall that the epidemic will persist if beta exceeds nu/N, that in this case is,  $\frac{1}{1000}$*

*We start with , 200, infected individuals, 0 removed and hence, 800, susceptible*

*We will show what happens once time is close to, 10*

*beta is,  $\frac{1}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [998.9666995, 0.9909989667]], [9.99, [998.9666995, 0.9909989667]], [10.00, [998.9666995, 0.9909989667]], [10.01, [998.9666995, 0.9909989667]]]*

*beta is,  $\frac{3}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [996.7009881, 2.978970309]], [9.99, [996.7009881, 2.978970309]], [10.00, [996.7009881, 2.978970309]], [10.01, [996.7009881, 2.978970309]]]*

*beta is,  $\frac{1}{2}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [994.1715221, 4.974854288]], [9.99, [994.1715221, 4.974854288]], [10.00,*

[994.1715221, 4.974854288]], [10.01, [994.1715221, 4.974854288]]]

*beta is,  $\frac{7}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [991.3807432, 6.978577656]], [9.99, [991.3807432, 6.978577656]], [10.00, [991.3807432, 6.978577656]], [10.01, [991.3807432, 6.978577656]]]

*beta is,  $\frac{9}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [988.3315033, 8.990054852]], [9.99, [988.3315033, 8.990054852]], [10.00, [988.3315033, 8.990054852]], [10.01, [988.3315033, 8.990054852]]]

*beta is,  $\frac{11}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [985.0270559, 11.00918827]], [9.99, [985.0270559, 11.00918827]], [10.00, [985.0270559, 11.00918827]], [10.01, [985.0270559, 11.00918827]]]

*beta is,  $\frac{13}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [981.4710448, 13.03586861]], [9.99, [981.4710448, 13.03586861]], [10.00, [981.4710448, 13.03586861]], [10.01, [981.4710448, 13.03586861]]]

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [977.6674922, 15.06997519]], [9.99, [977.6674922, 15.06997519]], [10.00, [977.6674922, 15.06997519]], [10.01, [977.6674922, 15.06997519]]]

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [973.6207848, 17.11137641]], [9.99, [973.6207848, 17.11137641]], [10.00, [973.6207848, 17.11137641]], [10.01, [973.6207848, 17.11137641]]]

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [969.3356593, 19.15993017]], [9.99, [969.3356593, 19.15993017]], [10.00, [969.3356593, 19.15993017]], [10.01, [969.3356593, 19.15993017]]]

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [964.8171858, 21.21548438]], [9.99, [964.8171858, 21.21548438]], [10.00, [964.8171858, 21.21548438]], [10.01, [964.8171858, 21.21548438]]]

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [960.0707508, 23.27787743]], [9.99, [960.0707508, 23.27787743]], [10.00, [960.0707508, 23.27787743]], [10.01, [960.0707508, 23.27787743]]]

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [955.1020392, 25.34693877]], [9.99, [955.1020392, 25.34693877]], [10.00, [955.1020392, 25.34693877]], [10.01, [955.1020392, 25.34693877]]]

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [949.9170149, 27.42248950]], [9.99, [949.9170149, 27.42248950]], [10.00, [949.9170149, 27.42248950]], [10.01, [949.9170149, 27.42248950]]]

*beta is,  $\frac{29}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [944.5219011, 29.50434292]], [9.99, [944.5219011, 29.50434292]], [10.00, [944.5219011, 29.50434292]], [10.01, [944.5219011, 29.50434292]]]

*beta is,  $\frac{31}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [938.9231598, 31.59230516]], [9.99, [938.9231598, 31.59230516]], [10.00, [938.9231598, 31.59230516]], [10.01, [938.9231598, 31.59230516]]]

*beta is,  $\frac{33}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [933.1274712, 33.68617582]], [9.99, [933.1274712, 33.68617582]], [10.00, [933.1274712, 33.68617582]], [10.01, [933.1274712, 33.68617582]]]

*beta is,  $\frac{7}{2}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [927.1417118, 35.78574860]], [9.99, [927.1417118, 35.78574860]], [10.00, [927.1417118, 35.78574860]], [10.01, [927.1417118, 35.78574860]]]

*beta is,  $\frac{37}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [920.9729335, 37.89081195]], [9.99, [920.9729335, 37.89081195]], [10.00, [920.9729335, 37.89081195]], [10.01, [920.9729335, 37.89081195]]]$

*beta is,  $\frac{39}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [914.6283415, 40.00114971]], [9.99, [914.6283415, 40.00114971]], [10.00, [914.6283415, 40.00114971]], [10.01, [914.6283415, 40.00114971]]]$

(1)

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> # For beta =  $0.3 \frac{N}{nu}$ , at t = 10, the number removed is 0.32

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> # For beta =  $0.9 \frac{N}{nu}$ , at t = 10, the number removed is 2.68

>

> # For beta =  $3.9 \frac{N}{nu}$ , at t = 10, the number removed is 45.37

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#(ii)

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> SIRSdemo(1000, 200, 3, 2, 0.01, 10)

*This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization*

*with mesh size=, 0.01, and letting it run until time t=, 10*

*with population size, 1000, and fixed parameters nu=, 2, and gamma=, 3*

*where we change beta from  $0.2*nu/N$  to  $4*nu/N$*

*Recall that the epidemic will persist if beta exceeds nu/N, that in this case is,  $\frac{1}{500}$*

*We start with , 200, infected individuals, 0 removed and hence, 800, susceptible*

*We will show what happens once time is close to, 10*

*beta is,  $\frac{1}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [998.9334028, 0.9819978668]], [9.99, [998.9334028, 0.9819978668]], [10.00, [998.9334028, 0.9819978668]], [10.01, [998.9334028, 0.9819978668]]]$

*beta is,  $\frac{3}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [996.4021571, 2.957935239]], [9.99, [996.4021571, 2.957935239]], [10.00, [996.4021571, 2.957935239]], [10.01, [996.4021571, 2.957935239]]]$

*beta is,  $\frac{1}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [993.3444243, 4.949667221]], [9.99, [993.3444243, 4.949667221]], [10.00, [993.3444243, 4.949667221]], [10.01, [993.3444243, 4.949667221]]]$

*beta is,  $\frac{7}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [989.7667603, 6.956997143]], [9.99, [989.7667603, 6.956997143]], [10.00, [989.7667603, 6.956997143]], [10.01, [989.7667603, 6.956997143]]]$

*beta is,  $\frac{9}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [985.6773407, 8.979679729]], [9.99, [985.6773407, 8.979679729]], [10.00, [985.6773407, 8.979679729]], [10.01, [985.6773407, 8.979679729]]]$

*beta is,  $\frac{11}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [981.0859054, 11.01742279]], [9.99, [981.0859054, 11.01742279]], [10.00, [981.0859054, 11.01742279]], [10.01, [981.0859054, 11.01742279]]]$

*beta is,  $\frac{13}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [976.0036901, 13.06988925]], [9.99, [976.0036901, 13.06988925]], [10.00, [976.0036901, 13.06988925]], [10.01, [976.0036901, 13.06988925]]]$

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [970.4433482, 15.13669951]], [9.99, [970.4433482, 15.13669951]], [10.00, [970.4433482, 15.13669951]], [10.01, [970.4433482, 15.13669951]]]$

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [964.4188616, 17.21743410]], [9.99, [964.4188616, 17.21743410]], [10.00, [964.4188616, 17.21743410]], [10.01, [964.4188616, 17.21743410]]]$

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [957.9454447, 19.31163661]], [9.99, [957.9454447, 19.31163661]], [10.00, [957.9454447, 19.31163661]], [10.01, [957.9454447, 19.31163661]]]$

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [951.0394389, 21.41881679]], [9.99, [951.0394389, 21.41881679]], [10.00, [951.0394389, 21.41881679]], [10.01, [951.0394389, 21.41881679]]]$

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [943.7182031, 23.53845386]], [9.99, [943.7182031, 23.53845386]], [10.00, [943.7182031, 23.53845386]], [10.01, [943.7182031, 23.53845386]]]$

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [935.9999984, 25.67000000]], [9.99, [935.9999984, 25.67000000]], [10.00, [935.9999984, 25.67000000]], [10.01, [935.9999984, 25.67000000]]]$

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [927.9038703, 27.81288384]], [9.99, [927.9038703, 27.81288384]], [10.00, [927.9038703, 27.81288384]], [10.01, [927.9038703, 27.81288384]]]$

*beta is,  $\frac{29}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [919.4495282, 29.96651411]], [9.99, [919.4495282, 29.96651411]], [10.00, [919.4495282, 29.96651411]], [10.01, [919.4495282, 29.96651411]]]$

*beta is,  $\frac{31}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [910.6572255, 32.13028319]], [9.99, [910.6572255, 32.13028319]], [10.00,$

[910.6572255, 32.13028319]], [10.01, [910.6572255, 32.13028319]]]  
*beta is,  $\frac{33}{10}$ , times the threshold value*  
*the long-term behavior is*  
[[9.98, [901.5476397, 34.30357076]], [9.99, [901.5476397, 34.30357076]], [10.00,  
[901.5476397, 34.30357076]], [10.01, [901.5476397, 34.30357076]]]  
*beta is,  $\frac{7}{2}$ , times the threshold value*  
*the long-term behavior is*  
[[9.98, [892.1417551, 36.48574730]], [9.99, [892.1417551, 36.48574730]], [10.00,  
[892.1417551, 36.48574730]], [10.01, [892.1417551, 36.48574730]]]  
*beta is,  $\frac{37}{10}$ , times the threshold value*  
*the long-term behavior is*  
[[9.98, [882.4607475, 38.67617753]], [9.99, [882.4607475, 38.67617753]], [10.00,  
[882.4607475, 38.67617753]], [10.01, [882.4607475, 38.67617753]]]  
*beta is,  $\frac{39}{10}$ , times the threshold value*  
*the long-term behavior is*  
[[9.98, [872.5258747, 40.87422371]], [9.99, [872.5258747, 40.87422371]], [10.00,  
[872.5258747, 40.87422371]], [10.01, [872.5258747, 40.87422371]]] (2)

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> # For beta = 0.3  $\frac{N}{nu}$ , at t=10, the number removed is 0.64
>
> # For beta = 0.9  $\frac{N}{nu}$ , at t=10, the number removed is 5.34
>
> # For beta = 3.9  $\frac{N}{nu}$ , at t=10, the number removed is 86.59
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> #(iii)  
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> SIRSdemo(1000, 200, 7, 3, 0.01, 10)

This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, 10

with population size, 1000, and fixed parameters nu=, 3, and gamma=, 7

where we change beta from 0.2\*nu/N to 4\*nu/N

Recall that the epidemic will persist if beta exceeds nu/N, that in this case is,  $\frac{3}{1000}$

We start with , 200, infected individuals, 0 removed and hence, 800, susceptible

We will show what happens once time is close to, 10

beta is,  $\frac{1}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [998.9571869, 0.9729968716]], [9.99, [998.9571869, 0.9729968716]], [10.00, [998.9571869, 0.9729968716]], [10.01, [998.9571869, 0.9729968716]]]

beta is,  $\frac{3}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [996.6155905, 2.936908621]], [9.99, [996.6155905, 2.936908621]], [10.00, [996.6155905, 2.936908621]], [10.01, [996.6155905, 2.936908621]]]

beta is,  $\frac{1}{2}$ , times the threshold value

the long-term behavior is

[[9.98, [993.9350689, 4.924545130]], [9.99, [993.9350689, 4.924545130]], [10.00, [993.9350689, 4.924545130]], [10.01, [993.9350689, 4.924545130]]]

beta is,  $\frac{7}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [990.9190693, 6.935665103]], [9.99, [990.9190693, 6.935665103]], [10.00, [990.9190693, 6.935665103]], [10.01, [990.9190693, 6.935665103]]]

beta is,  $\frac{9}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [987.5717147, 8.969979927]], [9.99, [987.5717147, 8.969979927]], [10.00,

[987.5717147, 8.969979927]], [10.01, [987.5717147, 8.969979927]]]

*beta is,  $\frac{11}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [983.8977865, 11.02715490]], [9.99, [983.8977865, 11.02715490]], [10.00, [983.8977865, 11.02715490]], [10.01, [983.8977865, 11.02715490]]]

*beta is,  $\frac{13}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [979.9027040, 13.10681067]], [9.99, [979.9027040, 13.10681067]], [10.00, [979.9027040, 13.10681067]], [10.01, [979.9027040, 13.10681067]]]

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [975.5925002, 15.20852494]], [9.99, [975.5925002, 15.20852494]], [10.00, [975.5925002, 15.20852494]], [10.01, [975.5925002, 15.20852494]]]

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [970.9737953, 17.33183428]], [9.99, [970.9737953, 17.33183428]], [10.00, [970.9737953, 17.33183428]], [10.01, [970.9737953, 17.33183428]]]

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [966.0537675, 19.47623623]], [9.99, [966.0537675, 19.47623623]], [10.00, [966.0537675, 19.47623623]], [10.01, [966.0537675, 19.47623623]]]

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [960.8401210, 21.64119148]], [9.99, [960.8401210, 21.64119148]], [10.00, [960.8401210, 21.64119148]], [10.01, [960.8401210, 21.64119148]]]

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [955.3410529, 23.82612625]], [9.99, [955.3410529, 23.82612625]], [10.00, [955.3410529, 23.82612625]], [10.01, [955.3410529, 23.82612625]]]

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [949.5652167, 26.03043478]], [9.99, [949.5652167, 26.03043478]], [10.00, [949.5652167, 26.03043478]], [10.01, [949.5652167, 26.03043478]]]

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [943.5216861, 28.25348193]], [9.99, [943.5216861, 28.25348193]], [10.00, [943.5216861, 28.25348193]], [10.01, [943.5216861, 28.25348193]]]

*beta is,  $\frac{29}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [937.2199158, 30.49460585]], [9.99, [937.2199158, 30.49460585]], [10.00, [937.2199158, 30.49460585]], [10.01, [937.2199158, 30.49460585]]]

*beta is,  $\frac{31}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [930.6697029, 32.75312075]], [9.99, [930.6697029, 32.75312075]], [10.00, [930.6697029, 32.75312075]], [10.01, [930.6697029, 32.75312075]]]

*beta is,  $\frac{33}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [923.8811464, 35.02831970]], [9.99, [923.8811464, 35.02831970]], [10.00, [923.8811464, 35.02831970]], [10.01, [923.8811464, 35.02831970]]]

*beta is,  $\frac{7}{2}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [916.8646074, 37.31947743]], [9.99, [916.8646074, 37.31947743]], [10.00, [916.8646074, 37.31947743]], [10.01, [916.8646074, 37.31947743]]]

*beta is,  $\frac{37}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [909.6306685, 39.62585316]], [9.99, [909.6306685, 39.62585316]], [10.00, [909.6306685, 39.62585316]], [10.01, [909.6306685, 39.62585316]]]

*beta is,  $\frac{39}{10}$ , times the threshold value*

*the long-term behavior is*

[ [9.98, [902.1900937, 41.94669340]], [9.99, [902.1900937, 41.94669340]], [10.00, [902.1900937, 41.94669340]], [10.01, [902.1900937, 41.94669340]]]

(3)



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> # For beta = 0.3  $\frac{N}{\text{nu}}$ , at t=10, the number removed is 0.45
>
> # For beta = 0.9  $\frac{N}{\text{nu}}$ , at t=10, the number removed is 3.46
>
> # For beta = 3.9  $\frac{N}{\text{nu}}$ , at t=10, the number removed is 55.86
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> #2
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> F := RandNice([x,y], 8)
      F := [(5 - 3 x - 8 y) (1 - 8 x - 5 y), (2 - 3 x - 2 y) (2 - 4 x - 8 y)] (4)
> #(i)
>
> sys := {(5 - 3 x - 8 y) · (1 - 8 x - 5 y) = 0, (2 - 3 x - 2 y) · (2 - 4 x - 8 y) = 0}
      sys := {(2 - 3 x - 2 y) (2 - 4 x - 8 y) = 0, (5 - 3 x - 8 y) (1 - 8 x - 5 y) = 0} (5)
> solve(sys, {x,y})
      {x =  $\frac{1}{3}$ , y =  $\frac{1}{2}$ }, {x = -8, y = 13}, {x = -3, y =  $\frac{7}{4}$ }, {x = - $\frac{1}{22}$ , y =  $\frac{3}{11}$ } (6)
> #These are the equilibrium points.
>
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> #(ii)
>
> J := Matrix([[diff(F[1], x), diff(F[1], y)], [diff(F[2], x), diff(F[2], y)]])
      J := 
$$\begin{bmatrix} -43 + 48x + 79y & -33 + 79x + 80y \\ -14 + 24x + 32y & -20 + 32x + 32y \end{bmatrix}$$
 (7)
>
> # @ {x =  $\frac{1}{3}$ , y =  $\frac{1}{2}$ }

```

>  $J := \text{subs}\left(x = \frac{1}{3}, J\right) :$   
 >  $J := \text{subs}\left(y = \frac{1}{2}, J\right)$

$$J := \begin{bmatrix} \frac{25}{2} & \frac{100}{3} \\ 10 & \frac{20}{3} \end{bmatrix} \quad (8)$$

>  $\text{evalf}(\text{Eigenvalues}(J))$

$$\begin{bmatrix} 28.07225644 \\ -8.905589777 \end{bmatrix} \quad (9)$$

> #28 > 0 so  $\left\{x = \frac{1}{3}, y = \frac{1}{2}\right\}$  is unstable.

>  
 >  
 >  
 >  
 >  
 > #@ {x = -8, y = 13}

>  $J := \text{Matrix}([[\text{diff}(F[1], x), \text{diff}(F[1], y)], [\text{diff}(F[2], x), \text{diff}(F[2], y)]]))$

$$J := \begin{bmatrix} -43 + 48x + 79y & -33 + 79x + 80y \\ -14 + 24x + 32y & -20 + 32x + 32y \end{bmatrix} \quad (10)$$

>  
 >  $J := \text{subs}(x = -8, J) :$   
 >  $J := \text{subs}(y = 13, J)$

$$J := \begin{bmatrix} 600 & 375 \\ 210 & 140 \end{bmatrix} \quad (11)$$

>  $\text{evalf}(\text{Eigenvalues}(J))$

$$\begin{bmatrix} 732.8360512 \\ 7.1639488 \end{bmatrix} \quad (12)$$

> #This point is not stable.

>  
 >  
 >  
 >  
 > #@  $\left\{x = -3, y = \frac{7}{4}\right\}$

$$> J := \text{Matrix}([ [ \text{diff}(F[1], x), \text{diff}(F[1], y) ], [ \text{diff}(F[2], x), \text{diff}(F[2], y) ] ]) \\ J := \begin{bmatrix} -43 + 48x + 79y & -33 + 79x + 80y \\ -14 + 24x + 32y & -20 + 32x + 32y \end{bmatrix} \quad (13)$$

$$> J := \text{subs}(x = -3, J) : \\ > J := \text{subs}\left(y = \frac{7}{4}, J\right) \\ J := \begin{bmatrix} -\frac{195}{4} & -130 \\ -30 & -60 \end{bmatrix} \quad (14)$$

$$> \text{evalf}(\text{Eigenvalues}(J)) \\ \begin{bmatrix} 8.32779600 \\ -117.0777960 \end{bmatrix} \quad (15)$$

> #This point is not stable.

$$> \# @ \left\{ x = -\frac{1}{22}, y = \frac{3}{11} \right\}$$

$$> J := \text{Matrix}([ [ \text{diff}(F[1], x), \text{diff}(F[1], y) ], [ \text{diff}(F[2], x), \text{diff}(F[2], y) ] ]) \\ J := \begin{bmatrix} -43 + 48x + 79y & -33 + 79x + 80y \\ -14 + 24x + 32y & -20 + 32x + 32y \end{bmatrix} \quad (16)$$

$$> J := \text{subs}\left(x = -\frac{1}{22}, J\right) : \\ > J := \text{subs}\left(y = \frac{3}{11}, J\right) \\ J := \begin{bmatrix} -\frac{260}{11} & -\frac{325}{22} \\ -\frac{70}{11} & -\frac{140}{11} \end{bmatrix} \quad (17)$$

$$> \text{evalf}(\text{Eigenvalues}(J)) \\ \begin{bmatrix} -7.05705614 \\ -29.30658022 \end{bmatrix} \quad (18)$$

```

> #This point is stable.
>
>
>
> #set of stable equilibrium points:  $\left\{ \left\{ x = -\frac{1}{22}, y = \frac{3}{11} \right\} \right\}$ 
>
>
>
>  $\left\{ x = \frac{1}{3}, y = \frac{1}{2} \right\}, \{x = -8, y = 13\}, \left\{ x = -3, y = \frac{7}{4} \right\}, \left\{ x = -\frac{1}{22}, y = \frac{3}{11} \right\}$ 
>
> #(iii)
>
>
>
> #` `  $\left\{ x = \frac{1}{3}, y = \frac{1}{2} \right\}$ 
>
>  $Dis2(F, x, y, \left[ \frac{1}{3} + 0.1, \frac{1}{2} + 0.1 \right], 0.01, 2);$ 
[[0.01, [0.4333333333, 0.6000000000]], [0.02, [0.4934666666, 0.6226666667]], [0.03, [0.5820632985, 0.6586282048]], [0.04, [0.7221136727, 0.7181522598]], [0.05, [0.9657433495, 0.8244665204]], [0.06, [1.453152444, 1.039838959]], [0.07, [2.668177721, 1.578364726]], [0.08, [7.082068891, 3.529679646]], [0.09, [39.69078148, 17.88349920]], [0.10, [1083.535906, 476.1434118]], [0.11, [780493.1737, 342483.1892]], [0.12, [4.042905036  $\times 10^{11}$ , 1.774055268  $\times 10^{11}$ ]], [0.13, [1.084787452  $\times 10^{23}$ , 4.760121104  $\times 10^{22}$ ]], [0.14, [7.809921795  $\times 10^{45}$ , 3.427046912  $\times 10^{45}$ ]], [0.15, [4.048095605  $\times 10^{91}$ , 1.776331937  $\times 10^{91}$ ]], [0.16, [1.087574238  $\times 10^{183}$ , 4.772349871  $\times 10^{182}$ ]], [0.17, [7.850100440  $\times 10^{365}$ , 3.444677568  $\times 10^{365}$ ]], [0.18, [4.089854114  $\times 10^{731}$ , 1.794655856  $\times 10^{731}$ ]], [0.19, [1.110127916  $\times 10^{1463}$ , 4.871316947  $\times 10^{1462}$ ]], [0.20, [8.179060822  $\times 10^{2925}$ , 3.589027626  $\times 10^{2925}$ ]], [0.21, [4.439808779  $\times 10^{5851}$ , 1.948218348  $\times 10^{5851}$ ]], [0.22, [1.308235474  $\times 10^{11703}$ , 5.740626415  $\times 10^{11702}$ ]], [0.23, [1.135871578  $\times 10^{23406}$ , 4.984281891  $\times 10^{23405}$ ]], [0.24, [8.562801087  $\times 10^{46811}$ , 3.757415469  $\times 10^{46811}$ ]], [0.25, [4.866190439  $\times 10^{93623}$ , 2.135317526  $\times 10^{93623}$ ]], [0.26, [1.571576740  $\times 10^{187247}$ , 6.896185831  $\times 10^{187246}$ ]], [0.27, [1.639187278  $\times 10^{374494}$ , 7.192865480  $\times 10^{374493}$ ]], [0.28, [1.783259472

```

$$\begin{aligned}
& \times 10^{748988}, 7.825064090 \times 10^{748987}]], [0.29, [2.110505408 \times 10^{1497976}, 9.261041552 \\
& \times 10^{1497975}]], [0.30, [2.956176286 \times 10^{2995952}, 1.297190299 \times 10^{2995952}]], [0.31, \\
& [5.799867173 \times 10^{5991904}, 2.545021240 \times 10^{5991904}]], [0.32, [2.232510372 \times 10^{11983809}, \\
& 9.796407651 \times 10^{11983808}]], [0.33, [3.307838982 \times 10^{23967618}, 1.451502286 \\
& \times 10^{23967618}]], [0.34, [7.261830570 \times 10^{47935236}, 3.186540741 \times 10^{47935236}]], [0.35, \\
& [3.499851471 \times 10^{95870473}, 1.535758676 \times 10^{95870473}]], [0.36, [8.129364897 \\
& \times 10^{191740946}, 3.567220714 \times 10^{191740946}]], [0.37, [4.386020181 \times 10^{383481893}, \\
& 1.924615545 \times 10^{383481893}]], [0.38, [1.276728760 \times 10^{766963787}, 5.602372800 \\
& \times 10^{766963786}]], [0.39, [1.081819170 \times 10^{1533927574}, 4.747096241 \times 10^{1533927573}]], [0.40, \\
& [7.767240204 \times 10^{3067855147}, 3.408317932 \times 10^{3067855147}]], [0.41, [4.003970436 \\
& \times 10^{6135710295}, 1.756969513 \times 10^{6135710295}]], [0.42, [1.063993842 \times 10^{12271420591}, \\
& 4.668877486 \times 10^{12271420590}]], [0.43, [7.513384576 \times 10^{24542841181}, 3.296924353 \\
& \times 10^{24542841181}]], [0.44, [3.746524940 \times 10^{49085682363}, 1.644000675 \times 10^{49085682363}]], \\
& [0.45, [9.315681808 \times 10^{98171364726}, 4.087784660 \times 10^{98171364726}]], [0.46, [5.759525192 \\
& \times 10^{196342729453}, 2.527318903 \times 10^{196342729453}]], [0.47, [2.201561159 \times 10^{392685458907}, \\
& 9.660600394 \times 10^{392685458906}]], [0.48, [3.216761774 \times 10^{785370917814}, 1.411536988 \\
& \times 10^{785370917814}]], [0.49, [6.867444978 \times 10^{1570741835628}, 3.013481657 \\
& \times 10^{1570741835628}]], [0.50, [3.130024718 \times 10^{3141483671257}, 1.373476176 \\
& \times 10^{3141483671257}]], [0.51, [6.502089218 \times 10^{6282967342514}, 2.853161060 \\
& \times 10^{6282967342514}]], [0.52, [2.805842175 \times 10^{12565934685029}, 1.231222667 \\
& \times 10^{12565934685029}]], [0.53, [5.224970801 \times 10^{25131869370058}, 2.292752794 \\
& \times 10^{25131869370058}]], [0.54, [1.811862037 \times 10^{50263738740117}, 7.950574092 \\
& \times 10^{50263738740116}]], [0.55, [2.178751210 \times 10^{100527477480234}, 9.560508780 \\
& \times 10^{100527477480233}]], [0.56, [3.150450588 \times 10^{201054954960468}, 1.382439187 \\
& \times 10^{201054954960468}]], [0.57, [6.587228596 \times 10^{402109909920936}, 2.890520798 \\
& \times 10^{402109909920936}]], [0.58, [2.879803532 \times 10^{804219819841873}, 1.263677415 \\
& \times 10^{804219819841873}]], [0.59, [5.504059378 \times 10^{1608439639683746}, 2.415218763 \\
& \times 10^{1608439639683746}]], [0.60, [2.010590429 \times 10^{3216879279367493}, 8.822607817 \\
& \times 10^{3216879279367492}]], [0.61, [2.682900780 \times 10^{6433758558734986}, 1.177275145 \\
& \times 10^{6433758558734986}]], [0.62, [4.777125089 \times 10^{12867517117469972}, 2.096235044 \\
& \times 10^{12867517117469972}]], [0.63, [1.514574418 \times 10^{25735034234939945}, 6.646055760 \\
& \times 10^{25735034234939944}]], [0.64, [1.522434525 \times 10^{51470068469879890}, 6.680546447
\end{aligned}$$

$$\begin{aligned}
& \times 10^{51470068469879889}], [0.65, [1.538277325 \times 10^{102940136939759780}, 6.750065732 \\
& \times 10^{102940136939759779}], [0.66, [1.570459232 \times 10^{205880273879519560}, 6.891282133 \\
& \times 10^{205880273879519559}], [0.67, [1.636856940 \times 10^{411760547759039120}, 7.182639795 \\
& \times 10^{411760547759039119}], [0.68, [1.778192763 \times 10^{823521095518078240}, 7.802831018 \\
& \times 10^{823521095518078239}], [0.69, [2.098529441 \times 10^{1647042191036156480}, 9.208490203 \\
& \times 10^{1647042191036156479}], [0.70, [2.922722098 \times 10^{3294084382072312960}, 1.282510375 \\
& \times 10^{3294084382072312960}], [0.71, [5.669339132 \times 10^{6588168764144625920}, 2.487744645 \\
& \times 10^{6588168764144625920}], [0.72, [\text{Float}(\infty), \text{Float}(\infty)]], [0.73, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [0.74, [\text{Float}(\infty), \text{Float}(\infty)]], [0.75, [\text{Float}(\infty), \text{Float}(\infty)]], [0.76, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [0.77, [\text{Float}(\infty), \text{Float}(\infty)]], [0.78, [\text{Float}(\infty), \text{Float}(\infty)]], [0.79, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.80, [\text{Float}(\infty), \text{Float}(\infty)]], [0.81, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [0.82, [\text{Float}(\infty), \text{Float}(\infty)]], [0.83, [\text{Float}(\infty), \text{Float}(\infty)]], [0.84, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [0.85, [\text{Float}(\infty), \text{Float}(\infty)]], [0.86, [\text{Float}(\infty), \text{Float}(\infty)]], [0.87, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.88, [\text{Float}(\infty), \text{Float}(\infty)]], [0.89, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [0.90, [\text{Float}(\infty), \text{Float}(\infty)]], [0.91, [\text{Float}(\infty), \text{Float}(\infty)]], [0.92, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [0.93, [\text{Float}(\infty), \text{Float}(\infty)]], [0.94, [\text{Float}(\infty), \text{Float}(\infty)]], [0.95, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.96, [\text{Float}(\infty), \text{Float}(\infty)]], [0.97, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [0.98, [\text{Float}(\infty), \text{Float}(\infty)]], [0.99, [\text{Float}(\infty), \text{Float}(\infty)]], [1.00, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [1.01, [\text{Float}(\infty), \text{Float}(\infty)]], [1.02, [\text{Float}(\infty), \text{Float}(\infty)]], [1.03, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [1.04, [\text{Float}(\infty), \text{Float}(\infty)]], [1.05, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [1.06, [\text{Float}(\infty), \text{Float}(\infty)]], [1.07, [\text{Float}(\infty), \text{Float}(\infty)]], [1.08, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [1.09, [\text{Float}(\infty), \text{Float}(\infty)]], [1.10, [\text{Float}(\infty), \text{Float}(\infty)]], [1.11, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [1.12, [\text{Float}(\infty), \text{Float}(\infty)]], [1.13, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [1.14, [\text{Float}(\infty), \text{Float}(\infty)]], [1.15, [\text{Float}(\infty), \text{Float}(\infty)]], [1.16, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [1.17, [\text{Float}(\infty), \text{Float}(\infty)]], [1.18, [\text{Float}(\infty), \text{Float}(\infty)]], [1.19, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [1.20, [\text{Float}(\infty), \text{Float}(\infty)]], [1.21, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [1.22, [\text{Float}(\infty), \text{Float}(\infty)]], [1.23, [\text{Float}(\infty), \text{Float}(\infty)]], [1.24, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [1.25, [\text{Float}(\infty), \text{Float}(\infty)]], [1.26, [\text{Float}(\infty), \text{Float}(\infty)]], [1.27, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [1.28, [\text{Float}(\infty), \text{Float}(\infty)]], [1.29, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [1.30, [\text{Float}(\infty), \text{Float}(\infty)]], [1.31, [\text{Float}(\infty), \text{Float}(\infty)]], [1.32, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [1.33, [\text{Float}(\infty), \text{Float}(\infty)]], [1.34, [\text{Float}(\infty), \text{Float}(\infty)]], [1.35, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [1.36, [\text{Float}(\infty), \text{Float}(\infty)]], [1.37, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [1.38, [\text{Float}(\infty), \text{Float}(\infty)]], [1.39, [\text{Float}(\infty), \text{Float}(\infty)]], [1.40, [\text{Float}(\infty), \\
& \text{Float}(\infty)]], [1.41, [\text{Float}(\infty), \text{Float}(\infty)]], [1.42, [\text{Float}(\infty), \text{Float}(\infty)]], [1.43, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [1.44, [\text{Float}(\infty), \text{Float}(\infty)]], [1.45, [\text{Float}(\infty), \text{Float}(\infty)]], \\
& [1.46, [\text{Float}(\infty), \text{Float}(\infty)]], [1.47, [\text{Float}(\infty), \text{Float}(\infty)]], [1.48, [\text{Float}(\infty), \\
& \text{Float}(\infty)]]
\end{aligned}$$

```

Float(∞)], [1.49, [Float(∞), Float(∞)]], [1.50, [Float(∞), Float(∞)]], [1.51, [
Float(∞), Float(∞)]], [1.52, [Float(∞), Float(∞)]], [1.53, [Float(∞), Float(∞)]],
[1.54, [Float(∞), Float(∞)]], [1.55, [Float(∞), Float(∞)]], [1.56, [Float(∞),
Float(∞)]], [1.57, [Float(∞), Float(∞)]], [1.58, [Float(∞), Float(∞)]], [1.59, [
Float(∞), Float(∞)]], [1.60, [Float(∞), Float(∞)]], [1.61, [Float(∞), Float(∞)]],
[1.62, [Float(∞), Float(∞)]], [1.63, [Float(∞), Float(∞)]], [1.64, [Float(∞),
Float(∞)]], [1.65, [Float(∞), Float(∞)]], [1.66, [Float(∞), Float(∞)]], [1.67, [
Float(∞), Float(∞)]], [1.68, [Float(∞), Float(∞)]], [1.69, [Float(∞), Float(∞)]],
[1.70, [Float(∞), Float(∞)]], [1.71, [Float(∞), Float(∞)]], [1.72, [Float(∞),
Float(∞)]], [1.73, [Float(∞), Float(∞)]], [1.74, [Float(∞), Float(∞)]], [1.75, [
Float(∞), Float(∞)]], [1.76, [Float(∞), Float(∞)]], [1.77, [Float(∞), Float(∞)]],
[1.78, [Float(∞), Float(∞)]], [1.79, [Float(∞), Float(∞)]], [1.80, [Float(∞),
Float(∞)]], [1.81, [Float(∞), Float(∞)]], [1.82, [Float(∞), Float(∞)]], [1.83, [
Float(∞), Float(∞)]], [1.84, [Float(∞), Float(∞)]], [1.85, [Float(∞), Float(∞)]],
[1.86, [Float(∞), Float(∞)]], [1.87, [Float(∞), Float(∞)]], [1.88, [Float(∞),
Float(∞)]], [1.89, [Float(∞), Float(∞)]], [1.90, [Float(∞), Float(∞)]], [1.91, [
Float(∞), Float(∞)]], [1.92, [Float(∞), Float(∞)]], [1.93, [Float(∞), Float(∞)]],
[1.94, [Float(∞), Float(∞)]], [1.95, [Float(∞), Float(∞)]], [1.96, [Float(∞),
Float(∞)]], [1.97, [Float(∞), Float(∞)]], [1.98, [Float(∞), Float(∞)]], [1.99, [
Float(∞), Float(∞)]], [2.00, [Float(∞), Float(∞)]], [2.01, [Float(∞), Float(∞)]]]

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```

# {x = -8, y = 13}
>
> Dis2(F, x, y, [-8 + 0.1, 13 + 0.1], 0.01, 2);
[[0.01, [-7.9, 13.1]], [0.02, [-6.9107, 13.4560]], [0.03, [2.095461710, 16.71653936]],
[0.04, [136.2316666, 69.56684993]], [0.05, [13931.73396, 6070.743074]], [0.06,
[1.281448992 × 108, 5.625503173 × 107]], [0.07, [1.090186749 × 1016, 4.783688944
× 1015]], [0.08, [7.887704643 × 1031, 3.461184031 × 1031]], [0.09, [4.129136016
× 1063, 1.811892848 × 1063]], [0.10, [1.131555179 × 10127, 4.965341265 × 10126]],
[0.11, [8.497846170 × 10253, 3.728912809 × 10253]], [0.12, [4.792643445 × 10507,
2.103044604 × 10507]], [0.13, [1.524430505 × 101015, 6.689304942 × 101014]], [0.14,
```

(20)

$$\begin{aligned}
& [1.542313470 \times 10^{2030}, 6.767776608 \times 10^{2029}]], [0.15, [1.578711211 \times 10^{4060}, \\
& 6.927492382 \times 10^{4059}]], [0.16, [1.654103865 \times 10^{8120}, 7.258320480 \times 10^{8119}]], [0.17, \\
& [1.815862429 \times 10^{16240}, 7.968128079 \times 10^{16239}]], [0.18, [2.188382715 \times 10^{32480}, \\
& 9.602772486 \times 10^{32479}]], [0.19, [3.178366259 \times 10^{64960}, 1.394688774 \times 10^{64960}]], [0.20, \\
& [6.704482684 \times 10^{129920}, 2.941972690 \times 10^{129920}]], [0.21, [2.983238237 \times 10^{259841}, \\
& 1.309065268 \times 10^{259841}]], [0.22, [5.906541555 \times 10^{519682}, 2.591830686 \times 10^{519682}]], [0.23, \\
& [2.315388744 \times 10^{1039365}, 1.016008359 \times 10^{1039365}]], [0.24, [3.557994112 \\
& \times 10^{2078730}, 1.561272064 \times 10^{2078730}]], [0.25, [8.401712970 \times 10^{4157460}, 3.686728906 \\
& \times 10^{4157460}]], [0.26, [4.684821748 \times 10^{8314921}, 2.055731708 \times 10^{8314921}]], [0.27, \\
& [1.456610822 \times 10^{16629843}, 6.391707549 \times 10^{16629842}]], [0.28, [1.408135523 \times 10^{33259686}, \\
& 6.178994636 \times 10^{33259685}]], [0.29, [1.315970941 \times 10^{66519372}, 5.774570166 \\
& \times 10^{66519371}]], [0.30, [1.149343883 \times 10^{133038744}, 5.043399282 \times 10^{133038743}]], [0.31, \\
& [8.767128407 \times 10^{266077487}, 3.847075691 \times 10^{266077487}]], [0.32, [5.101197347 \\
& \times 10^{532154975}, 2.238440158 \times 10^{532154975}]], [0.33, [1.727036993 \times 10^{1064309951}, \\
& 7.578356019 \times 10^{1064309950}]], [0.34, [1.979523539 \times 10^{2128619902}, 8.686284193 \\
& \times 10^{2128619901}]], [0.35, [2.600630976 \times 10^{4257239804}, 1.141174595 \times 10^{4257239804}]], \\
& [0.36, [4.488640797 \times 10^{8514479608}, 1.969646170 \times 10^{8514479608}]], [0.37, [1.337171449 \\
& \times 10^{17028959217}, 5.867599440 \times 10^{17028959216}]], [0.38, [1.186674418 \times 10^{34057918434}, \\
& 5.207208215 \times 10^{34057918433}]], [0.39, [9.345887528 \times 10^{68115836867}, 4.101039136 \\
& \times 10^{68115836867}]], [0.40, [5.796935798 \times 10^{136231673735}, 2.543734932 \times 10^{136231673735}]], \\
& [0.41, [2.230254226 \times 10^{272463347471}, 9.786507527 \times 10^{272463347470}]], [0.42, \\
& [3.301156639 \times 10^{544926694942}, 1.448570030 \times 10^{544926694942}]], [0.43, [7.232520182 \\
& \times 10^{1089853389884}, 3.173679144 \times 10^{1089853389884}]], [0.44, [3.471656107 \times 10^{2179706779769}, \\
& 1.523386358 \times 10^{2179706779769}]], [0.45, [7.998909574 \times 10^{4359413559538}, 3.509976032 \\
& \times 10^{4359413559538}]], [0.46, [4.246381065 \times 10^{8718827119077}, 1.863340949 \\
& \times 10^{8718827119077}]], [0.47, [1.196727633 \times 10^{17437654238155}, 5.251322410 \\
& \times 10^{17437654238154}]], [0.48, [9.504910433 \times 10^{34875308476309}, 4.170819470 \\
& \times 10^{34875308476309}]], [0.49, [5.995887112 \times 10^{69750616952619}, 2.631036125 \\
& \times 10^{69750616952619}]], [0.50, [2.385966190 \times 10^{139501233905239}, 1.046978224 \\
& \times 10^{139501233905239}]], [0.51, [3.778208847 \times 10^{279002467810478}, 1.657903789 \\
& \times 10^{279002467810478}]], [0.52, [9.473911233 \times 10^{558004935620956}, 4.157216811 \\
& \times 10^{558004935620956}]], [0.53, [5.956841063 \times 10^{1116009871241913}, 2.613902452
\end{aligned}$$

$$\begin{aligned}
& \times 10^{1116009871241913}], [0.54, [2.354991887 \times 10^{2232019742483827}, 1.033386489 \\
& \times 10^{2232019742483827}], [0.55, [3.680749153 \times 10^{4464039484967654}, 1.615137812 \\
& \times 10^{4464039484967654}], [0.56, [8.991452036 \times 10^{8928078969935308}, 3.945510426 \\
& \times 10^{8928078969935308}], [0.57, [5.365584687 \times 10^{17856157939870617}, 2.354455125 \\
& \times 10^{17856157939870617}], [0.58, [1.910695575 \times 10^{35712315879741235}, 8.384262390 \\
& \times 10^{35712315879741234}], [0.59, [2.422927315 \times 10^{71424631759482470}, 1.063197016 \\
& \times 10^{71424631759482470}], [0.60, [3.896172365 \times 10^{142849263518964940}, 1.709666985 \\
& \times 10^{142849263518964940}], [0.61, [1.007473690 \times 10^{285698527037929881}, 4.420863208 \\
& \times 10^{285698527037929880}], [0.62, [6.736352685 \times 10^{571397054075859761}, 2.955957466 \\
& \times 10^{571397054075859761}], [0.63, [3.011667511 \times 10^{1142794108151719523}, 1.321540227 \\
& \times 10^{1142794108151719523}], [0.64, [6.019652731 \times 10^{2285588216303439046}, 2.641464641 \\
& \times 10^{2285588216303439046}], [0.65, [2.404917961 \times 10^{4571176432606878093}, 1.055294390 \\
& \times 10^{4571176432606878093}], [0.66, [3.838467977 \times 10^{9142352865213756186}, 1.684345906 \\
& \times 10^{9142352865213756186}], [0.67, [Float(\infty), Float(\infty)]], [0.68, [Float(\infty), Float(\infty)]], \\
[0.69, [Float(\infty), Float(\infty)]], [0.70, [Float(\infty), Float(\infty)]], [0.71, [Float(\infty), \\
Float(\infty)]], [0.72, [Float(\infty), Float(\infty)]], [0.73, [Float(\infty), Float(\infty)]], [0.74, [ \\
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Float(\infty), Float(\infty)]], [0.83, [Float(\infty), Float(\infty)]], [0.84, [Float(\infty), Float(\infty)]], \\
[0.85, [Float(\infty), Float(\infty)]], [0.86, [Float(\infty), Float(\infty)]], [0.87, [Float(\infty), \\
Float(\infty)]], [0.88, [Float(\infty), Float(\infty)]], [0.89, [Float(\infty), Float(\infty)]], [0.90, [ \\
Float(\infty), Float(\infty)]], [0.91, [Float(\infty), Float(\infty)]], [0.92, [Float(\infty), Float(\infty)]], \\
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[1.17, [Float(\infty), Float(\infty)]], [1.18, [Float(\infty), Float(\infty)]], [1.19, [Float(\infty), \\
Float(\infty)]], [1.20, [Float(\infty), Float(\infty)]], [1.21, [Float(\infty), Float(\infty)]], [1.22, [ \\
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\end{aligned}$$

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[1.25, [Float(∞), Float(∞)]], [1.26, [Float(∞), Float(∞)]], [1.27, [Float(∞),
Float(∞)]], [1.28, [Float(∞), Float(∞)]], [1.29, [Float(∞), Float(∞)]], [1.30, [
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Float(∞), Float(∞)]], [1.39, [Float(∞), Float(∞)]], [1.40, [Float(∞), Float(∞)]],
[1.41, [Float(∞), Float(∞)]], [1.42, [Float(∞), Float(∞)]], [1.43, [Float(∞),
Float(∞)]], [1.44, [Float(∞), Float(∞)]], [1.45, [Float(∞), Float(∞)]], [1.46, [
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[1.49, [Float(∞), Float(∞)]], [1.50, [Float(∞), Float(∞)]], [1.51, [Float(∞),
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[1.81, [Float(∞), Float(∞)]], [1.82, [Float(∞), Float(∞)]], [1.83, [Float(∞),
Float(∞)]], [1.84, [Float(∞), Float(∞)]], [1.85, [Float(∞), Float(∞)]], [1.86, [
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[1.89, [Float(∞), Float(∞)]], [1.90, [Float(∞), Float(∞)]], [1.91, [Float(∞),
Float(∞)]], [1.92, [Float(∞), Float(∞)]], [1.93, [Float(∞), Float(∞)]], [1.94, [
Float(∞), Float(∞)]], [1.95, [Float(∞), Float(∞)]], [1.96, [Float(∞), Float(∞)]],
[1.97, [Float(∞), Float(∞)]], [1.98, [Float(∞), Float(∞)]], [1.99, [Float(∞),
Float(∞)]], [2.00, [Float(∞), Float(∞)]], [2.01, [Float(∞), Float(∞)]]]
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$$\# \left\{ x = -3, y = \frac{7}{4} \right\}$$

$$\begin{aligned}
& > \text{Dis2}\left(F, x, y, \left[-3 + 0.1, \frac{7}{4} + 0.1\right], 0.01, 2\right); \\
& [[0.01, [-2.9, 1.850000000]], [0.02, [-3.064450000, 1.766000000]], [0.03, \\
& [-3.053545960, 1.775944432]], [0.04, [-3.061310184, 1.776448769]], [0.05, \\
& [-3.065903956, 1.779016657]], [0.06, [-3.071628973, 1.781421823]], [0.07, \\
& [-3.077709978, 1.784110851]], [0.08, [-3.084349824, 1.787019921]], [0.09, \\
& [-3.091566291, 1.790186739]], [0.10, [-3.099419246, 1.793631585]], [0.11, \\
& [-3.107966610, 1.797381002]], [0.12, [-3.117273875, 1.801463410]], [0.13, \\
& [-3.127413041, 1.805910363]], [0.14, [-3.138463818, 1.810756715]], [0.15, \\
& [-3.150514510, 1.816041085]], [0.16, [-3.163663130, 1.821806324]], [0.17, \\
& [-3.178018685, 1.828100072]], [0.18, [-3.193702649, 1.834975405]], [0.19, \\
& [-3.210850703, 1.842491587]], [0.20, [-3.229614761, 1.850714945]], [0.21, \\
& [-3.250165343, 1.859719914]], [0.22, [-3.272694409, 1.869590248]], [0.23, \\
& [-3.297418695, 1.880420474]], [0.24, [-3.324583702, 1.892317628]], [0.25, \\
& [-3.354468486, 1.905403327]], [0.26, [-3.387391459, 1.919816270]], [0.27, \\
& [-3.423717377, 1.935715294]], [0.28, [-3.463865960, 1.953283073]], [0.29, \\
& [-3.508322422, 1.972730703]], [0.30, [-3.557650581, 1.994303362]], [0.31, \\
& [-3.612509211, 2.018287388]], [0.32, [-3.673672630, 2.045019203]], [0.33, \\
& [-3.742056925, 2.074896625]], [0.34, [-3.818753538, 2.108393423]], [0.35, \\
& [-3.905072882, 2.146078166]], [0.36, [-4.002601530, 2.188638954]], [0.37, \\
& [-4.113278181, 2.236916254]], [0.38, [-4.239495890, 2.291947106]], [0.39, \\
& [-4.384241757, 2.355025496]], [0.40, [-4.551290877, 2.427786193]], [0.41, \\
& [-4.745480558, 2.512323275]], [0.42, [-4.973105923, 2.611361101]], [0.43, \\
& [-5.242503548, 2.728506585]], [0.44, [-5.564934802, 2.868630943]], [0.45, \\
& [-5.955961700, 3.038464373]], [0.46, [-6.437662139, 3.247553450]], [0.47, \\
& [-7.042335169, 3.509862659]], [0.48, [-7.818982157, 3.846575592]], [0.49, \\
& [-8.845258266, 4.291260923]], [0.50, [-10.25095849, 4.900023832]], [0.51, \\
& [-12.26789811, 5.773067529]], [0.52, [-15.34666230, 7.105158682]], [0.53, \\
& [-20.46614942, 9.319439018]], [0.54, [-30.10225215, 13.48614570]], [0.55, \\
& [-52.04437432, 22.97260745]], [0.56, [-120.5519561, 52.58644309]], [0.57, \\
& [-500.1436309, 216.7652170]], [0.58, [-7174.081014, 3086.258300]], [0.59, \\
& [-1.334369298 \times 10^6, 618423.0093]], [0.60, [-7.160391027 \times 10^{10}, 1.079167875 \\
& \times 10^{10}]], [0.61, [6.666390702 \times 10^{20}, 3.866156018 \times 10^{20}]], [0.62, [3.700556070
\end{aligned} \tag{21}$$

$$\begin{aligned}
& \times 10^{41}, 1.597189587 \times 10^{41}]], [0.63, [8.976280289 \times 10^{82}, 3.942812838 \times 10^{82}]], [0.64, \\
& [5.351549170 \times 10^{165}, 2.348153045 \times 10^{165}]], [0.65, [1.900625055 \times 10^{331}, 8.340103131 \\
& \times 10^{330}]], [0.66, [2.397460734 \times 10^{662}, 1.052021871 \times 10^{662}]], [0.67, [3.814699409 \\
& \times 10^{1324}, 1.673916120 \times 10^{1324}]], [0.68, [9.657796249 \times 10^{2648}, 4.237906806 \times 10^{2648}]], \\
& [0.69, [6.190325241 \times 10^{5297}, 2.716356901 \times 10^{5297}]], [0.70, [2.543222313 \times 10^{10595}, \\
& 1.115983282 \times 10^{10595}]], [0.71, [4.292655542 \times 10^{21190}, 1.883646505 \times 10^{21190}]], [0.72, \\
& [1.222952168 \times 10^{42381}, 5.366397454 \times 10^{42380}]], [0.73, [9.926047123 \times 10^{84761}, \\
& 4.355617121 \times 10^{84761}]], [0.74, [6.538980700 \times 10^{169523}, 2.869349291 \times 10^{169523}]], \\
& [0.75, [2.837772012 \times 10^{339047}, 1.245233697 \times 10^{339047}]], [0.76, [5.344565355 \\
& \times 10^{678094}, 2.345231700 \times 10^{678094}]], [0.77, [1.895754844 \times 10^{1356189}, 8.318701444 \\
& \times 10^{1356188}]], [0.78, [2.385183184 \times 10^{2712378}, 1.046634635 \times 10^{2712378}]], [0.79, \\
& [3.775729451 \times 10^{5424756}, 1.656815814 \times 10^{5424756}]], [0.80, [9.461481076 \times 10^{10849512}, \\
& 4.151762372 \times 10^{10849512}]], [0.81, [5.941220080 \times 10^{21699025}, 2.607047858 \\
& \times 10^{21699025}]], [0.82, [2.342656808 \times 10^{43398051}, 1.027973772 \times 10^{43398051}]], [0.83, \\
& [3.642291757 \times 10^{86796102}, 1.598262444 \times 10^{86796102}]], [0.84, [8.804543673 \\
& \times 10^{173592204}, 3.863493764 \times 10^{173592204}]], [0.85, [5.144830772 \times 10^{347184409}, \\
& 2.257586803 \times 10^{347184409}]], [0.86, [1.756707998 \times 10^{694368819}, 7.708554409 \\
& \times 10^{694368818}]], [0.87, [2.048125416 \times 10^{1388737638}, 8.987313905 \times 10^{1388737637}]], [0.88, \\
& [2.784008034 \times 10^{2777475276}, 1.221641697 \times 10^{2777475276}]], [0.89, [5.143969188 \\
& \times 10^{5554950552}, 2.257208735 \times 10^{5554950552}]], [0.90, [1.756119669 \times 10^{11109901105}, \\
& 7.705972781 \times 10^{11109901104}]], [0.91, [2.046753795 \times 10^{22219802210}, 8.981295132 \\
& \times 10^{22219802209}]], [0.92, [2.780280405 \times 10^{44439604420}, 1.220005988 \times 10^{44439604420}]], \\
& [0.93, [5.130203442 \times 10^{88879208840}, 2.251168230 \times 10^{88879208840}]], [0.94, [1.746733162 \\
& \times 10^{177758417681}, 7.664784149 \times 10^{177758417680}]], [0.95, [2.024932360 \times 10^{355516835362}, \\
& 8.885541195 \times 10^{355516835361}]], [0.96, [2.721312598 \times 10^{711033670724}, 1.194130512 \\
& \times 10^{711033670724}]], [0.97, [4.914895113 \times 10^{1422067341448}, 2.156689470 \\
& \times 10^{1422067341448}]], [0.98, [1.603193334 \times 10^{2844134682897}, 7.034921603 \\
& \times 10^{2844134682896}]], [0.99, [1.705804229 \times 10^{5688269365794}, 7.485185206 \\
& \times 10^{5688269365793}]], [1.00, [1.931148911 \times 10^{11376538731588}, 8.474013027 \\
& \times 10^{11376538731587}]], [1.01, [2.475078157 \times 10^{22753077463176}, 1.086081162 \\
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& \times 10^{45506154926352}]], [1.03, [1.097053583 \times 10^{91012309852705}, 4.813945882
\end{aligned}$$

$$\begin{aligned}
& \times 10^{91012309852704}]], [1.04, [7.987540445 \times 10^{182024619705409}, 3.504987181 \\
& \times 10^{182024619705409}]], [1.05, [4.234318585 \times 10^{364049239410819}, 1.858047851 \\
& \times 10^{364049239410819}]], [1.06, [1.189938323 \times 10^{728098478821639}, 5.221530453 \\
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& \times 10^{2912393915286555}]], [1.09, [2.279803120 \times 10^{5824787830573111}, 1.000393145 \\
& \times 10^{5824787830573111}]], [1.10, [3.449467657 \times 10^{11649575661146222}, 1.513649915 \\
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& \times 10^{23299151322292444}]], [1.12, [4.138857553 \times 10^{46598302644584889}, 1.816158899 \\
& \times 10^{46598302644584889}]], [1.13, [1.136889745 \times 10^{93196605289169779}, 4.988749678 \\
& \times 10^{93196605289169778}]], [1.14, [8.578158932 \times 10^{186393210578339557}, 3.764154596 \\
& \times 10^{186393210578339557}]], [1.15, [4.883661643 \times 10^{372786421156679115}, 2.142984009 \\
& \times 10^{372786421156679115}]], [1.16, [1.582881939 \times 10^{745572842313358231}, 6.945793818 \\
& \times 10^{745572842313358230}]], [1.17, [1.662855218 \times 10^{1491145684626716462}, 7.296722015 \\
& \times 10^{1491145684626716461}]], [1.18, [1.835127593 \times 10^{2982291369253432924}, 8.052664932 \\
& \times 10^{2982291369253432923}]], [1.19, [2.235063778 \times 10^{5964582738506865848}, 9.807612177 \\
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Float(\infty)]], [1.49, [Float(\infty), Float(\infty)]], [1.50, [Float(\infty), Float(\infty)]], [1.51, [ \\
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[1.54, [Float(\infty), Float(\infty)]], [1.55, [Float(\infty), Float(\infty)]], [1.56, [Float(\infty), \\
Float(\infty)]], [1.57, [Float(\infty), Float(\infty)]], [1.58, [Float(\infty), Float(\infty)]], [1.59, [ \\
Float(\infty), Float(\infty)]], [1.60, [Float(\infty), Float(\infty)]], [1.61, [Float(\infty), Float(\infty)]], \\
[1.62, [Float(\infty), Float(\infty)]], [1.63, [Float(\infty), Float(\infty)]], [1.64, [Float(\infty), \\
Float(\infty)]], [1.65, [Float(\infty), Float(\infty)]], [1.66, [Float(\infty), Float(\infty)]], [1.67, [ \\
Float(\infty), Float(\infty)]], [1.68, [Float(\infty), Float(\infty)]], [1.69, [Float(\infty), Float(\infty)]]]
\end{aligned}$$

```

[1.70, [Float(∞), Float(∞)]], [1.71, [Float(∞), Float(∞)]], [1.72, [Float(∞),
Float(∞)]], [1.73, [Float(∞), Float(∞)]], [1.74, [Float(∞), Float(∞)]], [1.75, [
Float(∞), Float(∞)]], [1.76, [Float(∞), Float(∞)]], [1.77, [Float(∞), Float(∞)]],
[1.78, [Float(∞), Float(∞)]], [1.79, [Float(∞), Float(∞)]], [1.80, [Float(∞),
Float(∞)]], [1.81, [Float(∞), Float(∞)]], [1.82, [Float(∞), Float(∞)]], [1.83, [
Float(∞), Float(∞)]], [1.84, [Float(∞), Float(∞)]], [1.85, [Float(∞), Float(∞)]],
[1.86, [Float(∞), Float(∞)]], [1.87, [Float(∞), Float(∞)]], [1.88, [Float(∞),
Float(∞)]], [1.89, [Float(∞), Float(∞)]], [1.90, [Float(∞), Float(∞)]], [1.91, [
Float(∞), Float(∞)]], [1.92, [Float(∞), Float(∞)]], [1.93, [Float(∞), Float(∞)]],
[1.94, [Float(∞), Float(∞)]], [1.95, [Float(∞), Float(∞)]], [1.96, [Float(∞),
Float(∞)]], [1.97, [Float(∞), Float(∞)]], [1.98, [Float(∞), Float(∞)]], [1.99, [
Float(∞), Float(∞)]], [2.00, [Float(∞), Float(∞)]], [2.01, [Float(∞), Float(∞)]]]

```

>

>

>

>

```
#@ {x = -  $\frac{1}{22}$ , y =  $\frac{3}{11}$ }
```

>

>

```
Dis2(F, x, y,  $\left[-\frac{1}{22} + 0.1, \frac{3}{11} + 0.1\right]$ , 0.01, 2);
```

[ [0.01, [0.05454545455, 0.3727272727]], [0.02, [0.03043636365, 0.3596363636]], [0.03,
[0.00927374053, 0.3477560223]], [0.04, [-0.00853136500, 0.3372982943]], [0.05,
[-0.02291910698, 0.3283241462]], [0.06, [-0.03411076074, 0.3207705386]], [0.07,
[-0.04250462983, 0.3144932081]], [0.08, [-0.04857467177, 0.3093093948]], [0.09,
[-0.05279389866, 0.3050308053]], [0.10, [-0.05558821882, 0.3014840554]], [0.11,
[-0.05731593641, 0.2985203549]], [0.12, [-0.05826449118, 0.2960178418]], [0.13,
[-0.05865667235, 0.2938797771]], [0.14, [-0.05866078282, 0.2920309170]], [0.15,
[-0.05840146736, 0.2904134588]], [0.16, [-0.05796956343, 0.2889832735]], [0.17,
[-0.05743035064, 0.2877067124]], [0.18, [-0.05683012210, 0.2865580417]], [0.19,
[-0.05620125128, 0.2855174507]], [0.20, [-0.05556601278, 0.2845695396]], [0.21,
[-0.05493941838, 0.2837021886]], [0.22, [-0.05433129872, 0.2829057207]], [0.23,
[-0.05374781761, 0.2821722854]], [0.24, [-0.05319256624, 0.2814954077]], [0.25,
[-0.05266734954, 0.2808696575]], [0.26, [-0.05217274824, 0.2802904079]], [0.27,
[-0.05170851855, 0.2797536579]], [0.28, [-0.05127387534, 0.2792559018]], [0.29,
[-0.05086769110, 0.2787940323]], [0.30, [-0.05048863522, 0.2783652684]], [0.31,
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[-0.04949970348, 0.2772536402]], [0.34, [-0.04921458554, 0.2769343587]], [0.35,

(22)

[ $-0.04894937409, 0.2766376531$ ]], [ $0.36, [-0.04870274200, 0.2763619056]$ ]], [ $0.37, [-0.04847343119, 0.2761056212]$ ]], [ $0.38, [-0.04826025509, 0.2758674166]$ ]], [ $0.39, [-0.04806209892, 0.2756460101]$ ]], [ $0.40, [-0.04787791826, 0.2754402132]$ ]], [ $0.41, [-0.04770673670, 0.2752489230]$ ]], [ $0.42, [-0.04754764284, 0.2750711157]$ ]], [ $0.43, [-0.04739978700, 0.2749058403]$ ]], [ $0.44, [-0.04726237777, 0.2747522135]$ ]], [ $0.45, [-0.04713467841, 0.2746094145]$ ]], [ $0.46, [-0.04701600345, 0.2744766804]$ ]], [ $0.47, [-0.04690571543, 0.2743533022]$ ]], [ $0.48, [-0.04680322165, 0.2742386208]$ ]], [ $0.49, [-0.04670797104, 0.2741320237]$ ]], [ $0.50, [-0.04661945144, 0.2740329415]$ ]], [ $0.51, [-0.04653718690, 0.2739408447]$ ]], [ $0.52, [-0.04646073507, 0.2738552413]$ ]], [ $0.53, [-0.04638968483, 0.2737756738]$ ]], [ $0.54, [-0.04632365429, 0.2737017169]$ ]], [ $0.55, [-0.04626228849, 0.2736329752]$ ]], [ $0.56, [-0.04620525760, 0.2735690812]$ ]], [ $0.57, [-0.04615225514, 0.2735096933]$ ]], [ $0.58, [-0.04610299635, 0.2734544939]$ ]], [ $0.59, [-0.04605721663, 0.2734031877]$ ]], [ $0.60, [-0.04601467004, 0.2733555003]$ ]], [ $0.61, [-0.04597512815, 0.2733111766]$ ]], [ $0.62, [-0.04593837858, 0.2732699794]$ ]], [ $0.63, [-0.04590422403, 0.2732316882]$ ]], [ $0.64, [-0.04587248118, 0.2731960982]$ ]], [ $0.65, [-0.04584297965, 0.2731630188]$ ]], [ $0.66, [-0.04581556107, 0.2731322731]$ ]], [ $0.67, [-0.04579007833, 0.2731036964]$ ]], [ $0.68, [-0.04576639467, 0.2730771358]$ ]], [ $0.69, [-0.04574438307, 0.2730524491]$ ]], [ $0.70, [-0.04572392542, 0.2730295041]$ ]], [ $0.71, [-0.04570491197, 0.2730081779]$ ]], [ $0.72, [-0.04568724075, 0.2729883564]$ ]], [ $0.73, [-0.04567081696, 0.2729699334]$ ]], [ $0.74, [-0.04565555251, 0.2729528103]$ ]], [ $0.75, [-0.04564136559, 0.2729368954]$ ]], [ $0.76, [-0.04562818007, 0.2729221034]$ ]], [ $0.77, [-0.04561592526, 0.2729083551]$ ]], [ $0.78, [-0.04560453548, 0.2728955769]$ ]], [ $0.79, [-0.04559394960, 0.2728837003]$ ]], [ $0.80, [-0.04558411093, 0.2728726618]$ ]], [ $0.81, [-0.04557496670, 0.2728624022]$ ]], [ $0.82, [-0.04556646786, 0.2728528665]$ ]], [ $0.83, [-0.04555856887, 0.2728440037]$ ]], [ $0.84, [-0.04555122739, 0.2728357663]$ ]], [ $0.85, [-0.04554440411, 0.2728281102]$ ]], [ $0.86, [-0.04553806239, 0.2728209943]$ ]], [ $0.87, [-0.04553216827, 0.2728143806]$ ]], [ $0.88, [-0.04552669013, 0.2728082335]$ ]], [ $0.89, [-0.04552159863, 0.2728025202]$ ]], [ $0.90, [-0.04551686644, 0.2727972101]$ ]], [ $0.91, [-0.04551246821, 0.2727922747]$ ]], [ $0.92, [-0.04550838043, 0.2727876876]$ ]], [ $0.93, [-0.04550458115, 0.2727834242]$ ]], [ $0.94, [-0.04550105000, 0.2727794616]$ ]], [ $0.95, [-0.04549776805, 0.2727757787]$ ]], [ $0.96, [-0.04549471775, 0.2727723557]$ ]], [ $0.97, [-0.04549188268, 0.2727691742]$ ]], [ $0.98, [-0.04548924772, 0.2727662172]$ ]], [ $0.99, [-0.04548679869, 0.2727634689]$ ]], [ $1.00, [-0.04548452248, 0.2727609146]$ ]], [ $1.01, [-0.04548240695, 0.2727585405]$ ]], [ $1.02, [-0.04548044069, 0.2727563339]$ ]], [ $1.03, [-0.04547861322, 0.2727542831]$ ]], [ $1.04, [-0.04547691473, 0.2727523770]$ ]], [ $1.05, [-0.04547533610, 0.2727506054]$ ]], [ $1.06, [-0.04547386888, 0.2727489588]$ ]], [ $1.07, [-0.04547250520, 0.2727474284]$ ]], [ $1.08, [-0.04547123775, 0.2727460060]$ ]], [ $1.09, [-0.04547005975, 0.2727446840]$ ]], [ $1.10, [-0.04546896489, 0.2727434553]$ ]], [ $1.11,$

[ $-0.04546794729, 0.2727423133$ ]], [ $1.12, [-0.04546700151, 0.2727412519]$ ]], [ $1.13, [-0.04546612250, 0.2727402654]$ ]], [ $1.14, [-0.04546530550, 0.2727393485]$ ]], [ $1.15, [-0.04546454614, 0.2727384963]$ ]], [ $1.16, [-0.04546384040, 0.2727377043]$ ]], [ $1.17, [-0.04546318447, 0.2727369682]$ ]], [ $1.18, [-0.04546257481, 0.2727362840]$ ]], [ $1.19, [-0.04546200820, 0.2727356481]$ ]], [ $1.20, [-0.04546148153, 0.2727350570]$ ]], [ $1.21, [-0.04546099206, 0.2727345077]$ ]], [ $1.22, [-0.04546053713, 0.2727339971]$ ]], [ $1.23, [-0.04546011431, 0.2727335225]$ ]], [ $1.24, [-0.04545972130, 0.2727330815]$ ]], [ $1.25, [-0.04545935606, 0.2727326716]$ ]], [ $1.26, [-0.04545901659, 0.2727322906]$ ]], [ $1.27, [-0.04545870105, 0.2727319365]$ ]], [ $1.28, [-0.04545840778, 0.2727316074]$ ]], [ $1.29, [-0.04545813523, 0.2727313015]$ ]], [ $1.30, [-0.04545788191, 0.2727310172]$ ]], [ $1.31, [-0.04545764646, 0.2727307529]$ ]], [ $1.32, [-0.04545742759, 0.2727305073]$ ]], [ $1.33, [-0.04545722417, 0.2727302790]$ ]], [ $1.34, [-0.04545703514, 0.2727300669]$ ]], [ $1.35, [-0.04545685943, 0.2727298697]$ ]], [ $1.36, [-0.04545669613, 0.2727296864]$ ]], [ $1.37, [-0.04545654436, 0.2727295161]$ ]], [ $1.38, [-0.04545640328, 0.2727293578]$ ]], [ $1.39, [-0.04545627219, 0.2727292107]$ ]], [ $1.40, [-0.04545615034, 0.2727290739]$ ]], [ $1.41, [-0.04545603709, 0.2727289468]$ ]], [ $1.42, [-0.04545593182, 0.2727288287]$ ]], [ $1.43, [-0.04545583400, 0.2727287189]$ ]], [ $1.44, [-0.04545574306, 0.2727286168]$ ]], [ $1.45, [-0.04545565856, 0.2727285219]$ ]], [ $1.46, [-0.04545558003, 0.2727284337]$ ]], [ $1.47, [-0.04545550699, 0.2727283518]$ ]], [ $1.48, [-0.04545543912, 0.2727282757]$ ]], [ $1.49, [-0.04545537604, 0.2727282049]$ ]], [ $1.50, [-0.04545531742, 0.2727281391]$ ]], [ $1.51, [-0.04545526297, 0.2727280780]$ ]], [ $1.52, [-0.04545521233, 0.2727280212]$ ]], [ $1.53, [-0.04545516526, 0.2727279684]$ ]], [ $1.54, [-0.04545512153, 0.2727279193]$ ]], [ $1.55, [-0.04545508088, 0.2727278737]$ ]], [ $1.56, [-0.04545504309, 0.2727278313]$ ]], [ $1.57, [-0.04545500796, 0.2727277919]$ ]], [ $1.58, [-0.04545497534, 0.2727277553]$ ]], [ $1.59, [-0.04545494500, 0.2727277212]$ ]], [ $1.60, [-0.04545491681, 0.2727276895]$ ]], [ $1.61, [-0.04545489063, 0.2727276601]$ ]], [ $1.62, [-0.04545486626, 0.2727276328]$ ]], [ $1.63, [-0.04545484363, 0.2727276074]$ ]], [ $1.64, [-0.04545482259, 0.2727275838]$ ]], [ $1.65, [-0.04545480303, 0.2727275618]$ ]], [ $1.66, [-0.04545478486, 0.2727275414]$ ]], [ $1.67, [-0.04545476796, 0.2727275224]$ ]], [ $1.68, [-0.04545475224, 0.2727275048]$ ]], [ $1.69, [-0.04545473764, 0.2727274884]$ ]], [ $1.70, [-0.04545472408, 0.2727274732]$ ]], [ $1.71, [-0.04545471146, 0.2727274590]$ ]], [ $1.72, [-0.04545469973, 0.2727274459]$ ]], [ $1.73, [-0.04545468886, 0.2727274337]$ ]], [ $1.74, [-0.04545467873, 0.2727274223]$ ]], [ $1.75, [-0.04545466933, 0.2727274118]$ ]], [ $1.76, [-0.04545466058, 0.2727274020]$ ]], [ $1.77, [-0.04545465246, 0.2727273929]$ ]], [ $1.78, [-0.04545464490, 0.2727273844]$ ]], [ $1.79, [-0.04545463790, 0.2727273765]$ ]], [ $1.80, [-0.04545463137, 0.2727273692]$ ]], [ $1.81, [-0.04545462531, 0.2727273624]$ ]], [ $1.82, [-0.04545461970, 0.2727273561]$ ]], [ $1.83, [-0.04545461444, 0.2727273502]$ ]], [ $1.84, [-0.04545460957, 0.2727273447]$ ]], [ $1.85, [-0.04545460505, 0.2727273396]$ ]], [ $1.86, [-0.04545460085, 0.2727273349]$ ]], [ $1.87,$

```

[ [ -0.04545459692, 0.2727273305 ] ], [ 1.88, [ -0.04545459329, 0.2727273264 ] ], [ 1.89,
[ -0.04545458992, 0.2727273226 ] ], [ 1.90, [ -0.04545458679, 0.2727273191 ] ], [ 1.91,
[ -0.04545458389, 0.2727273158 ] ], [ 1.92, [ -0.04545458117, 0.2727273128 ] ], [ 1.93,
[ -0.04545457866, 0.2727273100 ] ], [ 1.94, [ -0.04545457633, 0.2727273074 ] ], [ 1.95,
[ -0.04545457414, 0.2727273049 ] ], [ 1.96, [ -0.04545457210, 0.2727273026 ] ], [ 1.97,
[ -0.04545457021, 0.2727273005 ] ], [ 1.98, [ -0.04545456844, 0.2727272985 ] ], [ 1.99,
[ -0.04545456679, 0.2727272967 ] ], [ 2.00, [ -0.04545456531, 0.2727272950 ] ], [ 2.01,
[ -0.04545456392, 0.2727272934 ] ] ]

```

>  $F := \text{RandNice}([x, y], 8)$

$$F := [(6 - 5x - 6y)(7 - 4x - 7y), (3 - 6x - 5y)(7 - 7x - 3y)] \quad (23)$$

> #(i)

>  $\text{sys} := \{(6 - 5x - 6y)(7 - 4x - 7y) = 0, (3 - 6x - 5y)(7 - 7x - 3y) = 0\}$

$$\text{sys} := \{(3 - 6x - 5y)(7 - 7x - 3y) = 0, (6 - 5x - 6y)(7 - 4x - 7y) = 0\} \quad (24)$$

>  $\text{solve}(\text{sys}, \{x, y\})$

$$\left\{ x = -\frac{12}{11}, y = \frac{21}{11} \right\}, \left\{ x = -\frac{7}{11}, y = \frac{15}{11} \right\}, \left\{ x = \frac{8}{9}, y = \frac{7}{27} \right\}, \left\{ x = \frac{28}{37}, y = \frac{21}{37} \right\} \quad (25)$$

> #These are the equilibrium points.

> #(ii)

>  $J := \text{Matrix}([[\text{diff}(F[1], x), \text{diff}(F[1], y)], [\text{diff}(F[2], x), \text{diff}(F[2], y)]])$

$$J := \begin{bmatrix} -59 + 40x + 59y & -84 + 59x + 84y \\ -63 + 84x + 53y & -44 + 53x + 30y \end{bmatrix} \quad (26)$$

> #@  $\left\{ x = -\frac{12}{11}, y = \frac{21}{11} \right\}$

```

> J := subs(x = -12/11, J) :
> J := subs(y = 21/11, J)

```

$$J := \begin{bmatrix} 10 & 12 \\ -\frac{588}{11} & -\frac{490}{11} \end{bmatrix} \quad (27)$$

```
> evalf(Eigenvalues(J))
```

$$\begin{bmatrix} -7.15605255 \\ -27.38940199 \end{bmatrix} \quad (28)$$

#This point is stable.

```
> J := Matrix([ [diff(F[1], x), diff(F[1], y)], [diff(F[2], x), diff(F[2], y)] ])
```

$$J := \begin{bmatrix} -59 + 40x + 59y & -84 + 59x + 84y \\ -63 + 84x + 53y & -44 + 53x + 30y \end{bmatrix} \quad (29)$$

```
#@ {x = -7/11, y = 15/11}
```

```
> J := subs(x = -7/11, J) :
```

```
> J := subs(y = 15/11, J)
```

$$J := \begin{bmatrix} -4 & -7 \\ -\frac{486}{11} & -\frac{405}{11} \end{bmatrix} \quad (30)$$

```
> evalf(Eigenvalues(J))
```

$$\begin{bmatrix} 3.64358028 \\ -44.46176210 \end{bmatrix} \quad (31)$$

#This point is not stable.

>  $J := \text{Matrix}([[\text{diff}(F[1], x), \text{diff}(F[1], y)], [\text{diff}(F[2], x), \text{diff}(F[2], y)]])$

$$J := \begin{bmatrix} -59 + 40x + 59y & -84 + 59x + 84y \\ -63 + 84x + 53y & -44 + 53x + 30y \end{bmatrix} \quad (32)$$

>  $\# @ \left\{ x = \frac{8}{9}, y = \frac{7}{27} \right\}$

>  $J := \text{subs}\left(x = \frac{8}{9}, J\right) :$

>  $J := \text{subs}\left(y = \frac{7}{27}, J\right)$

$$J := \begin{bmatrix} -\frac{220}{27} & -\frac{88}{9} \\ \frac{686}{27} & \frac{98}{9} \end{bmatrix} \quad (33)$$

>  $\text{evalf}(\text{Eigenvalues}(J))$

$$\begin{bmatrix} 1.370370370 + 12.56287343 \text{I} \\ 1.370370370 - 12.56287343 \text{I} \end{bmatrix} \quad (34)$$

> #This point is not stable.

>  $J := \text{Matrix}([[\text{diff}(F[1], x), \text{diff}(F[1], y)], [\text{diff}(F[2], x), \text{diff}(F[2], y)]])$

$$J := \begin{bmatrix} -59 + 40x + 59y & -84 + 59x + 84y \\ -63 + 84x + 53y & -44 + 53x + 30y \end{bmatrix} \quad (35)$$

> #@  $\left\{x = \frac{28}{37}, y = \frac{21}{37}\right\}$

>  $J := \text{subs}\left(x = \frac{28}{37}, J\right) :$

>  $J := \text{subs}\left(y = \frac{21}{37}, J\right)$

$$J := \begin{bmatrix} \frac{176}{37} & \frac{308}{37} \\ \frac{1134}{37} & \frac{486}{37} \end{bmatrix} \quad (36)$$

>  $\text{evalf}(\text{Eigenvalues}(J))$

$$\begin{bmatrix} 25.45892865 \\ -7.567036754 \end{bmatrix} \quad (37)$$

> #This point is not stable.

#(iii)

> #@  $\left\{x = -\frac{12}{11}, y = \frac{21}{11}\right\}$

>  $\text{Dis2}\left(F, x, y, \left[-\frac{12}{11} + 0.1, \frac{21}{11} + 0.1\right], 0.01, 2\right);$   
 $[[0.01, [-0.990909091, 2.009090909]], [0.02, [-0.9568090913, 1.922090909]], [0.03,$   
 $[-0.9371430026, 1.853119534]], [0.04, [-0.9275162176, 1.801696233]], [0.05,$   
 $[-0.9242337659, 1.765837453]], [0.06, [-0.9246687848, 1.742646218]], [0.07,$   
 $[-0.9271805301, 1.729024387]], [0.08, [-0.9308305876, 1.722212553]], [0.09,$   
 $[-0.9351052086, 1.720035151]], [0.10, [-0.9397236843, 1.720911910]], [0.11,$   
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>  
>  
>  
>  
>  
>  
>

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> #@ { $x = -\frac{7}{11}, y = \frac{15}{11}$ }
>
> Dis2(F, x, y,  $\left[ -\frac{7}{11} + 0.1, \frac{15}{11} + 0.1 \right], 0.01, 2$ )
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 $\times 10^{166683925920211}]], [1.39, [2.381141286 \times 10^{333367851840423}, 2.227237262$   
 $\times 10^{333367851840423}]], [1.40, [6.346399100 \times 10^{666735703680846}, 5.936202378$   
 $\times 10^{666735703680846}]], [1.41, [4.508289632 \times 10^{1333471407361693}, 4.216898304$   
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Float(∞)]], [1.91, [Float(∞), Float(∞)]], [1.92, [Float(∞), Float(∞)]], [1.93, [
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[1.96, [Float(∞), Float(∞)]], [1.97, [Float(∞), Float(∞)]], [1.98, [Float(∞),
Float(∞)]], [1.99, [Float(∞), Float(∞)]], [2.00, [Float(∞), Float(∞)]], [2.01, [
Float(∞), Float(∞)]]]]

>
>
>
>
> #@ { $x = \frac{8}{9}, y = \frac{7}{27}$ }
>
> Dis2( $F, x, y, \left[ \frac{8}{9} + 0.1, \frac{7}{27} + 0.1 \right], 0.01, 2$ )
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[0.9950230824, 0.6055403919]], [0.06, [1.026815705, 0.7124088787]], [0.07,
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[10.95426639, 10.76840790]], [0.12, [138.1639979, 129.6500164]], [0.13,
[21394.50163, 20018.51286]], [0.14, [5.125368593  $\times 10^8$ , 4.793448708  $\times 10^8$ ]], [0.15,
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 $\times 10^{34}$ ]], [0.17, [1.047796258  $\times 10^{70}$ , 9.800825424  $\times 10^{69}$ ]], [0.18, [1.228898175
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1.071027667  $\times 10^{1121}$ ]], [0.22, [1.467559325  $\times 10^{2242}$ , 1.372704073  $\times 10^{2242}$ ]], [0.23,
[2.410728543  $\times 10^{4484}$ , 2.254912300  $\times 10^{4484}$ ]], [0.24, [6.505095856  $\times 10^{8968}$ ,
6.084641673  $\times 10^{8968}$ ]], [0.25, [4.736575204  $\times 10^{17937}$ , 4.430428791  $\times 10^{17937}$ ]], [0.26,
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6.602527599  $\times 10^{71750}$ ]], [0.28, [5.577182575  $\times 10^{143501}$ , 5.216703819  $\times 10^{143501}$ ]],
[0.29, [3.481663325  $\times 10^{287003}$ , 3.256627542  $\times 10^{287003}$ ]], [0.30, [1.356846113
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$$\begin{aligned}
& \times 10^{315563785236296889}], [0.70, [9.345030296 \times 10^{631127570472593778}, 8.741018356 \\
& \times 10^{631127570472593778}], [0.71, [9.775038504 \times 10^{1262255140945187557}, 9.143233172 \\
& \times 10^{1262255140945187557}], [0.72, [1.069532542 \times 10^{2524510281890375116}, 1.000403774 \\
& \times 10^{2524510281890375116}], [0.73, [1.280398201 \times 10^{5049020563780750232}, 1.197640225 \\
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& Float(\infty)]], [0.87, [Float(\infty), Float(\infty)]], [0.88, [Float(\infty), Float(\infty)]], [0.89, [ \\
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& Float(\infty)]], [1.59, [Float(\infty), Float(\infty)]], [1.60, [Float(\infty), Float(\infty)]], [1.61, [
\end{aligned}$$



$[5.271510835 \times 10^{7996}, 4.930789142 \times 10^{7996}]]$ , [0.22,  $[3.110478950 \times 10^{15993}, 2.909434480 \times 10^{15993}]]$ , [0.23,  $[1.082957911 \times 10^{31987}, 1.012961405 \times 10^{31987}]]$ , [0.24,  $[1.312744501 \times 10^{63974}, 1.227895833 \times 10^{63974}]]$ , [0.25,  $[1.928934426 \times 10^{127948}, 1.804258596 \times 10^{127948}]]$ , [0.26,  $[4.164779164 \times 10^{255896}, 3.895590486 \times 10^{255896}]]$ , [0.27,  $[1.941516141 \times 10^{511793}, 1.816027096 \times 10^{511793}]]$ , [0.28,  $[4.219286930 \times 10^{1023586}, 3.946575170 \times 10^{1023586}]]$ , [0.29,  $[1.992669027 \times 10^{2047173}, 1.863873737 \times 10^{2047173}]]$ , [0.30,  $[4.444545846 \times 10^{4094346}, 4.157274569 \times 10^{4094346}]]$ , [0.31,  $[2.211117540 \times 10^{8188693}, 2.068202927 \times 10^{8188693}]]$ , [0.32,  $[5.472436224 \times 10^{16377386}, 5.118727706 \times 10^{16377386}]]$ , [0.33,  $[3.352111589 \times 10^{32754773}, 3.135449324 \times 10^{32754773}]]$ , [0.34,  $[1.257749010 \times 10^{65509547}, 1.176454954 \times 10^{65509547}]]$ , [0.35,  $[1.770700125 \times 10^{131019094}, 1.656251697 \times 10^{131019094}]]$ , [0.36,  $[3.509514856 \times 10^{262038188}, 3.282678902 \times 10^{262038188}]]$ , [0.37,  $[1.378641095 \times 10^{524076377}, 1.289533232 \times 10^{524076377}]]$ , [0.38,  $[2.127450624 \times 10^{1048152754}, 1.989943785 \times 10^{1048152754}]]$ , [0.39,  $[5.066126483 \times 10^{2096305508}, 4.738679612 \times 10^{2096305508}]]$ , [0.40,  $[2.872824565 \times 10^{4192611017}, 2.687140809 \times 10^{4192611017}]]$ , [0.41,  $[9.237942632 \times 10^{8385222034}, 8.640852259 \times 10^{8385222034}]]$ , [0.42,  $[9.552291597 \times 10^{16770444069}, 8.934883413 \times 10^{16770444069}]]$ , [0.43,  $[1.021344354 \times 10^{33540888140}, 9.553302082 \times 10^{33540888139}]]$ , [0.44,  $[1.167619754 \times 10^{67081776280}, 1.092151162 \times 10^{67081776280}]]$ , [0.45,  $[1.526018915 \times 10^{134163552560}, 1.427385351 \times 10^{134163552560}]]$ , [0.46,  $[2.606614957 \times 10^{268327105120}, 2.438137539 \times 10^{268327105120}]]$ , [0.47,  $[7.605203069 \times 10^{536654210240}, 7.113644107 \times 10^{536654210240}]]$ , [0.48,  $[6.474089210 \times 10^{1073308420481}, 6.055639287 \times 10^{1073308420481}]]$ , [0.49,  $[4.691529032 \times 10^{2146616840963}, 4.388294109 \times 10^{2146616840963}]]$ , [0.50,  $[2.463688894 \times 10^{4293233681927}, 2.304449441 \times 10^{4293233681927}]]$ , [0.51,  $[6.794050663 \times 10^{8586467363854}, 6.354920170 \times 10^{8586467363854}]]$ , [0.52,  $[5.166716250 \times 10^{17172934727709}, 4.832767809 \times 10^{17172934727709}]]$ , [0.53,  $[2.988039071 \times 10^{34345869455419}, 2.794908475 \times 10^{34345869455419}]]$ , [0.54,  $[9.993775594 \times 10^{68691738910838}, 9.347832289 \times 10^{68691738910838}]]$ , [0.55,  $[1.117934184 \times 10^{137383477821678}, 1.045676998 \times 10^{137383477821678}]]$ , [0.56,  $[1.398909186 \times 10^{274766955643356}, 1.308491302 \times 10^{274766955643356}]]$ , [0.57,  $[2.190463863 \times 10^{549533911286712}, 2.048884193 \times 10^{549533911286712}]]$ , [0.58,  $[5.370679494 \times 10^{1099067822573424}, 5.023547973 \times 10^{1099067822573424}]]$ , [0.59,  $[3.228609502 \times 10^{2198135645146849}, 3.019929741$ ]

$$\begin{aligned}
& \times 10^{2198135645146849}], [0.60, [1.166777621 \times 10^{4396271290293699}, 1.091363460 \\
& \times 10^{4396271290293699}], [0.61, [1.523818459 \times 10^{8792542580587398}, 1.425327123 \\
& \times 10^{8792542580587398}], [0.62, [2.599103121 \times 10^{17585085161174796}, 2.431111227 \\
& \times 10^{17585085161174796}], [0.63, [7.561432338 \times 10^{35170170322349592}, 7.072702479 \\
& \times 10^{35170170322349592}], [0.64, [6.399782148 \times 10^{70340340644699185}, 5.986135030 \\
& \times 10^{70340340644699185}], [0.65, [4.584452006 \times 10^{140680681289398371}, 4.288137959 \\
& \times 10^{140680681289398371}], [0.66, [2.352512341 \times 10^{281361362578796743}, 2.200458737 \\
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\end{aligned}$$

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Float(∞)]], [1.81, [Float(∞), Float(∞)]], [1.82, [Float(∞), Float(∞)]], [1.83,
[Float(∞), Float(∞)]], [1.84, [Float(∞), Float(∞)]], [1.85, [Float(∞), Float(∞)]],
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Float(∞)]], [1.89, [Float(∞), Float(∞)]], [1.90, [Float(∞), Float(∞)]], [1.91,
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Float(∞)]], [1.97, [Float(∞), Float(∞)]], [1.98, [Float(∞), Float(∞)]], [1.99,
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>

>  $F := \text{RandNice}([x, y], 8)$  (42)  
      $F := [(5 - 7x - 7y)(2 - 5x - 8y), (6 - 2x - 3y)(4 - 4x - 6y)]$   
> #(i)  
>

$$\begin{aligned} > \text{sys} := \{(5 - 7x - 7y) \cdot (2 - 5x - 8y) = 0, (6 - 2x - 3y) \cdot (4 - 4x - 6y) = 0\} \\ &\quad \text{sys} := \{(5 - 7x - 7y)(2 - 5x - 8y) = 0, (6 - 2x - 3y)(4 - 4x - 6y) = 0\} \end{aligned} \quad (43)$$

$$\begin{aligned} > \text{solve}(\text{sys}, \{x, y\}) \\ &\quad \left\{ x = \frac{1}{7}, y = \frac{4}{7} \right\}, \{x = 10, y = -6\}, \left\{ x = -\frac{27}{7}, y = \frac{32}{7} \right\}, \{x = 42, y = -26\} \end{aligned} \quad (44)$$

> #These are the equilibrium points.

> #(ii)

$$\begin{aligned} > J := \text{Matrix}([[\text{diff}(F[1], x), \text{diff}(F[1], y)], [\text{diff}(F[2], x), \text{diff}(F[2], y)]]) \\ &\quad J := \begin{bmatrix} -39 + 70x + 91y & -54 + 91x + 112y \\ -32 + 16x + 24y & -48 + 24x + 36y \end{bmatrix} \end{aligned} \quad (45)$$

$$\begin{aligned} > \# @ \left\{ x = \frac{1}{7}, y = \frac{4}{7} \right\} \end{aligned}$$

$$\begin{aligned} > J := \text{subs}\left(x = \frac{1}{7}, J\right) \\ &\quad J := \begin{bmatrix} -29 + 91y & -41 + 112y \\ -\frac{208}{7} + 24y & -\frac{312}{7} + 36y \end{bmatrix} \end{aligned} \quad (46)$$

$$\begin{aligned} > J := \text{subs}\left(y = \frac{4}{7}, J\right) \\ &\quad J := \begin{bmatrix} 23 & 23 \\ -16 & -24 \end{bmatrix} \end{aligned} \quad (47)$$

$$\begin{aligned} > \text{evalf}(\text{Eigenvalues}(J)) \\ &\quad \begin{bmatrix} 13.07387196 \\ -14.07387196 \end{bmatrix} \end{aligned} \quad (48)$$

> #This point is not stable.

$$\begin{aligned} > \# @ \{x = 10, y = -6\} \end{aligned}$$

$$\begin{aligned} > J := \text{Matrix}([[\text{diff}(F[1], x), \text{diff}(F[1], y)], [\text{diff}(F[2], x), \text{diff}(F[2], y)]]) \\ &\quad J := \begin{bmatrix} -39 + 70x + 91y & -54 + 91x + 112y \\ -32 + 16x + 24y & -48 + 24x + 36y \end{bmatrix} \end{aligned} \quad (49)$$

$$> J := \text{subs}(x=10, J) \\ J := \begin{bmatrix} 661 + 91y & 856 + 112y \\ 128 + 24y & 192 + 36y \end{bmatrix} \quad (50)$$

$$> J := \text{subs}(y=-6, J) \\ J := \begin{bmatrix} 115 & 184 \\ -16 & -24 \end{bmatrix} \quad (51)$$

$$> \text{evalf}(\text{Eigenvalues}(J)) \\ \begin{bmatrix} 88.93097972 \\ 2.06902028 \end{bmatrix} \quad (52)$$

> #This point is not stable.

$$> \# @ \left\{ x = -\frac{27}{7}, y = \frac{32}{7} \right\}$$

$$> J := \text{Matrix}([[\text{diff}(F[1], x), \text{diff}(F[1], y)], [\text{diff}(F[2], x), \text{diff}(F[2], y)]]) \\ J := \begin{bmatrix} -39 + 70x + 91y & -54 + 91x + 112y \\ -32 + 16x + 24y & -48 + 24x + 36y \end{bmatrix} \quad (53)$$

$$> J := \text{subs}\left(x = -\frac{27}{7}, J\right) \\ J := \begin{bmatrix} -309 + 91y & -405 + 112y \\ -\frac{656}{7} + 24y & -\frac{984}{7} + 36y \end{bmatrix} \quad (54)$$

$$> J := \text{subs}\left(y = \frac{32}{7}, J\right) \\ J := \begin{bmatrix} 107 & 107 \\ 16 & 24 \end{bmatrix} \quad (55)$$

$$> \text{evalf}(\text{Eigenvalues}(J)) \\ \begin{bmatrix} 124.1024744 \\ 6.89752565 \end{bmatrix} \quad (56)$$

> #This point is not stable.

```

> #@ {x=42, y=-26}
>
>
> J := Matrix( [[diff(F[1],x), diff(F[1],y)], [diff(F[2],x), diff(F[2],y)]] )
      J := 
$$\begin{bmatrix} -39 + 70x + 91y & -54 + 91x + 112y \\ -32 + 16x + 24y & -48 + 24x + 36y \end{bmatrix} \quad (57)$$

> J := subs(x=42, J)
      J := 
$$\begin{bmatrix} 2901 + 91y & 3768 + 112y \\ 640 + 24y & 960 + 36y \end{bmatrix} \quad (58)$$

> J := subs(y=-26, J)
      J := 
$$\begin{bmatrix} 535 & 856 \\ 16 & 24 \end{bmatrix} \quad (59)$$

> evalf(Eigenvalues(J) )
      
$$\begin{bmatrix} 560.5271339 \\ -1.5271339 \end{bmatrix} \quad (60)$$

> #This point is not stable.
>
>
>
>
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>
>
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>
> #(iii)
>
> #@ {x =  $\frac{1}{7}$ , y =  $\frac{4}{7}$ }
>
>
>
> Dis2(F, x, y,  $\left[ \frac{1}{7} + 0.1, \frac{4}{7} + 0.1 \right]$ , 0.01, 2)
[[0.01, [0.2428571429, 0.6714285714]], [0.02, [0.3070571429, 0.6364285714]], [0.03, [0.3812881469, 0.6000355226]], [0.04, [0.4692693407, 0.5613531337]], [0.05, [0.5763816080, 0.5192978545]], [0.06, [0.7108382978, 0.4725459733]], [0.07, [0.8860086818, 0.4194897892]], [0.08, [1.125460088, 0.3582889088]], [0.09,

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 Float( $\infty$ )]], [1.09, [Float( $\infty$ ), Float( $\infty$ )]], [1.10, [Float( $\infty$ ), Float( $\infty$ )]]]$



```

> #@ {x=10, y=-6}
>
> Dis2(F, x, y, [10 + 0.1, -6 + 0.1], 0.01, 2)
[[0.01, [10.1, -5.9]], [0.02, [10.4172, -5.9350]], [0.03, [11.10454292, -5.996158713]], [0.04, [12.81270979, -6.075185340]], [0.05, [18.48867650, -5.924003896]], [0.06, [54.20093836, -1.379955809]], [0.07, [995.1203869, 199.5894542]], [0.08, [550140.2185, 133844.9542]], [0.09, [1.829678365 × 1011, 4.510887744 × 1010]], [0.10, [2.036718536 × 1022, 5.025277976 × 1021]], [0.11, [2.524688971 × 1044, 6.229557886 × 1043]], [0.12, [3.879460778 × 1088, 9.572423624 × 1087]], [0.13, [9.160072446 × 10176, 2.260213810 × 10176]], [0.14, [5.106860899 × 10353, 1.260098948 × 10353]], [0.15, [1.587319207 × 10707, 3.916651155 × 10706]], [0.16, [1.533503448 × 101414, 3.783862770 × 101413]], [0.17, [1.431283709 × 102828, 3.531639359 × 102827]], [0.18, [1.246831225 × 105656, 3.076509714 × 105655]], [0.19, [9.461751862 × 1011311, 2.334652109 × 1011311]], [0.20, [5.448780620 × 1022623, 1.344466369 × 1022623]], [0.21, [1.806986297 × 1045247, 4.458671538 × 1045246]], [0.22, [1.987311441 × 1090494, 4.903617125 × 1090493]], [0.23, [2.403743260 × 10180988, 5.931147168 × 10180987]], [0.24, [3.516676126 × 10361976, 8.677267655 × 10361975]], [0.25, [7.526983434 × 10723952, 1.857255190 × 10723952]], [0.26, [3.448245153 × 101447905, 8.508416774 × 101447904]], [0.27, [7.236898522 × 102895810, 1.785677817 × 102895810]], [0.28, [3.187580636 × 105791621, 7.865236760 × 105791620]], [0.29, [6.184129476 × 1011583242, 1.525910967 × 1011583242]], [0.30, [2.327626868 × 1023166485, 5.743332796 × 1023166484]], [0.31, [3.297485827 × 1046332970, 8.136423733 × 1046332969]], [0.32, [6.617928782 × 1092665940, 1.632949333 × 1092665940]], [0.33, [2.665633222 × 10185331881, 6.577350917 × 10185331880]], [0.34, [4.324710082 × 10370663762, 1.067106142 × 10370663762]], [0.35, [1.138335321 × 10741327525, 2.808800103 × 10741327524]], [0.36, [7.886723903 × 101482655049, 1.946019815 × 101482655049]], [0.37, [3.785728712 × 102965310099, 9.341144917 × 102965310098]], [0.38, [8.722785477 × 105930620198, 2.152314902 × 105930620198]], [0.39, [4.630912741 × 1011861240397, 1.142660510 × 1011861240397]], [0.40, [1.305237100 × 1023722480795, 3.220624039 × 1023722480794]], [0.41, [1.036895605 × 1047444961590, 2.558501371 × 1047444961589]], [0.42, [6.543743707 × 1094889923179, 1.614644442 × 1094889923179]], [0.43, [2.606206220 × 10189779846359, 6.430716995 × 10189779846358]], [0.44, [4.134031372 × 10379559692718,

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$1.020056878 \times 10^{379559692718}]], [0.45, [1.040168626 \times 10^{759119385437}, 2.566577430$   
 $\times 10^{759119385436}]], [0.46, [6.585120320 \times 10^{1518238770873}, 1.624853968$   
 $\times 10^{1518238770873}]], [0.47, [2.639268919 \times 10^{3036477541747}, 6.512297976$   
 $\times 10^{3036477541746}]], [0.48, [4.239586502 \times 10^{6072955083494}, 1.046102215$   
 $\times 10^{6072955083494}]], [0.49, [1.093964467 \times 10^{12145910166989}, 2.699316668$   
 $\times 10^{12145910166988}]], [0.50, [7.283877712 \times 10^{24291820333977}, 1.797269757$   
 $\times 10^{24291820333977}]], [0.51, [3.229100083 \times 10^{48583640667955}, 7.967684454$   
 $\times 10^{48583640667954}]], [0.52, [6.346279945 \times 10^{97167281335910}, 1.565920992$   
 $\times 10^{97167281335910}]], [0.53, [2.451289841 \times 10^{194334562671821}, 6.048466589$   
 $\times 10^{194334562671820}]], [0.54, [3.657173336 \times 10^{388669125343642}, 9.023939304$   
 $\times 10^{388669125343641}]], [0.55, [8.140429201 \times 10^{777338250687284}, 2.008620653$   
 $\times 10^{777338250687284}]], [0.56, [4.033209866 \times 10^{1554676501374569}, 9.951795464$   
 $\times 10^{1554676501374568}]], [0.57, [9.900516588 \times 10^{3109353002749138}, 2.442915676$   
 $\times 10^{3109353002749138}]], [0.58, [5.965844450 \times 10^{6218706005498277}, 1.472049948$   
 $\times 10^{6218706005498277}]], [0.59, [2.166207551 \times 10^{12437412010996555}, 5.345036631$   
 $\times 10^{12437412010996554}]], [0.60, [2.855987780 \times 10^{24874824021993110}, 7.047043710$   
 $\times 10^{24874824021993109}]], [0.61, [4.964424427 \times 10^{49749648043986220}, 1.224953279$   
 $\times 10^{49749648043986220}]], [0.62, [1.500009542 \times 10^{99499296087972441}, 3.701217802$   
 $\times 10^{99499296087972440}]], [0.63, [1.369443936 \times 10^{198998592175944882}, 3.379052024$   
 $\times 10^{198998592175944881}]], [0.64, [1.141418031 \times 10^{397997184351889764}, 2.816406574$   
 $\times 10^{397997184351889763}]], [0.65, [7.929497595 \times 10^{795994368703779527}, 1.956574064$   
 $\times 10^{795994368703779527}]], [0.66, [3.826903909 \times 10^{1591988737407559055}, 9.442743180$   
 $\times 10^{1591988737407559054}]], [0.67, [8.913562807 \times 10^{3183977474815118110}, 2.199388499$   
 $\times 10^{3183977474815118110}]], [0.68, [4.835694679 \times 10^{6367954949630236221}, 1.193189692$   
 $\times 10^{6367954949630236221}]], [0.69, [Float( $\infty$ ), Float( $\infty$ )]], [0.70, [Float( $\infty$ ), Float( $\infty$ )]],  
[0.71, [Float( $\infty$ ), Float( $\infty$ )]], [0.72, [Float( $\infty$ ), Float( $\infty$ )]], [0.73, [Float( $\infty$ ),  
Float( $\infty$ )]], [0.74, [Float( $\infty$ ), Float( $\infty$ )]], [0.75, [Float( $\infty$ ), Float( $\infty$ )]], [0.76, [  
Float( $\infty$ ), Float( $\infty$ )]], [0.77, [Float( $\infty$ ), Float( $\infty$ )]], [0.78, [Float( $\infty$ ), Float( $\infty$ )]],  
[0.79, [Float( $\infty$ ), Float( $\infty$ )]], [0.80, [Float( $\infty$ ), Float( $\infty$ )]], [0.81, [Float( $\infty$ ),  
Float( $\infty$ )]], [0.82, [Float( $\infty$ ), Float( $\infty$ )]], [0.83, [Float( $\infty$ ), Float( $\infty$ )]], [0.84, [  
Float( $\infty$ ), Float( $\infty$ )]], [0.85, [Float( $\infty$ ), Float( $\infty$ )]], [0.86, [Float( $\infty$ ), Float( $\infty$ )]],  
[0.87, [Float( $\infty$ ), Float( $\infty$ )]], [0.88, [Float( $\infty$ ), Float( $\infty$ )]], [0.89, [Float( $\infty$ ),  
Float( $\infty$ )]], [0.90, [Float( $\infty$ ), Float( $\infty$ )]], [0.91, [Float( $\infty$ ), Float( $\infty$ )]], [0.92, [  
Float( $\infty$ ), Float( $\infty$ )]], [0.93, [Float( $\infty$ ), Float( $\infty$ )]], [0.94, [Float( $\infty$ ), Float( $\infty$ )]],$



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Float(∞), Float(∞)]], [1.97, [Float(∞), Float(∞)]], [1.98, [Float(∞), Float(∞)]],
[1.99, [Float(∞), Float(∞)]], [2.00, [Float(∞), Float(∞)]], [2.01, [Float(∞),
Float(∞)]]]

```

> #@  $\left\{x = -\frac{27}{7}, y = \frac{32}{7}\right\}$

>  $Dis2(F, x, y, \left[-\frac{27}{7} + 0.1, \frac{32}{7} + 0.1\right], 0.01, 2)$

$\begin{aligned} & [[0.01, [-3.757142857, 4.671428571]], [0.02, [-3.524942857, 4.716428571]], [0.03, \\ & [-2.920106173, 4.828554178]], [0.04, [-1.078763831, 5.180158326]], [0.05, \\ & [6.993804745, 6.860952334]], [0.06, [87.80724330, 25.47202076]], [0.07, \\ & [5137.119481, 1255.775085]], [0.08, [1.599252887 \times 10^7, 3.942319878 \times 10^6]], [0.09, \\ & [1.555931813 \times 10^{14}, 3.838985426 \times 10^{13}]], [0.10, [1.473416223 \times 10^{28}, 3.635587502 \\ & \times 10^{27}]], [0.11, [1.321315117 \times 10^{56}, 3.260295295 \times 10^{55}]], [0.12, [1.062597964 \\ & \times 10^{112}, 2.621920958 \times 10^{111}]], [0.13, [6.872174372 \times 10^{223}, 1.695683487 \times 10^{223}]], \\ & [0.14, [2.874382467 \times 10^{447}, 7.092431918 \times 10^{446}]], [0.15, [5.028579543 \times 10^{894}, \\ & 1.240783315 \times 10^{894}]], [0.16, [1.539029210 \times 10^{1789}, 3.797497385 \times 10^{1788}]], [0.17, \\ & [1.441617148 \times 10^{3578}, 3.557136739 \times 10^{3577}]], [0.18, [1.264899711 \times 10^{7156}, \\ & 3.121093030 \times 10^{7155}]], [0.19, [9.737969294 \times 10^{14311}, 2.402807735 \times 10^{14311}]], [0.20, \\ & [5.771557352 \times 10^{28623}, 1.424110329 \times 10^{28623}]], [0.21, [2.027413086 \times 10^{57247}, \\ & 5.002566447 \times 10^{57246}]], [0.22, [2.501731545 \times 10^{114494}, 6.172929617 \times 10^{114493}]], \\ & [0.23, [3.809233748 \times 10^{228988}, 9.399142719 \times 10^{228987}]], [0.24, [8.831438743 \\ & \times 10^{457976}, 2.179124690 \times 10^{457976}]], [0.25, [4.746998952 \times 10^{915953}, 1.171304351 \\ & \times 10^{915953}]], [0.26, [1.371495812 \times 10^{1831907}, 3.384114951 \times 10^{1831906}]], [0.27, \\ & [1.144841030 \times 10^{3663814}, 2.824852698 \times 10^{3663813}]], [0.28, [7.977128457 \times 10^{7327627}, \\ & 1.968326802 \times 10^{7327627}]], [0.29, [3.873016840 \times 10^{14655255}, 9.556525124 \times 10^{14655254}]], \\ & [0.30, [9.129668001 \times 10^{29310510}, 2.252711652 \times 10^{29310510}]], [0.31, [5.073015434 \\ & \times 10^{58621021}, 1.251747706 \times 10^{58621021}]], [0.32, [1.566349170 \times 10^{117242043}, 3.864908371 \\ & \times 10^{117242042}]], [0.33, [1.493252935 \times 10^{234484086}, 3.684546123 \times 10^{234484085}]], [0.34, \\ & [1.357134740 \times 10^{468968172}, 3.348679540 \times 10^{468968171}]], [0.35, [1.120991062$

$$\begin{aligned}
& \times 10^{937936344}, 2.766003787 \times 10^{937936343}]], [0.36, [7.648222499 \times 10^{1875872687}, \\
& 1.887170479 \times 10^{1875872687}]], [0.37, [3.560223328 \times 10^{3751745375}, 8.784718761 \\
& \times 10^{3751745374}]], [0.38, [7.714551761 \times 10^{7503490750}, 1.903536978 \times 10^{7503490750}]], \\
& [0.39, [3.622243223 \times 10^{15006981501}, 8.937750543 \times 10^{15006981500}]], [0.40, [7.985671319 \\
& \times 10^{30013963002}, 1.970434722 \times 10^{30013963002}]], [0.41, [3.881316661 \times 10^{60027926005}, \\
& 9.577004626 \times 10^{60027926004}]], [0.42, [9.168839429 \times 10^{120055852010}, 2.262377056 \\
& \times 10^{120055852010}]], [0.43, [5.116641021 \times 10^{240111704021}, 1.262512158 \times 10^{240111704021}]], \\
& [0.44, [1.593404762 \times 10^{480223408043}, 3.931667035 \times 10^{480223408042}]], [0.45, \\
& [1.545284453 \times 10^{960446816086}, 3.812931964 \times 10^{960446816085}]], [0.46, [1.453359603 \\
& \times 10^{1920893632172}, 3.586110811 \times 10^{1920893632171}]], [0.47, [1.285589697 \times 10^{3841787264344}, \\
& 3.172144802 \times 10^{3841787264343}]], [0.48, [1.005914296 \times 10^{7683574528688}, 2.482056145 \\
& \times 10^{7683574528687}]], [0.49, [6.158545791 \times 10^{15367149057375}, 1.519598288 \\
& \times 10^{15367149057375}]], [0.50, [2.308407964 \times 10^{30734298114751}, 5.695910864 \\
& \times 10^{30734298114750}]], [0.51, [3.243256835 \times 10^{61468596229502}, 8.002615710 \\
& \times 10^{61468596229501}]], [0.52, [6.402047589 \times 10^{122937192459004}, 1.579681451 \\
& \times 10^{122937192459004}]], [0.53, [2.494560322 \times 10^{245874384918009}, 6.155234893 \\
& \times 10^{245874384918008}]], [0.54, [3.787426683 \times 10^{491748769836018}, 9.345334593 \\
& \times 10^{491748769836017}]], [0.55, [8.730611903 \times 10^{983497539672036}, 2.154246042 \\
& \times 10^{983497539672036}]], [0.56, [4.639226542 \times 10^{1966995079344073}, 1.144711909 \\
& \times 10^{1966995079344073}]], [0.57, [1.309927848 \times 10^{3933990158688147}, 3.232198285 \\
& \times 10^{3933990158688146}]], [0.58, [1.044361767 \times 10^{7867980317376294}, 2.576923848 \\
& \times 10^{7867980317376293}]], [0.59, [6.638319373 \times 10^{15735960634752587}, 1.637980636 \\
& \times 10^{15735960634752587}]], [0.60, [2.682084766 \times 10^{31471921269505175}, 6.617944493 \\
& \times 10^{31471921269505174}]], [0.61, [4.378256618 \times 10^{62943842539010350}, 1.080318551 \\
& \times 10^{62943842539010350}]], [0.62, [1.166698501 \times 10^{125887685078020701}, 2.878785195 \\
& \times 10^{125887685078020700}]], [0.63, [8.284637183 \times 10^{251775370156041401}, 2.044203438 \\
& \times 10^{251775370156041401}]], [0.64, [4.177372482 \times 10^{503550740312082803}, 1.030751136 \\
& \times 10^{503550740312082803}]], [0.65, [1.062093173 \times 10^{1007101480624165607}, 2.620675435 \\
& \times 10^{1007101480624165606}]], [0.66, [6.865646658 \times 10^{2014202961248331213}, 1.694072799 \\
& \times 10^{2014202961248331213}]], [0.67, [2.868924447 \times 10^{4028405922496662427}, 7.078964461 \\
& \times 10^{4028405922496662426}]], [0.68, [5.009500644 \times 10^{8056811844993324854}, 1.236075668 \\
& \times 10^{8056811844993324854}]], [0.69, [Float(∞), Float(∞)]], [0.70, [Float(∞), Float(∞)]],
\end{aligned}$$



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Float(∞), Float(∞)]], [1.73, [Float(∞), Float(∞)]], [1.74, [Float(∞), Float(∞)]],
[1.75, [Float(∞), Float(∞)]], [1.76, [Float(∞), Float(∞)]], [1.77, [Float(∞),
Float(∞)]], [1.78, [Float(∞), Float(∞)]], [1.79, [Float(∞), Float(∞)]], [1.80, [
Float(∞), Float(∞)]], [1.81, [Float(∞), Float(∞)]], [1.82, [Float(∞), Float(∞)]],
[1.83, [Float(∞), Float(∞)]], [1.84, [Float(∞), Float(∞)]], [1.85, [Float(∞),
Float(∞)]], [1.86, [Float(∞), Float(∞)]], [1.87, [Float(∞), Float(∞)]], [1.88, [
Float(∞), Float(∞)]], [1.89, [Float(∞), Float(∞)]], [1.90, [Float(∞), Float(∞)]],
[1.91, [Float(∞), Float(∞)]], [1.92, [Float(∞), Float(∞)]], [1.93, [Float(∞),
Float(∞)]], [1.94, [Float(∞), Float(∞)]], [1.95, [Float(∞), Float(∞)]], [1.96, [
Float(∞), Float(∞)]], [1.97, [Float(∞), Float(∞)]], [1.98, [Float(∞), Float(∞)]],
[1.99, [Float(∞), Float(∞)]], [2.00, [Float(∞), Float(∞)]], [2.01, [Float(∞),
Float(∞)]]]

```

>

>

>

> #@ { $x = 42, y = -26$ }

>

>  $Dis2(F, x, y, [42 + 0.1, -26 + 0.1], 0.01, 2)$

[ [0.01, [42.1, -25.9]], [0.02, [43.5092, -25.8550]], [0.03, [53.83272256,

$-25.34020857]], [0.04, [179.1385351, -10.13548778]], [0.05, [9751.843230,$

$2087.627912]], [0.06, [5.425584451 \times 10^7, 1.327628801 \times 10^7]], [0.07, [1.784487118$

$\times 10^{15}, 4.400983830 \times 10^{14}]], [0.08, [1.937670889 \times 10^{30}, 4.780991024 \times 10^{29}]], [0.09,$

$[2.285125895 \times 10^{60}, 5.638453443 \times 10^{59}]], [0.10, [3.178162618 \times 10^{120}, 7.841997351$

$\times 10^{119}]], [0.11, [6.147639934 \times 10^{240}, 1.516907298 \times 10^{240}]], [0.12, [2.300239510$

$\times 10^{481}, 5.675755508 \times 10^{480}]], [0.13, [3.220344489 \times 10^{962}, 7.946080346 \times 10^{961}]],$

$[0.14, [6.311911159 \times 10^{1924}, 1.557440623 \times 10^{1924}]], [0.15, [2.424811422 \times 10^{3849},$

$5.983132077 \times 10^{3848}]], [0.16, [3.578591716 \times 10^{7698}, 8.830042073 \times 10^{7697}]], [0.17,$

$[7.794361038 \times 10^{15396}, 1.923229620 \times 10^{15396}]], [0.18, [3.697577209 \times 10^{30793},$

$9.123634356 \times 10^{30792}]], [0.19, [8.321291127 \times 10^{61586}, 2.053247662 \times 10^{61586}]], [0.20,$

$[4.214418376 \times 10^{123173}, 1.039892073 \times 10^{123173}]], [0.21, [1.081014472 \times 10^{246347},$

$2.667363036 \times 10^{246346}]], [0.22, [7.112450062 \times 10^{492693}, 1.754970622 \times 10^{492693}]],$

$[0.23, [3.078893554 \times 10^{985387}, 7.597055428 \times 10^{985386}]], [0.24, [5.769598111$

$\times 10^{1970774}, 1.423626894 \times 10^{1970774}]], [0.25, [2.026036849 \times 10^{3941549}, 4.999170632$

$\times 10^{3941548}]], [0.26, [2.498336274 \times 10^{7883098}, 6.164551920 \times 10^{7883097}]], [0.27,$

$[3.798901225 \times 10^{15766196}, 9.373647600 \times 10^{15766195}]], [0.28, [8.783593272 \times 10^{31532392},$

(64)

$2.167318999 \times 10^{31532392}]], [0.29, [4.695703309 \times 10^{63064785}, 1.158647341$   
 $\times 10^{63064785}]], [0.30, [1.342015438 \times 10^{126129571}, 3.311373222 \times 10^{126129570}]], [0.31,$   
 $[1.096153154 \times 10^{252259142}, 2.704717172 \times 10^{252259141}]], [0.32, [7.313052474$   
 $\times 10^{504518283}, 1.804468522 \times 10^{504518283}]], [0.33, [3.255019491 \times 10^{1009036567},$   
 $8.031639636 \times 10^{1009036566}]], [0.34, [6.448569743 \times 10^{2018073134}, 1.591160619$   
 $\times 10^{2018073134}]], [0.35, [2.530946799 \times 10^{4036146269}, 6.245017174 \times 10^{4036146268}]],$   
 $[0.36, [3.898721803 \times 10^{8072292538}, 9.619951164 \times 10^{8072292537}]], [0.37, [9.251256189$   
 $\times 10^{16144585076}, 2.282713086 \times 10^{16144585076}]], [0.38, [5.209039247 \times 10^{32289170153},$   
 $1.285311077 \times 10^{32289170153}]], [0.39, [1.651472984 \times 10^{64578340307}, 4.074948213$   
 $\times 10^{64578340306}]], [0.40, [1.659965879 \times 10^{129156680614}, 4.095904119 \times 10^{129156680613}]],$   
 $[0.41, [1.677082921 \times 10^{258313361228}, 4.138139785 \times 10^{258313361227}]], [0.42,$   
 $[1.711848342 \times 10^{516626722456}, 4.223922169 \times 10^{516626722455}]], [0.43, [1.783556152$   
 $\times 10^{1033253444912}, 4.400858529 \times 10^{1033253444911}]], [0.44, [1.936108929 \times 10^{2066506889824},$   
 $4.777276835 \times 10^{2066506889823}]], [0.45, [2.281475396 \times 10^{4133013779648}, 5.629455761$   
 $\times 10^{4133013779647}]], [0.46, [3.168019115 \times 10^{8266027559296}, 7.816969439$   
 $\times 10^{8266027559295}]], [0.47, [6.108460936 \times 10^{16532055118592}, 1.507240035$   
 $\times 10^{16532055118592}]], [0.48, [2.271014022 \times 10^{33064110237185}, 5.603642705$   
 $\times 10^{33064110237184}]], [0.49, [3.139032739 \times 10^{66128220474370}, 7.745446636$   
 $\times 10^{66128220474369}]], [0.50, [5.997191336 \times 10^{132256440948740}, 1.479784675$   
 $\times 10^{132256440948740}]], [0.51, [2.189031564 \times 10^{264512881897481}, 5.401354037$   
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 $\times 10^{67715297765755167}]], [0.60, [1.035289099 \times 10^{135430595531510336}, 2.554537379$   
 $\times 10^{135430595531510335}]], [0.61, [6.523482421 \times 10^{270861191063020671}, 1.609645045$   
 $\times 10^{270861191063020671}]], [0.62, [2.590092098 \times 10^{541722382126041343}, 6.390956000$   
 $\times 10^{541722382126041342}]], [0.63, [4.083068143 \times 10^{1083444764252082686}, 1.007481891$



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Float(∞)]], [1.60, [Float(∞), Float(∞)]], [1.61, [Float(∞), Float(∞)]], [1.62, [
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[1.65, [Float(∞), Float(∞)]], [1.66, [Float(∞), Float(∞)]], [1.67, [Float(∞),
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Float(∞)]], [1.92, [Float(∞), Float(∞)]], [1.93, [Float(∞), Float(∞)]], [1.94, [
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Float(∞)]], [2.00, [Float(∞), Float(∞)]], [2.01, [Float(∞), Float(∞)]]]
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#3
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```
> SIRS(s, i, beta, gamma, nu, N)
```

$$[-\beta s i + \gamma (N - s - i), \beta s i - \nu i] \quad (65)$$

```
>
```

```
> EquPts(SIRS(s, i, beta, gamma, nu, N), {s, i})
```

$$\left\{ \{0, N\}, \left\{ \frac{\nu}{\beta}, \frac{\gamma(N\beta - \nu)}{\beta(\gamma + \nu)} \right\} \right\} \quad (66)$$

```

> #4
>
> Chemostat := proc(N, C, a1, a2) :  $\left[ a1 \cdot \left( \frac{C}{1 + C} \right) \cdot N - N, - \left( \frac{C}{1 + C} \right) \cdot N - C + a2 \right]$  :end:
>
> EquPts(Chemostat(N, C, a1, a2), {N, C})
       $\left\{ \{0, a2\}, \left\{ \frac{1}{a1 - 1}, \frac{a1 (a2 a1 - a2 - 1)}{a1 - 1} \right\} \right\}$  (67)
>
> #5
>
> #(i)
>
> Orb3 := proc(F, x, y, z, pt0, K1, K2) local pt, L, i :
  pt := pt0 :
  for i from 1 to K1 - 1 do
    pt := subs({x = pt[1], y = pt[2], z = pt[3]}, F) :
  od:
  L := []:
  for i from K1 to K2 do
    L := [op(L), pt] :
    pt := normal(subs({x = pt[1], y = pt[2], z = pt[3]}, F)) :
  od:

```

```

L:
end:
>
>
> Dis3 :=proc(F, x, y, z, pt, h, A) local L, i :
  L := Orb3( [x + h * F[1], y + h * F[2], z + h * F[3]], x, y, z, pt, 0, trunc(A/h)) :
  L := [seq([i * h, [L[i][1], L[i][2], L[i][3]]], i = 1 .. nops(L))]:
end:
>
>
> Dis3([x + y + z, x + y + z, x + y + z], x, y, z, [1, 2, 3], 1, 3)
  [[1, [1, 2, 3]], [2, [7, 8, 9]], [3, [31, 32, 33]], [4, [127, 128, 129]]] (68)
>
>
>
>
> #(ii)
>
> RandNice([x, y, z], 10)
[(1 - 6x - 7y - 7z) (3 - 3x - 5y - 3z), (8 - 10x - 3y - z) (1 - 3x - 5y - 5z),
 (10 - 10x - 10y - 2z) (8 - 4x - 2y - 9z)] (69)
> F := [(1 - 6x - 7y - 7z) (3 - 3x - 5y - 3z), (8 - 10x - 3y - z) (1 - 3x - 5y
 - 5z), (10 - 10x - 10y - 2z) (8 - 4x - 2y - 9z)]
F := [(1 - 6x - 7y - 7z) (3 - 3x - 5y - 3z), (8 - 10x - 3y - z) (1 - 3x - 5y
 - 5z), (10 - 10x - 10y - 2z) (8 - 4x - 2y - 9z)] (70)
>
>
> sys := {(1 - 6·x - 7·y - 7·z)·(3 - 3·x - 5·y - 3·z) = 0, (8 - 10·x - 3·y - z)·(1 - 3
 ·x - 5·y - 5·z) = 0, (10 - 10·x - 10·y - 2·z)·(8 - 4·x - 2·y - 9·z) = 0}
sys := {(1 - 6x - 7y - 7z) (3 - 3x - 5y - 3z) = 0, (8 - 10x - 3y - z) (1 - 3x - 5y
 - 5z) = 0, (10 - 10x - 10y - 2z) (8 - 4x - 2y - 9z) = 0} (71)
> solve(sys, {x, y, z})
{ x = 0, y =  $\frac{6}{5}$ , z = -1 }, { x = - $\frac{2}{9}$ , y =  $\frac{13}{9}$ , z = - $\frac{10}{9}$  }, { x = - $\frac{2}{9}$ , y = - $\frac{53}{63}$ , z =  $\frac{74}{63}$  }, { x =  $\frac{73}{14}$ , y = - $\frac{27}{14}$ , z = -1 }, { x =  $\frac{27}{37}$ , y =  $\frac{12}{37}$ , z = - $\frac{10}{37}$  }, { x =  $\frac{76}{99}$ , y =  $\frac{83}{198}$ , z = - $\frac{185}{198}$  },
{ x =  $\frac{269}{331}$ , y = - $\frac{78}{331}$ , z =  $\frac{192}{331}$  }, { x =  $\frac{479}{396}$ , y = - $\frac{317}{198}$ , z =  $\frac{70}{99}$  } (72)
> #These are the equilibrium points.

```

```

> J := Matrix([ [diff(F[1],x), diff(F[1],y)], [diff(F[2],x), diff(F[2],y)]])
      J := 
$$\begin{bmatrix} -21 + 36x + 51y + 39z & -26 + 51x + 70y + 56z \\ -34 + 60x + 59y + 53z & -43 + 59x + 30y + 20z \end{bmatrix} \quad (73)$$

> #I'm just gonna test two of the equilibrium points.
>
> # {x=0, y=  $\frac{6}{5}$ , z= -1}
>
> J := subs(x=0, J)
      J := 
$$\begin{bmatrix} -21 + 51y + 39z & -26 + 70y + 56z \\ -34 + 59y + 53z & -43 + 30y + 20z \end{bmatrix} \quad (74)$$

> J := subs(y=  $\frac{6}{5}$ , J)
      J := 
$$\begin{bmatrix} \frac{201}{5} + 39z & 58 + 56z \\ \frac{184}{5} + 53z & -7 + 20z \end{bmatrix} \quad (75)$$

> J := subs(z= -1, J)
      J := 
$$\begin{bmatrix} \frac{6}{5} & 2 \\ -\frac{81}{5} & -27 \end{bmatrix} \quad (76)$$

> evalf(Eigenvalues(J))
      [ 0.          ]
      [ -25.80000000 ] \quad (77)
> #This point is not stable.
>
> Dis3(F, x, y, z, [0.1,  $\frac{6}{5} + 0.1$ , -0.9], 0.01, 2)
[[0.01, [0.1, 1.30000000, -0.9]], [0.02, [0.1264000000, 1.248000000, -1.188200000]],
 [0.03, [0.1264966420, 1.261451884, -1.402806527]], [0.04, [0.1329158081,
 1.319234956, -1.591769036]], [0.05, [0.1493838314, 1.403779996, -1.848067653]],
 [0.06, [0.1840003630, 1.518674199, -2.237699294]], [0.07, [0.2612762874,
 1.673997820, -2.859359078]], [0.08, [0.4486684040, 1.872084439, -3.925622500]], \quad (78)

```

$[0.09, [0.9649123895, 2.052925519, -5.949856279]], [0.10, [2.694365534, 1.726097098, -10.38583121]], [0.11, [10.62296271, -3.248515941, -22.10512834]], [0.12, [72.22459243, -66.90548732, -55.49912306]], [0.13, [1291.985795, -1882.305414, 183.4566274]], [0.14, [207854.6734, -345945.1677, -168780.8361]], [0.15, [3.799015461 \times 10^{10}, -1.700341682 \times 10^{10}, 2.370633929 \times 10^{10}]], [0.16, [2.750603780 \times 10^{20}, 5.200288902 \times 10^{20}, 8.523967122 \times 10^{20}]], [0.17, [6.734722239 \times 10^{41}, 3.969024717 \times 10^{41}, 9.474033396 \times 10^{41}]], [0.18, [9.210068946 \times 10^{83}, 7.756582449 \times 10^{83}, 1.513631041 \times 10^{84}]], [0.19, [2.409884428 \times 10^{168}, 1.854431332 \times 10^{168}, 3.770456891 \times 10^{168}]], [0.20, [1.497281530 \times 10^{337}, 1.181979126 \times 10^{337}, 2.372828977 \times 10^{337}]], [0.21, [5.933635931 \times 10^{674}, 4.651695568 \times 10^{674}, 9.369559555 \times 10^{674}]], [0.22, [9.251270196 \times 10^{1349}, 7.266496177 \times 10^{1349}, 1.462266281 \times 10^{1350}]], [0.23, [2.253348405 \times 10^{2700}, 1.768981101 \times 10^{2700}, 3.560702257 \times 10^{2700}]], [0.24, [1.336115244 \times 10^{5401}, 1.049063445 \times 10^{5401}, 2.111463578 \times 10^{5401}]], [0.25, [4.698298715 \times 10^{10802}, 3.688766272 \times 10^{10802}, 7.424571518 \times 10^{10802}]], [0.26, [5.809195640 \times 10^{21605}, 4.561012695 \times 10^{21605}, 9.180138253 \times 10^{21605}]], [0.27, [8.881201399 \times 10^{43211}, 6.972936107 \times 10^{43211}, 1.403473651 \times 10^{43212}]], [0.28, [2.075782209 \times 10^{86424}, 1.629769227 \times 10^{86424}, 3.280307189 \times 10^{86424}]], [0.29, [1.133971904 \times 10^{172849}, 8.903208067 \times 10^{172848}, 1.791987491 \times 10^{172849}]], [0.30, [3.384100164 \times 10^{345698}, 2.656974980 \times 10^{345698}, 5.347809180 \times 10^{345698}]], [0.31, [3.013873824 \times 10^{691397}, 2.366297337 \times 10^{691397}, 4.762749677 \times 10^{691397}]], [0.32, [2.390500143 \times 10^{1382795}, 1.876864952 \times 10^{1382795}, 3.777647797 \times 10^{1382795}]], [0.33, [1.503890414 \times 10^{2765591}, 1.180756761 \times 10^{2765591}, 2.376560537 \times 10^{2765591}]], [0.34, [5.952111040 \times 10^{5531182}, 4.673209756 \times 10^{5531182}, 9.405972721 \times 10^{5531182}]], [0.35, [9.323536852 \times 10^{11062365}, 7.320233625 \times 10^{11062365}, 1.473375291 \times 10^{11062366}]], [0.36, [2.287705026 \times 10^{22124732}, 1.796156921 \times 10^{22124732}, 3.615203233 \times 10^{22124732}]], [0.37, [1.377332182 \times 10^{44249465}, 1.081391483 \times 10^{44249465}, 2.176563718 \times 10^{44249465}]], [0.38, [4.992476539 \times 10^{88498930}, 3.919767274 \times 10^{88498930}, 7.889486238 \times 10^{88498930}]], [0.39, [6.559499566 \times 10^{176997861}, 5.150091652 \times 10^{176997861}, 1.036581368 \times 10^{176997862}]], [0.40, [1.132348367 \times 10^{353995724}, 8.890461555 \times 10^{353995723}, 1.789421903 \times 10^{353995724}]], [0.41, [3.374417070 \times 10^{707991448}, 2.649372409 \times 10^{707991448}, 5.332507190 \times 10^{707991448}]], [0.42, [2.996650962 \times 10^{1415982897}, 2.352775078 \times 10^{1415982897}, 4.735532827 \times 10^{1415982897}]], [0.43, [2.363257065 \times 10^{2831965795},$

$$\begin{aligned}
& 1.855475460 \times 10^{2831965795}, 3.734596236 \times 10^{2831965795}], [0.44, [1.469807883 \\
& \times 10^{5663931591}, 1.153997379 \times 10^{5663931591}, 2.322700763 \times 10^{5663931591}]], [0.45, \\
& [5.685383791 \times 10^{11327863182}, 4.463792902 \times 10^{11327863182}, 8.984470305 \times 10^{11327863182}]], \\
& [0.46, [8.506643193 \times 10^{22655726365}, 6.678861950 \times 10^{22655726365}, 1.344283621 \\
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& 3.009454396 \times 10^{45311452732}]], [0.48, [9.544403584 \times 10^{90622905464}, 7.493643790 \\
& \times 10^{90622905464}, 1.508278309 \times 10^{90622905465}]], [0.49, [2.397376438 \times 10^{181245810930}, \\
& 1.882263770 \times 10^{181245810930}, 3.788514231 \times 10^{181245810930}]], [0.50, [1.512554764 \\
& \times 10^{362491621861}, 1.187559445 \times 10^{362491621861}, 2.390252595 \times 10^{362491621861}]], [0.51, \\
& [6.020892294 \times 10^{724983243722}, 4.727212320 \times 10^{724983243722}, 9.514666031 \\
& \times 10^{724983243722}]], [0.52, [9.540263271 \times 10^{1449966487445}, 7.490393088 \times 10^{1449966487445}, \\
& 1.507624026 \times 10^{1449966487446}]], [0.53, [2.395296949 \times 10^{2899932974892}, 1.880631093 \\
& \times 10^{2899932974892}, 3.785228070 \times 10^{2899932974892}]], [0.54, [1.509931919 \times 10^{5799865949785}, \\
& 1.185500157 \times 10^{5799865949785}, 2.386107777 \times 10^{5799865949785}]], [0.55, [6.000029341 \\
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& \times 10^{23199463799142}]], [0.57, [2.362269398 \times 10^{46398927598284}, 1.854700010 \\
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& \times 10^{92797855196569}, 1.153033009 \times 10^{92797855196569}, 2.320759736 \times 10^{92797855196569}]], \\
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& \times 10^{185595710393138}]], [0.60, [8.478243596 \times 10^{371191420786277}, 6.656564437 \\
& \times 10^{371191420786277}, 1.339795704 \times 10^{371191420786278}]], [0.61, [1.891691984 \\
& \times 10^{742382841572556}, 1.485233286 \times 10^{742382841572556}, 2.989393693 \times 10^{742382841572556}]], \\
& [0.62, [9.417583719 \times 10^{1484765683145112}, 7.394073097 \times 10^{1484765683145112}, 1.488237283 \\
& \times 10^{1484765683145113}]], [0.63, [2.334090128 \times 10^{2969531366290226}, 1.832575483 \\
& \times 10^{2969531366290226}, 3.688504458 \times 10^{2969531366290226}]], [0.64, [1.433751505 \\
& \times 10^{5939062732580453}, 1.125688260 \times 10^{5939062732580453}, 2.265721768 \times 10^{5939062732580453}]], \\
& [0.65, [5.409864857 \times 10^{11878125465160906}, 4.247473386 \times 10^{11878125465160906}, 8.549074595 \\
& \times 10^{11878125465160906}]], [0.66, [7.702141178 \times 10^{23756250930321813}, 6.047219392 \\
& \times 10^{23756250930321813}, 1.217150174 \times 10^{23756250930321814}]], [0.67, [1.561210964 \\
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& \times 10^{47512501860643628}]], [0.68, [6.414485497 \times 10^{95025003721287256}, 5.036236055
\end{aligned}$$

$$\begin{aligned}
& \times 10^{95025003721287256}, 1.013665156 \times 10^{95025003721287257}], [0.69, [1.082835033 \\
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\text{Float}(\infty), \text{Float}(\infty)]], [0.96, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.97, [\text{Float}(\infty), \\
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\text{Float}(\infty), \text{Float}(\infty)]], [1.00, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.01, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.02, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.03, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.04, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.05, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.06, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.07, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.08, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.09, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.10, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.11, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.12, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.13, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.14, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.15, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.16, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.17, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.18, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.19, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.20, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.21, [\text{Float}(\infty), \\
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\text{Float}(\infty), \text{Float}(\infty)]], [1.24, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.25, [\text{Float}(\infty), \\
\text{Float}(\infty), \text{Float}(\infty)]], [1.26, [\text{Float}(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.27, [\text{Float}(\infty),
\end{aligned}$$



>  $\# \left\{ x = -\frac{2}{9}, y = \frac{13}{9}, z = -\frac{10}{9} \right\}$

>  $J := \text{Matrix}([ [ \text{diff}(F[1], x), \text{diff}(F[1], y) ], [ \text{diff}(F[2], x), \text{diff}(F[2], y) ] ])$

$$J := \begin{bmatrix} -21 + 36x + 51y + 39z & -26 + 51x + 70y + 56z \\ -34 + 60x + 59y + 53z & -43 + 59x + 30y + 20z \end{bmatrix} \quad (79)$$

>  $J := \text{subs}\left(x = -\frac{2}{9}, J\right)$

$$J := \begin{bmatrix} -29 + 51y + 39z & -\frac{112}{3} + 70y + 56z \\ -\frac{142}{3} + 59y + 53z & -\frac{505}{9} + 30y + 20z \end{bmatrix} \quad (80)$$

>  $J := \text{subs}\left(y = \frac{13}{9}, J\right)$

$$J := \begin{bmatrix} \frac{134}{3} + 39z & \frac{574}{9} + 56z \\ \frac{341}{9} + 53z & -\frac{115}{9} + 20z \end{bmatrix} \quad (81)$$

>  $J := \text{subs}\left(z = -\frac{10}{9}, J\right)$

$$J := \begin{bmatrix} \frac{4}{3} & \frac{14}{9} \\ -21 & -35 \end{bmatrix} \quad (82)$$

>  $\text{evalf}(\text{Eigenvalues}(J))$

$$\begin{bmatrix} 0.41082832 \\ -34.07749498 \end{bmatrix} \quad (83)$$

> #This point is not stable.

>  
>  
>

$$\begin{aligned}
 & \text{Dis3}\left(F, x, y, z, \left[-\frac{2}{9} + 0.1, \frac{13}{9} + 0.1, -\frac{10}{9} + 0.1\right], 0.01, 2\right) \\
 & [[0.01, [-0.1222222222, 1.5444444444, -1.0111111111]], [0.02, [-0.09577777780, \\
 & 1.4716444444, -1.3301111111]], [0.03, [-0.09624816853, 1.505688010, \\
 & -1.521359319]], [0.04, [-0.09077522683, 1.587259881, -1.721871012]], [0.05, \\
 & [-0.07829981197, 1.701411816, -2.036517874]], [0.06, [-0.04634869906, \\
 & 1.867751040, -2.538035870]], [0.07, [0.03809210819, 2.110158737, -3.394452404]], \\
 & [0.08, [0.2839147898, 2.452358566, -4.998603425]], [0.09, [1.119770940, \\
 & 2.813290513, -8.456501266]], [0.10, [4.816987072, 1.990766982, -17.64588763]], \\
 & [0.11, [30.57426939, -16.48184714, -50.35793123]], [0.12, [443.7674688, \\
 & -498.4165112, -162.6991964]], [0.13, [32923.07248, -55247.65780, 5958.102304]], \\
 & [0.14, [2.354227942 \times 10^8, -2.502803247 \times 10^8, -1.581012380 \times 10^8]], [0.15, \\
 & [1.474242648 \times 10^{16}, -1.930380626 \times 10^{16}, 4.563098132 \times 10^{15}]], [0.16, [5.686295622 \\
 & \times 10^{30}, -2.773007102 \times 10^{31}, -2.241432508 \times 10^{31}]], [0.17, [5.984031308 \times 10^{62}, \\
 & 1.138910882 \times 10^{62}, 6.219008641 \times 10^{62}]], [0.18, [3.697748282 \times 10^{125}, 3.803236737 \\
 & \times 10^{125}, 6.876210561 \times 10^{125}]], [0.19, [4.918680530 \times 10^{251}, 3.563963497 \times 10^{251}, \\
 & 7.481182614 \times 10^{251}]], [0.20, [5.877619033 \times 10^{503}, 4.713963662 \times 10^{503}, 9.393448830 \\
 & \times 10^{503}]], [0.21, [9.298546187 \times 10^{1007}, 7.257400992 \times 10^{1007}, 1.465000663 \times 10^{1008}]], \\
 & [0.22, [2.261520373 \times 10^{2016}, 1.778484267 \times 10^{2016}, 3.576822127 \times 10^{2016}]], [0.23, \\
 & [1.348265758 \times 10^{4033}, 1.058096646 \times 10^{4033}, 2.130141379 \times 10^{4033}]], [0.24, \\
 & [4.781756010 \times 10^{8066}, 3.754785220 \times 10^{8066}, 7.556968091 \times 10^{8066}]], [0.25, \\
 & [6.018234640 \times 10^{16133}, 4.724965726 \times 10^{16133}, 9.510300733 \times 10^{16133}]], [0.26, \\
 & [9.531506947 \times 10^{32267}, 7.483587883 \times 10^{32267}, 1.506247498 \times 10^{32268}]], [0.27, \\
 & [2.390925209 \times 10^{64536}, 1.877193875 \times 10^{64536}, 3.778314541 \times 10^{64536}]], [0.28, \\
 & [1.504421275 \times 10^{129073}, 1.181174391 \times 10^{129073}, 2.377400306 \times 10^{129073}]], [0.29, \\
 & [5.956318248 \times 10^{258146}, 4.676512075 \times 10^{258146}, 9.412620328 \times 10^{258146}]], [0.30, \\
 & [9.336720176 \times 10^{516293}, 7.330584705 \times 10^{516293}, 1.475458659 \times 10^{516294}]], [0.31, \\
 & [2.294179279 \times 10^{1032588}, 1.801240058 \times 10^{1032588}, 3.625434307 \times 10^{1032588}]], [0.32, \\
 & [1.385138951 \times 10^{2065177}, 1.087520854 \times 10^{2065177}, 2.188900564 \times 10^{2065177}]], [0.33, \\
 & [5.049232028 \times 10^{4130354}, 3.964327980 \times 10^{4130354}, 7.979175520 \times 10^{4130354}]], [0.34, \\
 & [6.709486736 \times 10^{8260709}, 5.267851804 \times 10^{8260709}, 1.060283466 \times 10^{8260710}]], [0.35,
 \end{aligned} \tag{84}$$

$$\begin{aligned}
& [1.184724146 \times 10^{16521420}, 9.301682043 \times 10^{16521419}, 1.872190039 \times 10^{16521420}], [0.36, \\
& [3.693797836 \times 10^{33042840}, 2.900129377 \times 10^{33042840}, 5.837216652 \times 10^{33042840}], [0.37, \\
& [3.590747671 \times 10^{66085681}, 2.819221102 \times 10^{66085681}, 5.674369046 \times 10^{66085681}], [0.38, \\
& [3.393191867 \times 10^{132171363}, 2.664113158 \times 10^{132171363}, 5.362176533 \times 10^{132171363}], \\
& [0.39, [3.030089645 \times 10^{264342727}, 2.379028952 \times 10^{264342727}, 4.788375144 \\
& \times 10^{264342727}]], [0.40, [2.416293008 \times 10^{528685455}, 1.897115827 \times 10^{528685455}, \\
& 3.818407616 \times 10^{528685455}]], [0.41, [1.536518653 \times 10^{1057370911}, 1.206374329 \\
& \times 10^{1057370911}, 2.428122131 \times 10^{1057370911}]], [0.42, [6.213185446 \times 10^{2114741822}, \\
& 4.878188371 \times 10^{2114741822}, 9.818542104 \times 10^{2114741822}]], [0.43, [1.015938165 \\
& \times 10^{4229483646}, 7.976484496 \times 10^{4229483645}, 1.605461761 \times 10^{4229483646}]], [0.44, \\
& [2.716271605 \times 10^{8458967292}, 2.132639475 \times 10^{8458967292}, 4.292456315 \times 10^{8458967292}]], \\
& [0.45, [1.941712962 \times 10^{16917934585}, 1.524506499 \times 10^{16917934585}, 3.068440599 \\
& \times 10^{16917934585}]], [0.46, [9.922216577 \times 10^{33835869170}, 7.790277939 \times 10^{33835869170}, \\
& 1.567983155 \times 10^{33835869171}]], [0.47, [2.590932193 \times 10^{67671738342}, 2.034231138 \\
& \times 10^{67671738342}, 4.094385570 \times 10^{67671738342}]], [0.48, [1.766650895 \times 10^{135343476685}, \\
& 1.387059169 \times 10^{135343476685}, 2.791794376 \times 10^{135343476685}]], [0.49, [8.213724233 \\
& \times 10^{270686953370}, 6.448881075 \times 10^{270686953370}, 1.297994368 \times 10^{270686953371}]], [0.50, \\
& [1.775492648 \times 10^{541373906742}, 1.394001139 \times 10^{541373906742}, 2.805766779 \\
& \times 10^{541373906742}]], [0.51, [8.296146249 \times 10^{1082747813484}, 6.513593469 \times 10^{1082747813484}, \\
& 1.311019314 \times 10^{1082747813485}]], [0.52, [1.811304398 \times 10^{2165495626970}, 1.422118190 \\
& \times 10^{2165495626970}, 2.862359194 \times 10^{2165495626970}]], [0.53, [8.634188493 \times 10^{4330991253940}, \\
& 6.779002212 \times 10^{4330991253940}, 1.364439288 \times 10^{4330991253941}]], [0.54, [1.961921804 \\
& \times 10^{8661982507882}, 1.540373164 \times 10^{8661982507882}, 3.100376127 \times 10^{8661982507882}]], [0.55, \\
& [1.012982704 \times 10^{17323965015765}, 7.953280145 \times 10^{17323965015764}, 1.600791319 \\
& \times 10^{17323965015765}]], [0.56, [2.700490804 \times 10^{34647930031530}, 2.120249419 \\
& \times 10^{34647930031530}, 4.267518311 \times 10^{34647930031530}]], [0.57, [1.919216851 \\
& \times 10^{69295860063061}, 1.506844018 \times 10^{69295860063061}, 3.032890555 \times 10^{69295860063061}]], \\
& [0.58, [9.693636695 \times 10^{138591720126122}, 7.610811910 \times 10^{138591720126122}, 1.531861247 \\
& \times 10^{138591720126123}]], [0.59, [2.472931693 \times 10^{277183440252246}, 1.941584833 \\
& \times 10^{277183440252246}, 3.907912317 \times 10^{277183440252246}]], [0.60, [1.609395874 \\
& \times 10^{554366880504493}, 1.263592774 \times 10^{554366880504493}, 2.543288186 \times 10^{554366880504493}]], \\
& [0.61, [6.816546625 \times 10^{1108733761008986}, 5.351908253 \times 10^{1108733761008986}, 1.077201873
\end{aligned}$$

$$\begin{aligned}
& \times 10^{1108733761008987}], [0.62, [1.222833877 \times 10^{2217467522017974}, 9.600894819 \\
& \times 10^{2217467522017973}, 1.932413898 \times 10^{2217467522017974}]], [0.63, [3.935261227 \\
& \times 10^{4434935044035948}, 3.089710697 \times 10^{4434935044035948}, 6.218795228 \times 10^{4434935044035948}]], \\
& [0.64, [4.075545774 \times 10^{8869870088071897}, 3.199852986 \times 10^{8869870088071897}, 6.440483408 \\
& \times 10^{8869870088071897}]], [0.65, [4.371295776 \times 10^{17739740176143795}, 3.432056615 \\
& \times 10^{17739740176143795}, 6.907849763 \times 10^{17739740176143795}]], [0.66, [5.028738230 \\
& \times 10^{35479480352287591}, 3.948237592 \times 10^{35479480352287591}, 7.946789687 \\
& \times 10^{35479480352287591}]], [0.67, [6.655132411 \times 10^{70958960704575183}, 5.225176331 \\
& \times 10^{70958960704575183}, 1.051693988 \times 10^{70958960704575184}]], [0.68, [1.165606725 \\
& \times 10^{141917921409150368}, 9.151584503 \times 10^{141917921409150367}, 1.841979254 \\
& \times 10^{141917921409150368}]], [0.69, [3.575548975 \times 10^{283835842818300736}, 2.807288077 \\
& \times 10^{283835842818300736}, 5.650350927 \times 10^{283835842818300736}]], [0.70, [3.364527672 \\
& \times 10^{567671685636601473}, 2.641607900 \times 10^{567671685636601473}, 5.316879222 \\
& \times 10^{567671685636601473}]], [0.71, [2.979112144 \times 10^{1135343371273202947}, 2.339004740 \\
& \times 10^{1135343371273202947}, 4.707816668 \times 10^{1135343371273202947}]], [0.72, [2.335674644 \\
& \times 10^{2270686742546405895}, 1.833819541 \times 10^{2270686742546405895}, 3.691008426 \\
& \times 10^{2270686742546405895}]], [0.73, [1.435698792 \times 10^{4541373485092811791}, 1.127217143 \\
& \times 10^{4541373485092811791}, 2.268799017 \times 10^{4541373485092811791}]], [0.74, [5.424569932 \\
& \times 10^{9082746970185623582}, 4.259018853 \times 10^{9082746970185623582}, 8.572312658 \\
& \times 10^{9082746970185623582}]], [0.75, [Float(\infty), Float(\infty), Float(\infty)]], [0.76, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.77, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.78, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.79, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.80, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.81, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.82, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.83, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.84, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.85, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.86, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.87, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.88, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.89, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.90, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.91, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.92, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.93, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.94, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.95, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.96, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.97, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [0.98, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [0.99, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.00, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [1.01, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.02, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]], [1.03, [Float(\infty), \text{Float}(\infty), \text{Float}(\infty)]], [1.04, [Float(\infty), \\
& \text{Float}(\infty), \text{Float}(\infty)]]
\end{aligned}$$



```
Float(∞), Float(∞)]], [1.81, [Float(∞), Float(∞), Float(∞)]], [1.82, [Float(∞),  
Float(∞), Float(∞)]], [1.83, [Float(∞), Float(∞), Float(∞)]], [1.84, [Float(∞),  
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Float(∞), Float(∞)]], [1.99, [Float(∞), Float(∞), Float(∞)]], [2.00, [Float(∞),  
Float(∞), Float(∞)]], [2.01, [Float(∞), Float(∞), Float(∞)]]]
```

