

Charles Griebell

Homework 19

OK to post

PREAMBLE:

```
> read `C:/Users/cgrie/Dynam Models Bio/Homeworks/HW19/M19.txt`;
Help19();
SIRSDemo(N,IN,gamma,nu,h,A),e.g. SIRSDemo(100,20,1, 1,0.01, 10); EquPts(F,var), StEquPts(F,
var), IsStable(M), RandNice(var,K) (1)
```

#Problem 1

Carefully read the Maple code for procedure

```
SIRSDemo(N,IN, gamma,nu,h,A)
```

and run it for the following parameter values (with h=0.01)

Population = 1000 people

Initial infected people = 200 people

No dead people (or removed people) at t=0 (the start)

```
> SIRSDemo(1000,200,gamma,nu,0.01,A);
```

*This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, A*

*with population size, 1000, and fixed parameters nu=, v, and gamma=, γ*

*where we change beta from 0.2\*nu/N to 4\*nu/N*

*Recall that the epidemic will persist if beta exceeds nu/N, that in this case is,  $\frac{v}{1000}$*

*We start with , 200, infected individuals, 0 removed and hence, 800, susceptible*

*We will show what happens once time is close to, A*

*beta is,  $\frac{1}{10}$ , times the threshold value*

```
Error, (in Orb2) final value in for loop must be numeric or character
[C:/Users/cgrie/Dynam Models Bio/Homeworks/HW19/M19.txt:198]
```

```
> #at time t=10 (In SIRSDemo, let A=10),
#SIRSDemo(1000,200,gamma,nu,0.01,10);
```

```
#Let nu =1, gamma = 3
```

**SIRSdemo(1000,200,3,1,0.01,10);**

This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, 10  
with population size, 1000, and fixed parameters nu=, 1, and gamma=, 3  
where we change beta from 0.2\*nu/N to 4\*nu/N

Recall that the epidemic will persist if beta exceeds nu/N, that in this case is,  $\frac{1}{1000}$

We start with , 200, infected individuals, 0 removed and hence, 800, susceptible

We will show what happens once time is close to, 10

beta is,  $\frac{1}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [998.9666995, 0.9909989667]], [9.99, [998.9666995, 0.9909989667]], [10.00, [998.9666995, 0.9909989667]], [10.01, [998.9666995, 0.9909989667]]]

beta is,  $\frac{3}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [996.7009881, 2.978970309]], [9.99, [996.7009881, 2.978970309]], [10.00, [996.7009881, 2.978970309]], [10.01, [996.7009881, 2.978970309]]]

beta is,  $\frac{1}{2}$ , times the threshold value

the long-term behavior is

[[9.98, [994.1715221, 4.974854288]], [9.99, [994.1715221, 4.974854288]], [10.00, [994.1715221, 4.974854288]], [10.01, [994.1715221, 4.974854288]]]

beta is,  $\frac{7}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [991.3807432, 6.978577656]], [9.99, [991.3807432, 6.978577656]], [10.00, [991.3807432, 6.978577656]], [10.01, [991.3807432, 6.978577656]]]

beta is,  $\frac{9}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [988.3315033, 8.990054852]], [9.99, [988.3315033, 8.990054852]], [10.00, [988.3315033, 8.990054852]], [10.01, [988.3315033, 8.990054852]]]

beta is,  $\frac{11}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [985.0270559, 11.00918827]], [9.99, [985.0270559, 11.00918827]], [10.00, [985.0270559, 11.00918827]], [10.01, [985.0270559, 11.00918827]]]

*beta is,  $\frac{13}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [981.4710448, 13.03586861]], [9.99, [981.4710448, 13.03586861]], [10.00, [981.4710448, 13.03586861]], [10.01, [981.4710448, 13.03586861]]]$

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [977.6674922, 15.06997519]], [9.99, [977.6674922, 15.06997519]], [10.00, [977.6674922, 15.06997519]], [10.01, [977.6674922, 15.06997519]]]$

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [973.6207848, 17.11137641]], [9.99, [973.6207848, 17.11137641]], [10.00, [973.6207848, 17.11137641]], [10.01, [973.6207848, 17.11137641]]]$

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [969.3356593, 19.15993017]], [9.99, [969.3356593, 19.15993017]], [10.00, [969.3356593, 19.15993017]], [10.01, [969.3356593, 19.15993017]]]$

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [964.8171858, 21.21548438]], [9.99, [964.8171858, 21.21548438]], [10.00, [964.8171858, 21.21548438]], [10.01, [964.8171858, 21.21548438]]]$

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [960.0707508, 23.27787743]], [9.99, [960.0707508, 23.27787743]], [10.00, [960.0707508, 23.27787743]], [10.01, [960.0707508, 23.27787743]]]$

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [955.1020392, 25.34693877]], [9.99, [955.1020392, 25.34693877]], [10.00, [955.1020392, 25.34693877]], [10.01, [955.1020392, 25.34693877]]]$

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [949.9170149, 27.42248950]], [9.99, [949.9170149, 27.42248950]], [10.00,$

$[949.9170149, 27.42248950]], [10.01, [949.9170149, 27.42248950]]]$   
*beta is,  $\frac{29}{10}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [944.5219011, 29.50434292]], [9.99, [944.5219011, 29.50434292]], [10.00,$   
 $[944.5219011, 29.50434292]], [10.01, [944.5219011, 29.50434292]]]$   
*beta is,  $\frac{31}{10}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [938.9231598, 31.59230516]], [9.99, [938.9231598, 31.59230516]], [10.00,$   
 $[938.9231598, 31.59230516]], [10.01, [938.9231598, 31.59230516]]]$   
*beta is,  $\frac{33}{10}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [933.1274712, 33.68617582]], [9.99, [933.1274712, 33.68617582]], [10.00,$   
 $[933.1274712, 33.68617582]], [10.01, [933.1274712, 33.68617582]]]$   
*beta is,  $\frac{7}{2}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [927.1417118, 35.78574860]], [9.99, [927.1417118, 35.78574860]], [10.00,$   
 $[927.1417118, 35.78574860]], [10.01, [927.1417118, 35.78574860]]]$   
*beta is,  $\frac{37}{10}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [920.9729335, 37.89081195]], [9.99, [920.9729335, 37.89081195]], [10.00,$   
 $[920.9729335, 37.89081195]], [10.01, [920.9729335, 37.89081195]]]$   
*beta is,  $\frac{39}{10}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [914.6283415, 40.00114971]], [9.99, [914.6283415, 40.00114971]], [10.00,$   
 $[914.6283415, 40.00114971]], [10.01, [914.6283415, 40.00114971]]]$  (2)  
 1000 - (914.6283415 + 40.00114971) people have died  

```
> #LET nu=2, gamma =3
SIRSDemo(1000,200,3,2,0.01,10);
```

This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, 10  
 with population size, 1000, and fixed parameters nu=, 2, and gamma=, 3  
 where we change beta from 0.2\*nu/N to 4\*nu/N

Recall that the epidemic will persist if beta exceeds nu/N, that in this case is,  $\frac{1}{500}$

We start with 200, infected individuals, 0 removed and hence, 800, susceptible

We will show what happens once time is close to, 10

beta is,  $\frac{1}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [998.9334028, 0.9819978668]], [9.99, [998.9334028, 0.9819978668]], [10.00, [998.9334028, 0.9819978668]], [10.01, [998.9334028, 0.9819978668]]]

beta is,  $\frac{3}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [996.4021571, 2.957935239]], [9.99, [996.4021571, 2.957935239]], [10.00, [996.4021571, 2.957935239]], [10.01, [996.4021571, 2.957935239]]]

beta is,  $\frac{1}{2}$ , times the threshold value

the long-term behavior is

[[9.98, [993.3444243, 4.949667221]], [9.99, [993.3444243, 4.949667221]], [10.00, [993.3444243, 4.949667221]], [10.01, [993.3444243, 4.949667221]]]

beta is,  $\frac{7}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [989.7667603, 6.956997143]], [9.99, [989.7667603, 6.956997143]], [10.00, [989.7667603, 6.956997143]], [10.01, [989.7667603, 6.956997143]]]

beta is,  $\frac{9}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [985.6773407, 8.979679729]], [9.99, [985.6773407, 8.979679729]], [10.00, [985.6773407, 8.979679729]], [10.01, [985.6773407, 8.979679729]]]

beta is,  $\frac{11}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [981.0859054, 11.01742279]], [9.99, [981.0859054, 11.01742279]], [10.00, [981.0859054, 11.01742279]], [10.01, [981.0859054, 11.01742279]]]

beta is,  $\frac{13}{10}$ , times the threshold value

the long-term behavior is

[[9.98, [976.0036901, 13.06988925]], [9.99, [976.0036901, 13.06988925]], [10.00, [976.0036901, 13.06988925]], [10.01, [976.0036901, 13.06988925]]]

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [970.4433482, 15.13669951]], [9.99, [970.4433482, 15.13669951]], [10.00, [970.4433482, 15.13669951]], [10.01, [970.4433482, 15.13669951]]]$

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [964.4188616, 17.21743410]], [9.99, [964.4188616, 17.21743410]], [10.00, [964.4188616, 17.21743410]], [10.01, [964.4188616, 17.21743410]]]$

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [957.9454447, 19.31163661]], [9.99, [957.9454447, 19.31163661]], [10.00, [957.9454447, 19.31163661]], [10.01, [957.9454447, 19.31163661]]]$

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [951.0394389, 21.41881679]], [9.99, [951.0394389, 21.41881679]], [10.00, [951.0394389, 21.41881679]], [10.01, [951.0394389, 21.41881679]]]$

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [943.7182031, 23.53845386]], [9.99, [943.7182031, 23.53845386]], [10.00, [943.7182031, 23.53845386]], [10.01, [943.7182031, 23.53845386]]]$

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [935.9999984, 25.67000000]], [9.99, [935.9999984, 25.67000000]], [10.00, [935.9999984, 25.67000000]], [10.01, [935.9999984, 25.67000000]]]$

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [927.9038703, 27.81288384]], [9.99, [927.9038703, 27.81288384]], [10.00, [927.9038703, 27.81288384]], [10.01, [927.9038703, 27.81288384]]]$

*beta is,  $\frac{29}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [919.4495282, 29.96651411]], [9.99, [919.4495282, 29.96651411]], [10.00,$

$[919.4495282, 29.96651411]], [10.01, [919.4495282, 29.96651411]]]$   
 beta is,  $\frac{31}{10}$ , times the threshold value  
 the long-term behavior is  
 $[[9.98, [910.6572255, 32.13028319]], [9.99, [910.6572255, 32.13028319]], [10.00,$   
 $[910.6572255, 32.13028319]], [10.01, [910.6572255, 32.13028319]]]$   
 beta is,  $\frac{33}{10}$ , times the threshold value  
 the long-term behavior is  
 $[[9.98, [901.5476397, 34.30357076]], [9.99, [901.5476397, 34.30357076]], [10.00,$   
 $[901.5476397, 34.30357076]], [10.01, [901.5476397, 34.30357076]]]$   
 beta is,  $\frac{7}{2}$ , times the threshold value  
 the long-term behavior is  
 $[[9.98, [892.1417551, 36.48574730]], [9.99, [892.1417551, 36.48574730]], [10.00,$   
 $[892.1417551, 36.48574730]], [10.01, [892.1417551, 36.48574730]]]$   
 beta is,  $\frac{37}{10}$ , times the threshold value  
 the long-term behavior is  
 $[[9.98, [882.4607475, 38.67617753]], [9.99, [882.4607475, 38.67617753]], [10.00,$   
 $[882.4607475, 38.67617753]], [10.01, [882.4607475, 38.67617753]]]$   
 beta is,  $\frac{39}{10}$ , times the threshold value  
 the long-term behavior is  
 $[[9.98, [872.5258747, 40.87422371]], [9.99, [872.5258747, 40.87422371]], [10.00,$   
 $[872.5258747, 40.87422371]], [10.01, [872.5258747, 40.87422371]]]$   
 # here,  $1000 - (872.5258747 + 40.87422371)$  have died

```
> #LET nu = 3, gamma = 7
SIRSdemo(1000,200,7,3,0.01,10);
```

This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, 10

with population size, 1000, and fixed parameters nu=, 3, and gamma=, 7

where we change beta from  $0.2 * \text{nu}/N$  to  $4 * \text{nu}/N$

Recall that the epidemic will persist if beta exceeds  $\text{nu}/N$ , that in this case is,  $\frac{3}{1000}$

We start with , 200, infected individuals, 0 removed and hence, 800, susceptible

We will show what happens once time is close to, 10

beta is,  $\frac{1}{10}$ , times the threshold value

(3)

*the long-term behavior is*

$[[9.98, [998.9571869, 0.9729968716]], [9.99, [998.9571869, 0.9729968716]], [10.00, [998.9571869, 0.9729968716]], [10.01, [998.9571869, 0.9729968716]]]$

*beta is,  $\frac{3}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [996.6155905, 2.936908621]], [9.99, [996.6155905, 2.936908621]], [10.00, [996.6155905, 2.936908621]], [10.01, [996.6155905, 2.936908621]]]$

*beta is,  $\frac{1}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [993.9350689, 4.924545130]], [9.99, [993.9350689, 4.924545130]], [10.00, [993.9350689, 4.924545130]], [10.01, [993.9350689, 4.924545130]]]$

*beta is,  $\frac{7}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [990.9190693, 6.935665103]], [9.99, [990.9190693, 6.935665103]], [10.00, [990.9190693, 6.935665103]], [10.01, [990.9190693, 6.935665103]]]$

*beta is,  $\frac{9}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [987.5717147, 8.969979927]], [9.99, [987.5717147, 8.969979927]], [10.00, [987.5717147, 8.969979927]], [10.01, [987.5717147, 8.969979927]]]$

*beta is,  $\frac{11}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [983.8977865, 11.02715490]], [9.99, [983.8977865, 11.02715490]], [10.00, [983.8977865, 11.02715490]], [10.01, [983.8977865, 11.02715490]]]$

*beta is,  $\frac{13}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [979.9027040, 13.10681067]], [9.99, [979.9027040, 13.10681067]], [10.00, [979.9027040, 13.10681067]], [10.01, [979.9027040, 13.10681067]]]$

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [975.5925002, 15.20852494]], [9.99, [975.5925002, 15.20852494]], [10.00, [975.5925002, 15.20852494]], [10.01, [975.5925002, 15.20852494]]]$

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [970.9737953, 17.33183428]], [9.99, [970.9737953, 17.33183428]], [10.00, [970.9737953, 17.33183428]], [10.01, [970.9737953, 17.33183428]]]$

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [966.0537675, 19.47623623]], [9.99, [966.0537675, 19.47623623]], [10.00, [966.0537675, 19.47623623]], [10.01, [966.0537675, 19.47623623]]]$

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [960.8401210, 21.64119148]], [9.99, [960.8401210, 21.64119148]], [10.00, [960.8401210, 21.64119148]], [10.01, [960.8401210, 21.64119148]]]$

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [955.3410529, 23.82612625]], [9.99, [955.3410529, 23.82612625]], [10.00, [955.3410529, 23.82612625]], [10.01, [955.3410529, 23.82612625]]]$

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [949.5652167, 26.03043478]], [9.99, [949.5652167, 26.03043478]], [10.00, [949.5652167, 26.03043478]], [10.01, [949.5652167, 26.03043478]]]$

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [943.5216861, 28.25348193]], [9.99, [943.5216861, 28.25348193]], [10.00, [943.5216861, 28.25348193]], [10.01, [943.5216861, 28.25348193]]]$

*beta is,  $\frac{29}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [937.2199158, 30.49460585]], [9.99, [937.2199158, 30.49460585]], [10.00, [937.2199158, 30.49460585]], [10.01, [937.2199158, 30.49460585]]]$

*beta is,  $\frac{31}{10}$ , times the threshold value*

*the long-term behavior is*

$[[9.98, [930.6697029, 32.75312075]], [9.99, [930.6697029, 32.75312075]], [10.00,$

$[930.6697029, 32.75312075]], [10.01, [930.6697029, 32.75312075]]]$   
*beta is,  $\frac{33}{10}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [923.8811464, 35.02831970]], [9.99, [923.8811464, 35.02831970]], [10.00,$   
 $[923.8811464, 35.02831970]], [10.01, [923.8811464, 35.02831970]]]$   
*beta is,  $\frac{7}{2}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [916.8646074, 37.31947743]], [9.99, [916.8646074, 37.31947743]], [10.00,$   
 $[916.8646074, 37.31947743]], [10.01, [916.8646074, 37.31947743]]]$   
*beta is,  $\frac{37}{10}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [909.6306685, 39.62585316]], [9.99, [909.6306685, 39.62585316]], [10.00,$   
 $[909.6306685, 39.62585316]], [10.01, [909.6306685, 39.62585316]]]$   
*beta is,  $\frac{39}{10}$ , times the threshold value*  
*the long-term behavior is*  
 $[[9.98, [902.1900937, 41.94669340]], [9.99, [902.1900937, 41.94669340]], [10.00,$   
 $[902.1900937, 41.94669340]], [10.01, [902.1900937, 41.94669340]]]$ 
(4)

# here,  $1000 - 902.1900937 + 41.94669340$  people died

## #PROBLEM 2

Using RandNice([x,y],8) 3 times, (call it F) each time.

```

> F1 := RandNice([x,y],8);
F2 := RandNice([x,y],8);
F3 := RandNice([x,y],8);
    F1 := [(1 - 2 x - 4 y) (5 - 3 x - 4 y), (8 - x - 7 y) (8 - x - y)]
    F2 := [(2 - 2 x - 3 y) (4 - 7 x - 5 y), (8 - x - 6 y) (4 - x - 7 y)]
    F3 := [(2 - x - 5 y) (1 - x - 4 y), (3 - 5 x - 7 y) (4 - 6 x - 4 y)]

```

(5)

For each of them find the following:

- (i) The set of equilibrium points

```

> print(`Equilibrium points for F1`);
e1 := EquPts(F1,[x,y]);
print(`Equilibrium points for F2`);
e2 := EquPts(F2,[x,y]);
print(`Equilibrium points for F3`);
e3:= EquPts(F3,[x,y]);

```

$$\begin{aligned}
& \text{Equilibrium points for } F1 \\
e1 &:= \left\{ [27, -19], \left[ -\frac{5}{2}, \frac{3}{2} \right], \left[ \frac{3}{17}, \frac{19}{17} \right], \left[ \frac{31}{2}, -\frac{15}{2} \right] \right\} \\
& \text{Equilibrium points for } F2 \\
e2 &:= \left\{ \left[ -\frac{16}{37}, \frac{52}{37} \right], \left[ -\frac{4}{3}, \frac{14}{9} \right], \left[ \frac{2}{11}, \frac{6}{11} \right] \right\} \\
& \text{Equilibrium points for } F3 \\
e3 &:= \left\{ \left[ \frac{1}{18}, \frac{7}{18} \right], \left[ \frac{3}{5}, \frac{1}{10} \right], \left[ \frac{5}{13}, \frac{2}{13} \right], \left[ \frac{6}{13}, \frac{4}{13} \right] \right\} \tag{6}
\end{aligned}$$

(ii) The set of stable equilibrium points

$$\begin{aligned}
> \text{print(`Stable Equilibrium points for F1`)}; \\
s1 := \text{StEquPts}(F1, [x, y]); \\
\text{print(`Stable Equilibrium points for F2`)}; \\
s2 := \text{StEquPts}(F2, [x, y]); \\
\text{print(`Stable Equilibrium points for F3`)}; \\
s3 := \text{StEquPts}(F3, [x, y]);
\end{aligned}
\begin{aligned}
& \text{Stable Equilibrium points for } F1 \\
s1 &:= \left\{ \left[ -\frac{5}{2}, \frac{3}{2} \right], \left[ \frac{31}{2}, -\frac{15}{2} \right] \right\} \\
& \text{Stable Equilibrium points for } F2 \\
s2 &:= \emptyset \\
& \text{Stable Equilibrium points for } F3 \\
s3 &:= \left\{ \left[ \frac{1}{18}, \frac{7}{18} \right] \right\} \tag{7}
\end{aligned}$$

(iii) Using  $\text{Dis2}(F, x, y, \text{pt} + [0.1, 0.1], 0.01, 10)$  ;  
confirm numerically that for **pt** in the stable set it converges to that point, but for the other equilibrium points, the orbit goes elsewhere.

$$\begin{aligned}
> \text{alleged\_unstable1} := e1 \text{ minus } s1; \\
\text{alleged\_unstable2} &:= e2 \text{ minus } s2; \\
\text{alleged\_unstable3} &:= e3 \text{ minus } s3;
\end{aligned}
\begin{aligned}
\text{alleged\_unstable1} &:= \left\{ [27, -19], \left[ \frac{3}{17}, \frac{19}{17} \right] \right\} \\
\text{alleged\_unstable2} &:= \left\{ \left[ -\frac{16}{37}, \frac{52}{37} \right], \left[ -\frac{4}{3}, \frac{14}{9} \right], \left[ \frac{2}{11}, \frac{6}{11} \right] \right\} \\
\text{alleged\_unstable3} &:= \left\{ \left[ \frac{3}{5}, \frac{1}{10} \right], \left[ \frac{5}{13}, \frac{2}{13} \right], \left[ \frac{6}{13}, \frac{4}{13} \right] \right\} \tag{8}
\end{aligned}$$

```

> #Stable equilibria of f1:
if nops(s1)=0 then print(`no stable equilibra`);
end if;
for i in s1 do:
print(`for stable equilibrium point`, i);
print(Dis2(F1,x,y,i+[0.01,0.01],0.01,10));
od:

```

*for stable equilibrium point,  $\left[ -\frac{5}{2}, \frac{3}{2} \right]$*

```

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```

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$[-2.499999993, 1.499999998]], [9.76, [-2.499999993, 1.499999998]], [9.77,$   
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 $[-2.499999993, 1.499999998]]]$

$$\text{for stable equilibrium point, } \left[ \frac{31}{2}, -\frac{15}{2} \right]$$

$[[0.01, [15.51000000, -7.490000000]], [0.02, [15.51694200, -7.498984000]], [0.03,$   
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$[15.50000015, -7.500000125]]$ ,  $[1.98, [15.50000013, -7.500000136]]$ ,  $[1.99, [15.50000010, -7.500000133]]$ ,  $[2.00, [15.50000006, -7.500000118]]$ ,  $[2.01, [15.50000002, -7.500000092]]$ ,  $[2.02, [15.49999998, -7.500000060]]$ ,  $[2.03, [15.49999995, -7.500000024]]$ ,  $[2.04, [15.49999993, -7.499999991]]$ ,  $[2.05, [15.49999992, -7.499999964]]$ ,  $[2.06, [15.49999992, -7.499999944]]$ ,  $[2.07, [15.49999993, -7.499999933]]$ ,  $[2.08, [15.49999994, -7.499999932]]$ ,  $[2.09, [15.49999996, -7.499999936]]$ ,  $[2.10, [15.49999998, -7.499999947]]$ ,  $[2.11, [15.50000000, -7.499999962]]$ ,  $[2.12, [15.50000002, -7.499999979]]$ ,  $[2.13, [15.50000003, -7.499999997]]$ ,  $[2.14, [15.50000004, -7.500000012]]$ ,  $[2.15, [15.50000004, -7.500000025]]$ ,  $[2.16, [15.50000004, -7.500000032]]$ ,  $[2.17, [15.50000003, -7.500000036]]$ ,  $[2.18, [15.50000002, -7.500000033]]$ ,  $[2.19, [15.50000001, -7.500000027]]$ ,  $[2.20, [15.50000000, -7.500000019]]$ ,  $[2.21, [15.49999999, -7.500000010]]$ ,  $[2.22, [15.49999998, -7.500000001]]$ ,  $[2.23, [15.49999998, -7.499999992]]$ ,  $[2.24, [15.49999998, -7.499999987]]$ ,  $[2.25, [15.49999998, -7.499999984]]$ ,  $[2.26, [15.49999998, -7.499999982]]$ ,  $[2.27, [15.49999998, -7.499999981]]$ ,  $[2.28, [15.49999998, -7.499999981]]$ ,  $[2.29, [15.49999998, -7.499999981]]$ ,  $[2.30, [15.49999998, -7.499999981]]$ ,  $[2.31, [15.49999998, -7.499999981]]$ ,  $[2.32, [15.49999998, -7.499999981]]$ ,  $[2.33, [15.49999998, -7.499999981]]$ ,  $[2.34, [15.49999998, -7.499999981]]$ ,  $[2.35, [15.49999998, -7.499999981]]$ ,  $[2.36, [15.49999998, -7.499999981]]$ ,  $[2.37, [15.49999998, -7.499999981]]$ ,  $[2.38, [15.49999998, -7.499999981]]$ ,  $[2.39, [15.49999998, -7.499999981]]$ ,  $[2.40, [15.49999998, -7.499999981]]$ ,  $[2.41, [15.49999998, -7.499999981]]$ ,  $[2.42, [15.49999998, -7.499999981]]$ ,  $[2.43, [15.49999998, -7.499999981]]$ ,  $[2.44, [15.49999998, -7.499999981]]$ ,  $[2.45, [15.49999998, -7.499999981]]$ ,  $[2.46, [15.49999998, -7.499999981]]$ ,  $[2.47, [15.49999998, -7.499999981]]$ ,  $[2.48, [15.49999998, -7.499999981]]$ ,  $[2.49, [15.49999998, -7.499999981]]$ ,  $[2.50, [15.49999998, -7.499999981]]$ ,  $[2.51, [15.49999998, -7.499999981]]$ ,  $[2.52, [15.49999998, -7.499999981]]$ ,  $[2.53, [15.49999998, -7.499999981]]$ ,  $[2.54, [15.49999998, -7.499999981]]$ ,  $[2.55, [15.49999998, -7.499999981]]$ ,  $[2.56, [15.49999998, -7.499999981]]$ ,  $[2.57, [15.49999998, -7.499999981]]$ ,  $[2.58, [15.49999998, -7.499999981]]$ ,  $[2.59, [15.49999998, -7.499999981]]$ ,  $[2.60, [15.49999998, -7.499999981]]$ ,  $[2.61, [15.49999998, -7.499999981]]$ ,  $[2.62, [15.49999998, -7.499999981]]$ ,  $[2.63, [15.49999998, -7.499999981]]$ ,  $[2.64, [15.49999998, -7.499999981]]$ ,  $[2.65, [15.49999998, -7.499999981]]$ ,  $[2.66, [15.49999998, -7.499999981]]$ ,  $[2.67, [15.49999998, -7.499999981]]$ ,  $[2.68, [15.49999998, -7.499999981]]$ ,  $[2.69, [15.49999998, -7.499999981]]$ ,  $[2.70, [15.49999998, -7.499999981]]$ ,  $[2.71, [15.49999998, -7.499999981]]$ ,  $[2.72, [15.49999998, -7.499999981]]$ ,  $[2.73,$



















```

[15.49999998, -7.499999981]], [9.58, [15.49999998, -7.499999981]], [9.59,
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[15.49999998, -7.499999981]], [10.00, [15.49999998, -7.499999981]], [10.01,
[15.49999998, -7.499999981]]]

```

```

> #unstable equilibrium point of f1:
for i in alleged_unstable1 do:
print(`for unstable equilibrium point`, i);
print(Dis2(F1,x,y,i+[0.01,0.01],0.01,10));
od:

```

*for unstable equilibrium point, [27, -19]*

```

[[0.01, [27.01, -18.99]], [0.02, [26.993942, -19.012784]], [0.03, [27.00992714,
-18.99128612]], [0.04, [26.99509601, -19.01252366]], [0.05, [27.01004035,
-18.99264001]], [0.06, [26.99637081, -19.01246569]], [0.07, [27.01037809,
-18.99410290]], [0.08, [26.99781614, -19.01264821]], [0.09, [27.01099076,
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-18.99757447]], [0.12, [27.00148648, -19.01395170]], [0.13, [27.01332350,
-18.99972936]], [0.14, [27.00389268, -19.01522461]], [0.15, [27.01523951,
-19.00229457]], [0.16, [27.00684304, -19.01705191]], [0.17, [27.01783509,

```

$-19.00540231]], [0.18, [27.01050349, -19.01957816]], [0.19, [27.02129481, -19.00922155]], [0.20, [27.01508676, -19.02299029]], [0.21, [27.02585682, -19.01396874]], [0.22, [27.02086595, -19.02752970]], [0.23, [27.03182827, -19.01992157]], [0.24, [27.02819208, -19.03350802]], [0.25, [27.03960532, -19.02743688]], [0.26, [27.03751681, -19.04132745]], [0.27, [27.04969909, -19.03697373]], [0.28, [27.04942197, -19.05150725]], [0.29, [27.06276939, -19.04912354]], [0.30, [27.06465798, -19.06471817]], [0.31, [27.07966877, -19.06464932]], [0.32, [27.08419414, -19.08182750]], [0.33, [27.10150024, -19.08453703]], [0.34, [27.10928462, -19.10395825]], [0.35, [27.12969337, -19.11006325]], [0.36, [27.14155569, -19.13256737]], [0.37, [27.16610525, -19.14288474]], [0.38, [27.18312183, -19.16954980]], [0.39, [27.21315549, -19.18515814]], [0.40, [27.23674168, -19.21737832]], [0.41, [27.27400880, -19.23970135]], [0.42, [27.30602984, -19.27929349]], [0.43, [27.35282487, -19.31021382]], [0.44, [27.39574854, -19.35956537]], [0.45, [27.45510567, -19.40158170]], [0.46, [27.51221563, -19.46386003]], [0.47, [27.58818727, -19.52030785]], [0.48, [27.66388668, -19.59976340]], [0.49, [27.76195153, -19.67513035]], [0.50, [27.86220394, -19.77754805]], [0.51, [27.98988312, -19.87793354]], [0.52, [28.12286719, -20.01132779]], [0.53, [28.29068830, -20.14512647]], [0.54, [28.46779238, -20.32085628]], [0.55, [28.69086554, -20.49979242]], [0.56, [28.92822982, -20.73444489]], [0.57, [29.22897094, -20.97515074]], [0.58, [29.54990291, -21.29394151]], [0.59, [29.96309758, -21.62031197]], [0.60, [30.40176166, -22.06380486]], [0.61, [30.98500278, -22.51005948]], [0.62, [31.59118386, -23.14926388]], [0.63, [32.44994377, -23.76111828]], [0.64, [33.28917879, -24.73840931]], [0.65, [34.65292638, -25.55288549]], [0.66, [35.75579806, -27.22733772]], [0.67, [38.30616031, -28.08785911]], [0.68, [39.20000665, -31.77709040]], [0.69, [46.41186362, -30.67347759]], [0.70, [42.84892571, -44.31644403]], [0.71, [92.57548824, -18.24610025]], [0.72, [314.6219002, -46.86538294]], [0.73, [3626.678242, -102.5462196]], [0.74, [719649.6632, 101895.3350]], [0.75, [4.740135409  $\times 10^{10}$ , 1.177197955  $\times 10^{10}]], [0.76, [2.685875769  $\times 10^{20}$ , 7.681007052  $\times 10^{19}]], [0.77, [9.398369244  $\times 10^{39}$ , 2.784796407  $\times 10^{39}]], [0.78, [1.177508421  $\times 10^{79}$ , 3.519953408  $\times 10^{78}]], [0.79, [1.859111757  $\times 10^{157}$ , 5.569650946  $\times 10^{156}]], [0.80, [4.641034812$$$$$$

$$\begin{aligned}
& \times 10^{313}, 1.391145019 \times 10^{313}]], [0.81, [2.893268255 \times 10^{626}, 8.673701504 \times 10^{625}]], [0.82, \\
& [1.124539933 \times 10^{1252}, 3.371359421 \times 10^{1251}]], [0.83, [1.698856725 \times 10^{2503}, 5.093197203 \\
& \times 10^{2502}]], [0.84, [3.877241491 \times 10^{5005}, 1.162405007 \times 10^{5005}]], [0.85, [2.019554743 \\
& \times 10^{10010}, 6.054669876 \times 10^{10009}]], [0.86, [5.479252705 \times 10^{20019}, 1.642692309 \\
& \times 10^{20019}]], [0.87, [4.033227954 \times 10^{40038}, 1.209170865 \times 10^{40038}]], [0.88, [2.185323080 \\
& \times 10^{80076}, 6.551648087 \times 10^{80075}]], [0.89, [6.415661217 \times 10^{160151}, 1.923429767 \\
& \times 10^{160151}]], [0.90, [5.529590414 \times 10^{320302}, 1.657783734 \times 10^{320302}]], [0.91, \\
& [4.107674725 \times 10^{640604}, 1.231490188 \times 10^{640604}]], [0.92, [2.266742616 \times 10^{1281208}, \\
& 6.795745718 \times 10^{1281207}]], [0.93, [6.902629095 \times 10^{2562415}, 2.069423842 \times 10^{2562415}]], \\
& [0.94, [6.400872756 \times 10^{5124830}, 1.918996154 \times 10^{5124830}]], [0.95, [5.504127763 \\
& \times 10^{10249660}, 1.650149974 \times 10^{10249660}]], [0.96, [4.069931795 \times 10^{20499320}, 1.220174773 \\
& \times 10^{20499320}]], [0.97, [2.225278545 \times 10^{40998640}, 6.671435501 \times 10^{40998639}]], [0.98, \\
& [6.652408044 \times 10^{81997279}, 1.994407005 \times 10^{81997279}]], [0.99, [5.945219296 \times 10^{163994558}, \\
& 1.782390215 \times 10^{163994558}]], [1.00, [4.748384469 \times 10^{327989116}, 1.423576422 \\
& \times 10^{327989116}]], [1.01, [3.029018113 \times 10^{655978232}, 9.081064923 \times 10^{655978231}]], [1.02, \\
& [1.232576431 \times 10^{1311956464}, 3.695292064 \times 10^{1311956463}]], [1.03, [2.040975711 \\
& \times 10^{2623912927}, 6.118891421 \times 10^{2623912926}]], [1.04, [5.596104180 \times 10^{5247825853}, \\
& 1.677724712 \times 10^{5247825853}]], [1.05, [4.207089009 \times 10^{10495651706}, 1.261294816 \\
& \times 10^{10495651706}]], [1.06, [2.377790125 \times 10^{20991303412}, 7.128668667 \times 10^{20991303411}]], \\
& [1.07, [7.595513791 \times 10^{41982606823}, 2.277152244 \times 10^{41982606823}]], [1.08, [7.750405615 \\
& \times 10^{83965213646}, 2.323589163 \times 10^{83965213646}]], [1.09, [8.069729584 \times 10^{167930427292}, \\
& 2.419323214 \times 10^{167930427292}]], [1.10, [8.748388929 \times 10^{335860854584}, 2.622786822 \\
& \times 10^{335860854584}]], [1.11, [1.028173209 \times 10^{671721709169}, 3.082486574 \times 10^{671721709168}]], \\
& [1.12, [1.420177687 \times 10^{1343443418337}, 4.257724880 \times 10^{1343443418336}]], [1.13, [2.709539510 \\
& \times 10^{2686886836673}, 8.123260841 \times 10^{2686886836672}]], [1.14, [9.862819723 \times 10^{5373773673345}, \\
& 2.956895698 \times 10^{5373773673345}]], [1.15, [1.306809576 \times 10^{10747547346691}, 3.917844717 \\
& \times 10^{10747547346690}]], [1.16, [2.294218275 \times 10^{21495094693381}, 6.878118370 \\
& \times 10^{21495094693380}]], [1.17, [7.070979665 \times 10^{42990189386761}, 2.119895724 \\
& \times 10^{42990189386761}]], [1.18, [6.716906381 \times 10^{85980378773522}, 2.013743751 \\
& \times 10^{85980378773522}]], [1.19, [6.061061750 \times 10^{171960757547044}, 1.817120046 \\
& \times 10^{171960757547044}]], [1.20, [4.935231573 \times 10^{343921515094088}, 1.479593608 \\
& \times 10^{343921515094088}]], [1.21, [3.272089618 \times 10^{687843030188176}, 9.809798811
\end{aligned}$$

$$\begin{aligned}
& \times 10^{687843030188175}]], [1.22, [1.438336489 \times 10^{1375686060376352}, 4.312165385 \\
& \times 10^{1375686060376351}]], [1.23, [2.779272402 \times 10^{2751372120752703}, 8.332321636 \\
& \times 10^{2751372120752702}]], [1.24, [1.037701270 \times 10^{5502744241505406}, 3.111051921 \\
& \times 10^{5502744241505405}]], [1.25, [1.446621166 \times 10^{11005488483010811}, 4.337003033 \\
& \times 10^{11005488483010810}]], [1.26, [2.811381280 \times 10^{22010976966021621}, 8.428584776 \\
& \times 10^{22010976966021620}]], [1.27, [1.061816857 \times 10^{44021953932043242}, 3.183350996 \\
& \times 10^{44021953932043241}]], [1.28, [1.514639749 \times 10^{88043907864086483}, 4.540924288 \\
& \times 10^{88043907864086482}]], [1.29, [3.081972920 \times 10^{176087815728172965}, 9.239824647 \\
& \times 10^{176087815728172964}]], [1.30, [1.276050187 \times 10^{352175631456345930}, 3.825627373 \\
& \times 10^{352175631456345929}]], [1.31, [2.187487749 \times 10^{704351262912691859}, 6.558137834 \\
& \times 10^{704351262912691858}]], [1.32, [6.428377575 \times 10^{1408702525825383717}, 1.927242161 \\
& \times 10^{1408702525825383717}]], [1.33, [5.551532325 \times 10^{2817405051650767434}, 1.664361970 \\
& \times 10^{2817405051650767434}]], [1.34, [4.140338648 \times 10^{5634810103301534868}, 1.241282908 \\
& \times 10^{5634810103301534868}]], [1.35, [Float(\infty), Float(\infty)]], [1.36, [Float(\infty), Float(\infty)]], \\
[1.37, [Float(\infty), Float(\infty)]], [1.38, [Float(\infty), Float(\infty)]], [1.39, [Float(\infty), \\
Float(\infty)]], [1.40, [Float(\infty), Float(\infty)]], [1.41, [Float(\infty), Float(\infty)]], [1.42, [ \\
Float(\infty), Float(\infty)]], [1.43, [Float(\infty), Float(\infty)]], [1.44, [Float(\infty), Float(\infty)]], \\
[1.45, [Float(\infty), Float(\infty)]], [1.46, [Float(\infty), Float(\infty)]], [1.47, [Float(\infty), \\
Float(\infty)]], [1.48, [Float(\infty), Float(\infty)]], [1.49, [Float(\infty), Float(\infty)]], [1.50, [ \\
Float(\infty), Float(\infty)]], [1.51, [Float(\infty), Float(\infty)]], [1.52, [Float(\infty), Float(\infty)]], \\
[1.53, [Float(\infty), Float(\infty)]], [1.54, [Float(\infty), Float(\infty)]], [1.55, [Float(\infty), \\
Float(\infty)]], [1.56, [Float(\infty), Float(\infty)]], [1.57, [Float(\infty), Float(\infty)]], [1.58, [ \\
Float(\infty), Float(\infty)]], [1.59, [Float(\infty), Float(\infty)]], [1.60, [Float(\infty), Float(\infty)]], \\
[1.61, [Float(\infty), Float(\infty)]], [1.62, [Float(\infty), Float(\infty)]], [1.63, [Float(\infty), \\
Float(\infty)]], [1.64, [Float(\infty), Float(\infty)]], [1.65, [Float(\infty), Float(\infty)]], [1.66, [ \\
Float(\infty), Float(\infty)]], [1.67, [Float(\infty), Float(\infty)]], [1.68, [Float(\infty), Float(\infty)]], \\
[1.69, [Float(\infty), Float(\infty)]], [1.70, [Float(\infty), Float(\infty)]], [1.71, [Float(\infty), \\
Float(\infty)]], [1.72, [Float(\infty), Float(\infty)]], [1.73, [Float(\infty), Float(\infty)]], [1.74, [ \\
Float(\infty), Float(\infty)]], [1.75, [Float(\infty), Float(\infty)]], [1.76, [Float(\infty), Float(\infty)]], \\
[1.77, [Float(\infty), Float(\infty)]], [1.78, [Float(\infty), Float(\infty)]], [1.79, [Float(\infty), \\
Float(\infty)]], [1.80, [Float(\infty), Float(\infty)]], [1.81, [Float(\infty), Float(\infty)]], [1.82, [ \\
Float(\infty), Float(\infty)]], [1.83, [Float(\infty), Float(\infty)]], [1.84, [Float(\infty), Float(\infty)]], \\
[1.85, [Float(\infty), Float(\infty)]], [1.86, [Float(\infty), Float(\infty)]], [1.87, [Float(\infty), \\
Float(\infty)]], [1.88, [Float(\infty), Float(\infty)]], [1.89, [Float(\infty), Float(\infty)]], [1.90, [ \\
Float(\infty), Float(\infty)]], [1.91, [Float(\infty), Float(\infty)]], [1.92, [Float(\infty), Float(\infty)]]]
\end{aligned}$$

















*for unstable equilibrium point,  $\left[ \frac{3}{17}, \frac{19}{17} \right]$*

- (10)
- $[ [0.01, [0.1864705882, 1.127647059]], [0.02, [0.1891890588, 1.122298353]], [0.03,$   
 $[0.1913843151, 1.119269960]], [0.04, [0.1933618230, 1.117512399]], [0.05,$   
 $[0.1952954188, 1.116445576]], [0.06, [0.1972879513, 1.115749031]], [0.07,$   
 $[0.1994042145, 1.115245425]], [0.08, [0.2016889919, 1.114836135]], [0.09,$   
 $[0.2041770300, 1.114465741]], [0.10, [0.2068986169, 1.114102461]], [0.11,$   
 $[0.2098827670, 1.113727379]], [0.12, [0.2131591076, 1.113328503]], [0.13,$   
 $[0.2167590701, 1.112897486]], [0.14, [0.2207167191, 1.112427796]], [0.15,$   
 $[0.2250694057, 1.111913695]], [0.16, [0.2298583517, 1.111349653]], [0.17,$   
 $[0.2351292290, 1.110729991]], [0.18, [0.2409327720, 1.110048662]], [0.19,$   
 $[0.2473254542, 1.109299091]], [0.20, [0.2543702522, 1.108474044]], [0.21,$   
 $[0.2621375198, 1.107565513]], [0.22, [0.2707059977, 1.106564596]], [0.23,$   
 $[0.2801639866, 1.105461370]], [0.24, [0.2906107185, 1.104244750]], [0.25,$   
 $[0.3021579674, 1.102902323]], [0.26, [0.3149319506, 1.101420161]], [0.27,$   
 $[0.3290755857, 1.099782605]], [0.28, [0.3447511843, 1.097972004]], [0.29,$   
 $[0.3621436853, 1.095968414]], [0.30, [0.3814645602, 1.093749237]], [0.31,$   
 $[0.4029565604, 1.091288791]], [0.32, [0.4268995287, 1.088557799]], [0.33,$   
 $[0.4536175660, 1.085522766]], [0.34, [0.4834879394, 1.082145227]], [0.35,$   
 $[0.5169522480, 1.078380831]], [0.36, [0.5545305476, 1.074178212]], [0.37,$   
 $[0.5968393926, 1.069477599]], [0.38, [0.6446151291, 1.064209078]], [0.39,$   
 $[0.6987443118, 1.058290423]], [0.40, [0.7603039283, 1.051624355]], [0.41,$   
 $[0.8306153273, 1.044095055]], [0.42, [0.9113176195, 1.035563708]], [0.43,$   
 $[1.004469269, 1.025862764]], [0.44, [1.112691341, 1.014788516]], [0.45, [1.239373740,$   
 $1.002091484]], [0.46, [1.388979182, 0.9874639921]], [0.47, [1.567503328,$   
 $0.9705243134]], [0.48, [1.783192870, 0.9507971155]], [0.49, [2.047706450,$   
 $0.9276913023]], [0.50, [2.378070478, 0.9004807916]], [0.51, [2.800138940,$   
 $0.8683071393]], [0.52, [3.355083142, 0.8302635814]], [0.53, [4.112468735,$   
 $0.7857493161]], [0.54, [5.199070125, 0.7357264460]], [0.55, [6.870062093,$   
 $0.6872116113]], [0.56, [9.713687281, 0.6709168780]], [0.57, [15.37666718,$   
 $0.8237725186]], [0.58, [30.05846001, 1.901562443]], [0.59, [91.96530440,$   
 $10.37607793]], [0.60, [793.1005008, 158.1126542]], [0.61, [67472.38755, 18002.65933]],$   
 $[0.62, [5.679975654 \times 10^8, 1.653822114 \times 10^8]], [0.63, [4.252081736 \times 10^{16}, 1.265573710$

$\times 10^{16}]], [0.64, [2.417344807 \times 10^{32}, 7.234251968 \times 10^{31}]], [0.65, [7.841020261 \times 10^{63},$   
 $2.349710917 \times 10^{63}]], [0.66, [8.257104728 \times 10^{126}, 2.475226358 \times 10^{126}]], [0.67,$   
 $[9.158706645 \times 10^{252}, 2.745726234 \times 10^{252}]], [0.68, [1.126861668 \times 10^{505}, 3.378334041$   
 $\times 10^{504}]], [0.69, [1.705883612 \times 10^{1009}, 5.114269187 \times 10^{1008}]], [0.70, [3.909384927$   
 $\times 10^{2017}, 1.172041975 \times 10^{2017}]], [0.71, [2.053179258 \times 10^{4034}, 6.155477308 \times 10^{4033}]],$   
 $[0.72, [5.663225120 \times 10^{8067}, 1.697847680 \times 10^{8067}]], [0.73, [4.308615731 \times 10^{16134},$   
 $1.291732750 \times 10^{16134}]], [0.74, [2.493937939 \times 10^{32268}, 7.476882437 \times 10^{32267}]], [0.75,$   
 $[8.355672356 \times 10^{64535}, 2.505049503 \times 10^{64535}]], [0.76, [9.379353888 \times 10^{129070},$   
 $2.811951547 \times 10^{129070}]], [0.77, [1.181832594 \times 10^{258141}, 3.543160895 \times 10^{258140}]], [0.78,$   
 $[1.876385400 \times 10^{516281}, 5.625445945 \times 10^{516280}]], [0.79, [4.729924503 \times 10^{1032561},$   
 $1.418042083 \times 10^{1032561}]], [0.80, [3.005512483 \times 10^{2065122}, 9.010594518 \times 10^{2065121}]],$   
 $[0.81, [1.213520705 \times 10^{4130244}, 3.638162568 \times 10^{4130243}]], [0.82, [1.978356252$   
 $\times 10^{8260487}, 5.931156867 \times 10^{8260486}]], [0.83, [5.257982279 \times 10^{16520973}, 1.576355000$   
 $\times 10^{16520973}]], [0.84, [3.714055205 \times 10^{33041946}, 1.113482165 \times 10^{33041946}]], [0.85,$   
 $[1.853134016 \times 10^{66083892}, 5.555737763 \times 10^{66083891}]], [0.86, [4.613428288 \times 10^{132167783},$   
 $1.383116253 \times 10^{132167783}]], [0.87, [2.859286454 \times 10^{264335566}, 8.572205574$   
 $\times 10^{264335565}]], [0.88, [1.098311300 \times 10^{528671132}, 3.292762163 \times 10^{528671131}]], [0.89,$   
 $[1.620544728 \times 10^{1057342263}, 4.858429810 \times 10^{1057342262}]], [0.90, [3.528029136$   
 $\times 10^{2114684525}, 1.057711128 \times 10^{2114684525}]], [0.91, [1.672146963 \times 10^{4229369050},$   
 $5.013134480 \times 10^{4229369049}]], [0.92, [3.756289076 \times 10^{8458738099}, 1.126143975$   
 $\times 10^{8458738099}]], [0.93, [1.895518960 \times 10^{16917476198}, 5.682808787 \times 10^{16917476197}]], [0.94,$   
 $[4.826878689 \times 10^{33834952395}, 1.447109167 \times 10^{33834952395}]], [0.95, [3.129989545$   
 $\times 10^{67669904790}, 9.383779567 \times 10^{67669904789}]], [0.96, [1.316121222 \times 10^{135339809580},$   
 $3.945761243 \times 10^{135339809579}]], [0.97, [2.327029573 \times 10^{270679619159}, 6.976487382$   
 $\times 10^{270679619158}]], [0.98, [7.274680490 \times 10^{541359238317}, 2.180965693 \times 10^{541359238317}]],$   
 $[0.99, [7.109482105 \times 10^{1082718476634}, 2.131438843 \times 10^{1082718476634}]], [1.00, [6.790254457$   
 $\times 10^{2165436953268}, 2.035733670 \times 10^{2165436953268}]], [1.01, [6.194157111 \times 10^{4330873906536},$   
 $1.857022337 \times 10^{4330873906536}]], [1.02, [5.154357675 \times 10^{8661747813072}, 1.545288109$   
 $\times 10^{8661747813072}]], [1.03, [3.569104163 \times 10^{17323495626144}, 1.070025514$   
 $\times 10^{17323495626144}]], [1.04, [1.711309511 \times 10^{34646991252288}, 5.130544686$   
 $\times 10^{34646991252287}]], [1.05, [3.934297949 \times 10^{69293982504575}, 1.179511439$   
 $\times 10^{69293982504575}]], [1.06, [2.079431466 \times 10^{138587965009150}, 6.234182647$

$$\begin{aligned}
& \times 10^{138587965009149}], [1.07, [5.808972778 \times 10^{277175930018299}, 1.741543200 \\
& \times 10^{277175930018299}], [1.08, [4.533240927 \times 10^{554351860036598}, 1.359075901 \\
& \times 10^{554351860036598}], [1.09, [2.760754066 \times 10^{1108703720073196}, 8.276803239 \\
& \times 10^{1108703720073195}], [1.10, [1.023918899 \times 10^{2217407440146392}, 3.069732060 \\
& \times 10^{2217407440146391}], [1.11, [1.408449360 \times 10^{4434814880292783}, 4.222563093 \\
& \times 10^{4434814880292782}], [1.12, [2.664971642 \times 10^{8869629760585565}, 7.989645362 \\
& \times 10^{8869629760585564}], [1.13, [9.541030903 \times 10^{17739259521171129}, 2.860422682 \\
& \times 10^{17739259521171129}], [1.14, [1.222927535 \times 10^{35478519042342259}, 3.666364455 \\
& \times 10^{35478519042342258}], [1.15, [2.009146316 \times 10^{70957038084684517}, 6.023466172 \\
& \times 10^{70957038084684516}], [1.16, [5.422920641 \times 10^{141914076169369033}, 1.625803894 \\
& \times 10^{141914076169369033}], [1.17, [3.950723325 \times 10^{283828152338738066}, 1.184435804 \\
& \times 10^{283828152338738066}], [1.18, [2.096830629 \times 10^{567656304677476132}, 6.286345725 \\
& \times 10^{567656304677476131}], [1.19, [5.906589945 \times 10^{1135312609354952263}, 1.770809048 \\
& \times 10^{1135312609354952263}], [1.20, [4.686879220 \times 10^{2270625218709904526}, 1.405137009 \\
& \times 10^{2270625218709904526}], [1.21, [2.951057303 \times 10^{4541250437419809052}, 8.847336649 \\
& \times 10^{4541250437419809051}], [1.22, [1.169944886 \times 10^{9082500874839618104}, 3.507521275 \\
& \times 10^{9082500874839618103}], [1.23, [Float(\infty), Float(\infty)]], [1.24, [Float(\infty), Float(\infty)]], \\
[1.25, [Float(\infty), Float(\infty)]], [1.26, [Float(\infty), Float(\infty)]], [1.27, [Float(\infty), \\
Float(\infty)]], [1.28, [Float(\infty), Float(\infty)]], [1.29, [Float(\infty), Float(\infty)]], [1.30, [ \\
Float(\infty), Float(\infty)]], [1.31, [Float(\infty), Float(\infty)]], [1.32, [Float(\infty), Float(\infty)]], \\
[1.33, [Float(\infty), Float(\infty)]], [1.34, [Float(\infty), Float(\infty)]], [1.35, [Float(\infty), \\
Float(\infty)]], [1.36, [Float(\infty), Float(\infty)]], [1.37, [Float(\infty), Float(\infty)]], [1.38, [ \\
Float(\infty), Float(\infty)]], [1.39, [Float(\infty), Float(\infty)]], [1.40, [Float(\infty), Float(\infty)]], \\
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Float(\infty), Float(\infty)]], [1.55, [Float(\infty), Float(\infty)]], [1.56, [Float(\infty), Float(\infty)]], \\
[1.57, [Float(\infty), Float(\infty)]], [1.58, [Float(\infty), Float(\infty)]], [1.59, [Float(\infty), \\
Float(\infty)]], [1.60, [Float(\infty), Float(\infty)]], [1.61, [Float(\infty), Float(\infty)]], [1.62, [ \\
Float(\infty), Float(\infty)]], [1.63, [Float(\infty), Float(\infty)]], [1.64, [Float(\infty), Float(\infty)]], \\
[1.65, [Float(\infty), Float(\infty)]], [1.66, [Float(\infty), Float(\infty)]], [1.67, [Float(\infty), \\
Float(\infty)]], [1.68, [Float(\infty), Float(\infty)]], [1.69, [Float(\infty), Float(\infty)]], [1.70, [ \\
Float(\infty), Float(\infty)]], [1.71, [Float(\infty), Float(\infty)]], [1.72, [Float(\infty), Float(\infty)]]]
\end{aligned}$$

















```

Float(∞)], [9.84, [Float(∞), Float(∞)]], [9.85, [Float(∞), Float(∞)]], [9.86, [
Float(∞), Float(∞)]], [9.87, [Float(∞), Float(∞)]], [9.88, [Float(∞), Float(∞)]],
[9.89, [Float(∞), Float(∞)]], [9.90, [Float(∞), Float(∞)]], [9.91, [Float(∞),
Float(∞)]], [9.92, [Float(∞), Float(∞)]], [9.93, [Float(∞), Float(∞)]], [9.94, [
Float(∞), Float(∞)]], [9.95, [Float(∞), Float(∞)]], [9.96, [Float(∞), Float(∞)]],
[9.97, [Float(∞), Float(∞)]], [9.98, [Float(∞), Float(∞)]], [9.99, [Float(∞),
Float(∞)]], [10.00, [Float(∞), Float(∞)]], [10.01, [Float(∞), Float(∞)]]]

> #Stable equilibrium points of f2
if nops(s2)=0 then print(`no stable equilibra`);
end if;
for i in s2 do:
print(`for stable equilibrium point`, i);
print(Dis2(F2,x,y,i+[0.01,0.01],0.01,10));
od:

```

*no stable equilibra*

(11)

```

> #unstable equilibrium point of f2:
for i in alleged_unstable2 do:
print(`for unstable equilibrium point`, i);
print(Dis2(F2,x,y,i+[0.01,0.01],0.01,10));
od:

```

*for unstable equilibrium point,  $\left[ -\frac{16}{37}, \frac{52}{37} \right]$*

```

[[0.01, [-0.4224324324, 1.415405405]], [0.02, [-0.4207508108, 1.419245189]], [0.03,
[-0.4186127186, 1.424468035]], [0.04, [-0.4158545210, 1.431586299]], [0.05,
[-0.4122415216, 1.441320559]], [0.06, [-0.4074295126, 1.454700222]], [0.07,
[-0.4008995440, 1.473226309]], [0.08, [-0.3918420907, 1.499146581]], [0.09,
[-0.3789402830, 1.535945032]], [0.10, [-0.3599386012, 1.589267109]], [0.11,
[-0.3307195297, 1.668799973]], [0.12, [-0.2831411378, 1.792447683]], [0.13,
[-0.1993644865, 1.996695977]], [0.14, [-0.0345955061, 2.366365087]], [0.15,
[0.3471569686, 3.138661083]], [0.16, [1.492607022, 5.186428835]], [0.17, [6.849781371,
13.50441920]], [0.18, [65.05170752, 91.28852853]], [0.19, [3714.144767, 4325.200538]],
[0.20, [9.719302001  $\times 10^6$ , 1.008383417  $\times 10^7$ ]], [0.21, [5.886006570  $\times 10^{13}$ , 5.639282587
 $\times 10^{13}$ ]], [0.22, [1.991032133  $\times 10^{27}$ , 1.801815520  $\times 10^{27}$ ]], [0.23, [2.154086634  $\times 10^{54}$ ,
1.869559977  $\times 10^{54}$ ]], [0.24, [2.422330857  $\times 10^{108}$ , 2.037943025  $\times 10^{108}$ ]], [0.25,
[2.974795320  $\times 10^{216}$ , 2.444780210  $\times 10^{216}$ ]], [0.26, [4.390002974  $\times 10^{432}$ , 3.544266882
 $\times 10^{432}$ ]]

```

$$\begin{aligned}
& \times 10^{432}]], [0.27, [9.405767886 \times 10^{864}, 7.491403384 \times 10^{864}]], [0.28, [4.264709884 \\
& \times 10^{1729}, 3.361566923 \times 10^{1729}]], [0.29, [8.685498266 \times 10^{3458}, 6.791627016 \times 10^{3458}]], \\
& [0.30, [3.576671889 \times 10^{6917}, 2.779590817 \times 10^{6917}]], [0.31, [6.031802363 \times 10^{13834}, \\
& 4.665317328 \times 10^{13834}]], [0.32, [1.708183178 \times 10^{27669}, 1.316343979 \times 10^{27669}]], [0.33, \\
& [1.365471347 \times 10^{55338}, 1.049251079 \times 10^{55338}]], [0.34, [8.703147618 \times 10^{110675}, \\
& 6.672887042 \times 10^{110675}]], [0.35, [3.528666971 \times 10^{221351}, 2.700873053 \times 10^{221351}]], [0.36, \\
& [5.791865245 \times 10^{442702}, 4.427257910 \times 10^{442702}]], [0.37, [1.558553549 \times 10^{885405}, \\
& 1.190118488 \times 10^{885405}]], [0.38, [1.127537437 \times 10^{1770810}, 8.603035793 \times 10^{1770809}]], \\
& [0.39, [5.897136244 \times 10^{3541619}, 4.496679352 \times 10^{3541619}]], [0.40, [1.612212355 \\
& \times 10^{7083239}, 1.228749374 \times 10^{7083239}]], [0.41, [1.204477294 \times 10^{14166478}, 9.176494365 \\
& \times 10^{14166477}]], [0.42, [6.720585027 \times 10^{28332955}, 5.118688890 \times 10^{28332955}]], [0.43, \\
& [2.091760424 \times 10^{56665911}, 1.592814844 \times 10^{56665911}]], [0.44, [2.025977490 \times 10^{113331822}, \\
& 1.542451767 \times 10^{113331822}]], [0.45, [1.900256982 \times 10^{226663644}, 1.446538411 \\
& \times 10^{226663644}]], [0.46, [1.671534091 \times 10^{453327288}, 1.272291897 \times 10^{453327288}]], [0.47, \\
& [1.293243248 \times 10^{906654576}, 9.842737704 \times 10^{906654575}]], [0.48, [7.740668385 \\
& \times 10^{1813309151}, 5.890963231 \times 10^{1813309151}]], [0.49, [2.773002754 \times 10^{3626618303}, \\
& 2.110262661 \times 10^{3626618303}]], [0.50, [3.558564365 \times 10^{7253236606}, 2.707972354 \\
& \times 10^{7253236606}]], [0.51, [5.860153503 \times 10^{14506473212}, 4.459286004 \times 10^{14506473212}]], [0.52, \\
& [1.589153178 \times 10^{29012946425}, 1.209238435 \times 10^{29012946425}]], [0.53, [1.168611916 \\
& \times 10^{58025892850}, 8.892187301 \times 10^{58025892849}]], [0.54, [6.319350230 \times 10^{116051785699}, \\
& 4.808444256 \times 10^{116051785699}]], [0.55, [1.847869208 \times 10^{232103571399}, 1.406043069 \\
& \times 10^{232103571399}]], [0.56, [1.580027397 \times 10^{464207142798}, 1.202232073 \times 10^{464207142798}]], \\
& [0.57, [1.155175894 \times 10^{928414285596}, 8.789596375 \times 10^{928414285595}]], [0.58, [6.174653206 \\
& \times 10^{1856828571191}, 4.698196201 \times 10^{1856828571191}]], [0.59, [1.764166203 \times 10^{3713657142383}, \\
& 1.342320859 \times 10^{3713657142383}]], [0.60, [1.440097227 \times 10^{7427314284766}, 1.095739468 \\
& \times 10^{7427314284766}]], [0.61, [9.596110751 \times 10^{14854628569531}, 7.301459706 \\
& \times 10^{14854628569531}]], [0.62, [4.260898585 \times 10^{29709257139063}, 3.242013531 \\
& \times 10^{29709257139063}]], [0.63, [8.400639875 \times 10^{59418514278126}, 6.391832111 \\
& \times 10^{59418514278126}]], [0.64, [3.265383141 \times 10^{118837028556253}, 2.484543732 \\
& \times 10^{118837028556253}]], [0.65, [4.933751459 \times 10^{237674057112506}, 3.753957781 \\
& \times 10^{237674057112506}]], [0.66, [1.126323569 \times 10^{475348114225013}, 8.569884935 \\
& \times 10^{475348114225012}]], [0.67, [5.869954261 \times 10^{950696228450025}, 4.466283686
\end{aligned}$$

$$\begin{aligned}
& \times 10^{950696228450025}]], [0.68, [1.594327741 \times 10^{1901392456900051}, 1.213078794 \\
& \times 10^{1901392456900051}]], [0.69, [1.176151360 \times 10^{3802784913800102}, 8.948999495 \\
& \times 10^{3802784913800101}]], [0.70, [6.400800868 \times 10^{7605569827600203}, 4.870185195 \\
& \times 10^{7605569827600203}]], [0.71, [1.895729737 \times 10^{15211139655200407}, 1.442405926 \\
& \times 10^{15211139655200407}]], [0.72, [1.662878661 \times 10^{30422279310400814}, 1.265236086 \\
& \times 10^{30422279310400814}]], [0.73, [1.279466082 \times 10^{60844558620801628}, 9.735084740 \\
& \times 10^{60844558620801627}]], [0.74, [7.574695285 \times 10^{121689117241603255}, 5.763364486 \\
& \times 10^{121689117241603255}]], [0.75, [2.654837298 \times 10^{243378234483206511}, 2.019988044 \\
& \times 10^{243378234483206511}]], [0.76, [3.261244583 \times 10^{486756468966413022}, 2.481385472 \\
& \times 10^{486756468966413022}]], [0.77, [4.921236878 \times 10^{973512937932826044}, 3.744424822 \\
& \times 10^{973512937932826044}]], [0.78, [1.120614020 \times 10^{1947025875865652089}, 8.526423165 \\
& \times 10^{1947025875865652088}]], [0.79, [5.810581569 \times 10^{3894051751731304177}, 4.421100856 \\
& \times 10^{3894051751731304177}]], [0.80, [1.562236188 \times 10^{7788103503462608355}, 1.188659608 \\
& \times 10^{7788103503462608355}]], [0.81, [Float(\infty), Float(\infty)]], [0.82, [Float(\infty), Float(\infty)]], \\
[0.83, [Float(\infty), Float(\infty)]], [0.84, [Float(\infty), Float(\infty)]], [0.85, [Float(\infty), \\
Float(\infty)]], [0.86, [Float(\infty), Float(\infty)]], [0.87, [Float(\infty), Float(\infty)]], [0.88, [ \\
Float(\infty), Float(\infty)]], [0.89, [Float(\infty), Float(\infty)]], [0.90, [Float(\infty), Float(\infty)]], \\
[0.91, [Float(\infty), Float(\infty)]], [0.92, [Float(\infty), Float(\infty)]], [0.93, [Float(\infty), \\
Float(\infty)]], [0.94, [Float(\infty), Float(\infty)]], [0.95, [Float(\infty), Float(\infty)]], [0.96, [ \\
Float(\infty), Float(\infty)]], [0.97, [Float(\infty), Float(\infty)]], [0.98, [Float(\infty), Float(\infty)]], \\
[0.99, [Float(\infty), Float(\infty)]], [1.00, [Float(\infty), Float(\infty)]], [1.01, [Float(\infty), \\
Float(\infty)]], [1.02, [Float(\infty), Float(\infty)]], [1.03, [Float(\infty), Float(\infty)]], [1.04, [ \\
Float(\infty), Float(\infty)]], [1.05, [Float(\infty), Float(\infty)]], [1.06, [Float(\infty), Float(\infty)]], \\
[1.07, [Float(\infty), Float(\infty)]], [1.08, [Float(\infty), Float(\infty)]], [1.09, [Float(\infty), \\
Float(\infty)]], [1.10, [Float(\infty), Float(\infty)]], [1.11, [Float(\infty), Float(\infty)]], [1.12, [ \\
Float(\infty), Float(\infty)]], [1.13, [Float(\infty), Float(\infty)]], [1.14, [Float(\infty), Float(\infty)]], \\
[1.15, [Float(\infty), Float(\infty)]], [1.16, [Float(\infty), Float(\infty)]], [1.17, [Float(\infty), \\
Float(\infty)]], [1.18, [Float(\infty), Float(\infty)]], [1.19, [Float(\infty), Float(\infty)]], [1.20, [ \\
Float(\infty), Float(\infty)]], [1.21, [Float(\infty), Float(\infty)]], [1.22, [Float(\infty), Float(\infty)]], \\
[1.23, [Float(\infty), Float(\infty)]], [1.24, [Float(\infty), Float(\infty)]], [1.25, [Float(\infty), \\
Float(\infty)]], [1.26, [Float(\infty), Float(\infty)]], [1.27, [Float(\infty), Float(\infty)]], [1.28, [ \\
Float(\infty), Float(\infty)]], [1.29, [Float(\infty), Float(\infty)]], [1.30, [Float(\infty), Float(\infty)]], \\
[1.31, [Float(\infty), Float(\infty)]], [1.32, [Float(\infty), Float(\infty)]], [1.33, [Float(\infty), \\
Float(\infty)]], [1.34, [Float(\infty), Float(\infty)]], [1.35, [Float(\infty), Float(\infty)]], [1.36, [ \\
Float(\infty), Float(\infty)]], [1.37, [Float(\infty), Float(\infty)]], [1.38, [Float(\infty), Float(\infty)]]]
\end{aligned}$$

















Float(∞)], [9.50, [Float(∞), Float(∞)]], [9.51, [Float(∞), Float(∞)]], [9.52, [Float(∞), Float(∞)]], [9.53, [Float(∞), Float(∞)]], [9.54, [Float(∞), Float(∞)]], [9.55, [Float(∞), Float(∞)]], [9.56, [Float(∞), Float(∞)]], [9.57, [Float(∞), Float(∞)]], [9.58, [Float(∞), Float(∞)]], [9.59, [Float(∞), Float(∞)]], [9.60, [Float(∞), Float(∞)]], [9.61, [Float(∞), Float(∞)]], [9.62, [Float(∞), Float(∞)]], [9.63, [Float(∞), Float(∞)]], [9.64, [Float(∞), Float(∞)]], [9.65, [Float(∞), Float(∞)]], [9.66, [Float(∞), Float(∞)]], [9.67, [Float(∞), Float(∞)]], [9.68, [Float(∞), Float(∞)]], [9.69, [Float(∞), Float(∞)]], [9.70, [Float(∞), Float(∞)]], [9.71, [Float(∞), Float(∞)]], [9.72, [Float(∞), Float(∞)]], [9.73, [Float(∞), Float(∞)]], [9.74, [Float(∞), Float(∞)]], [9.75, [Float(∞), Float(∞)]], [9.76, [Float(∞), Float(∞)]], [9.77, [Float(∞), Float(∞)]], [9.78, [Float(∞), Float(∞)]], [9.79, [Float(∞), Float(∞)]], [9.80, [Float(∞), Float(∞)]], [9.81, [Float(∞), Float(∞)]], [9.82, [Float(∞), Float(∞)]], [9.83, [Float(∞), Float(∞)]], [9.84, [Float(∞), Float(∞)]], [9.85, [Float(∞), Float(∞)]], [9.86, [Float(∞), Float(∞)]], [9.87, [Float(∞), Float(∞)]], [9.88, [Float(∞), Float(∞)]], [9.89, [Float(∞), Float(∞)]], [9.90, [Float(∞), Float(∞)]], [9.91, [Float(∞), Float(∞)]], [9.92, [Float(∞), Float(∞)]], [9.93, [Float(∞), Float(∞)]], [9.94, [Float(∞), Float(∞)]], [9.95, [Float(∞), Float(∞)]], [9.96, [Float(∞), Float(∞)]], [9.97, [Float(∞), Float(∞)]], [9.98, [Float(∞), Float(∞)]], [9.99, [Float(∞), Float(∞)]], [10.00, [Float(∞), Float(∞)]], [10.01, [Float(∞), Float(∞)]]]

$$\text{for unstable equilibrium point, } \left[ -\frac{4}{3}, \frac{14}{9} \right]$$

[[0.01, [-1.323333333, 1.565555556]], [0.02, [-1.326051111, 1.569500445]], [0.03, [-1.329116321, 1.574648714]], [0.04, [-1.332684939, 1.581411134]], [0.05, [-1.336960713, 1.590348640]], [0.06, [-1.342212217, 1.602236973]], [0.07, [-1.348796489, 1.618166325]], [0.08, [-1.357192127, 1.639700493]], [0.09, [-1.368045912, 1.669141777]], [0.10, [-1.382238316, 1.709993619]], [0.11, [-1.400972966, 1.767815552]], [0.12, [-1.425886183, 1.851913252]], [0.13, [-1.459124968, 1.978964960]], [0.14, [-1.503120752, 2.181642982]], [0.15, [-1.558723228, 2.532009100]], [0.16, [-1.614516507, 3.217323041]], [0.17, [-1.579796474, 4.855488846]], [0.18, [-0.7125891290, 10.41026619]], [0.19, [11.26140272, 47.04519994]], [0.20, [512.4926944, 1008.084558]], [0.21, [349541.1949, 496748.0816]], [0.22, [1.079455430 × 10<sup>11</sup>, 1.274328929 × 10<sup>11</sup>]], [0.23, [8.331486942 × 10<sup>21</sup>, 8.725217790 × 10<sup>21</sup>]], [0.24, [4.367248006 × 10<sup>43</sup>, 4.211872040 × 10<sup>43</sup>]], [0.25, [1.103340946 × 10<sup>87</sup>, 1.003272998 × 10<sup>87</sup>]], [0.26, [6.645692556 × 10<sup>173</sup>, 5.788312132 × 10<sup>173</sup>]], [0.27, [2.313369202 × 10<sup>347</sup>, 1.951432095 × 10<sup>347</sup>]], [0.28, [2.719906573

$$\begin{aligned}
& \times 10^{694}, 2.239783180 \times 10^{694}]], [0.29, [3.676719460 \times 10^{1388}, 2.972923097 \times 10^{1388}]], \\
& [0.30, [6.606785301 \times 10^{2776}, 5.268235337 \times 10^{2776}]], [0.31, [2.106398215 \times 10^{5553}, \\
& 1.661809659 \times 10^{5553}]], [0.32, [2.120543782 \times 10^{1106}, 1.659302174 \times 10^{1106}]], [0.33, \\
& [2.133304487 \times 10^{22212}, 1.658767194 \times 10^{22212}]], [0.34, [2.146847820 \times 10^{44424}, \\
& 1.661168709 \times 10^{44424}]], [0.35, [2.164721691 \times 10^{88848}, 1.668687711 \times 10^{88848}]], [0.36, \\
& [2.193516392 \times 10^{177696}, 1.685949828 \times 10^{177696}]], [0.37, [2.246405167 \times 10^{355392}, \\
& 1.722695023 \times 10^{355392}]], [0.38, [2.351298796 \times 10^{710784}, 1.799971413 \times 10^{710784}]], [0.39, \\
& [2.571993298 \times 10^{1421568}, 1.966238018 \times 10^{1421568}]], [0.40, [3.073751537 \times 10^{2843136}, \\
& 2.347339744 \times 10^{2843136}]], [0.41, [4.385906509 \times 10^{5686272}, 3.346649202 \times 10^{5686272}]], \\
& [0.42, [8.923281822 \times 10^{11372544}, 6.804539096 \times 10^{11372544}]], [0.43, [3.691559124 \\
& \times 10^{22745089}, 2.813643216 \times 10^{22745089}]], [0.44, [6.315239840 \times 10^{45490178}, 4.811518045 \\
& \times 10^{45490178}]], [0.45, [1.847574752 \times 10^{90980357}, 1.407228478 \times 10^{90980357}]], [0.46, \\
& [1.580925883 \times 10^{181960714}, 1.203852735 \times 10^{181960714}]], [0.47, [1.157287546 \times 10^{363921428}, \\
& 8.810993111 \times 10^{363921427}]], [0.48, [6.200568549 \times 10^{727842855}, 4.720133468 \\
& \times 10^{727842855}]], [0.49, [1.779746449 \times 10^{1455685711}, 1.354670413 \times 10^{1455685711}]], [0.50, \\
& [1.466120083 \times 10^{2911371422}, 1.115856465 \times 10^{2911371422}]], [0.51, [9.948551485 \\
& \times 10^{5822742843}, 7.571293987 \times 10^{5822742843}]], [0.52, [4.580524510 \times 10^{11645485687}, \\
& 3.485806672 \times 10^{11645485687}]], [0.53, [9.709710994 \times 10^{23290971374}, 7.388855248 \\
& \times 10^{23290971374}]], [0.54, [4.362879674 \times 10^{46581942749}, 3.319943564 \times 10^{46581942749}]], \\
& [0.55, [8.808363889 \times 10^{93163885498}, 6.702584659 \times 10^{93163885498}]], [0.56, [3.590294404 \\
& \times 10^{186327770997}, 2.731926662 \times 10^{186327770997}]], [0.57, [5.964753951 \times 10^{372655541994}, \\
& 4.538634647 \times 10^{372655541994}]], [0.58, [1.646311130 \times 10^{745311083989}, 1.252678783 \\
& \times 10^{745311083989}]], [0.59, [1.254140964 \times 10^{1490622167978}, 9.542680123 \times 10^{1490622167977}]], \\
& [0.60, [7.277997015 \times 10^{2981244335955}, 5.537744787 \times 10^{2981244335955}]], [0.61, [2.450983018 \\
& \times 10^{5962488671911}, 1.864915139 \times 10^{5962488671911}]], [0.62, [2.779682110 \times 10^{11924977343822}, \\
& 2.115008531 \times 10^{11924977343822}]], [0.63, [3.575223658 \times 10^{23849954687644}, 2.720312663 \\
& \times 10^{23849954687644}]], [0.64, [5.914501655 \times 10^{47699909375288}, 4.500209061 \\
& \times 10^{47699909375288}]], [0.65, [1.618628153 \times 10^{95399818750577}, 1.231574778 \\
& \times 10^{95399818750577}]], [0.66, [1.212283557 \times 10^{190799637501154}, 9.223956823 \\
& \times 10^{190799637501153}]], [0.67, [6.800140552 \times 10^{381599275002307}, 5.174047735 \\
& \times 10^{381599275002307}]], [0.68, [2.139660117 \times 10^{76319855004615}, 1.628009523 \\
& \times 10^{76319855004615}]], [0.69, [2.118352594 \times 10^{1526397100009230}, 1.611796074
\end{aligned}$$

$$\begin{aligned}
& \times 10^{1526397100009230}], [0.70, [2.076370710 \times 10^{3052794200018460}, 1.579852354 \\
& \times 10^{3052794200018460}], [0.71, [1.994885502 \times 10^{6105588400036920}, 1.517851896 \\
& \times 10^{6105588400036920}], [0.72, [1.841382330 \times 10^{12211176800073840}, 1.401055217 \\
& \times 10^{12211176800073840}], [0.73, [1.568902082 \times 10^{24422353600147680}, 1.193732473 \\
& \times 10^{24422353600147680}], [0.74, [1.138936409 \times 10^{48844707200295360}, 8.665837857 \\
& \times 10^{48844707200295359}], [0.75, [6.002147644 \times 10^{97689414400590719}, 4.566859909 \\
& \times 10^{97689414400590719}], [0.76, [1.666944001 \times 10^{195378828801181439}, 1.268329149 \\
& \times 10^{195378828801181439}], [0.77, [1.285729584 \times 10^{390757657602362878}, 9.782741079 \\
& \times 10^{390757657602362877}], [0.78, [7.649038617 \times 10^{781515315204725755}, 5.819929773 \\
& \times 10^{781515315204725755}], [0.79, [2.707205718 \times 10^{1563030630409451511}, 2.059833538 \\
& \times 10^{1563030630409451511}], [0.80, [3.391173794 \times 10^{3126061260818903022}, 2.580244703 \\
& \times 10^{3126061260818903022}], [0.81, [5.321175817 \times 10^{6252122521637806044}, 4.048726510 \\
& \times 10^{6252122521637806044}], [0.82, [Float(\infty), Float(\infty)]], [0.83, [Float(\infty), Float(\infty)]], \\
[0.84, [Float(\infty), Float(\infty)]], [0.85, [Float(\infty), Float(\infty)]], [0.86, [Float(\infty), \\
Float(\infty)]], [0.87, [Float(\infty), Float(\infty)]], [0.88, [Float(\infty), Float(\infty)]], [0.89, [ \\
Float(\infty), Float(\infty)]], [0.90, [Float(\infty), Float(\infty)]], [0.91, [Float(\infty), Float(\infty)]], \\
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Float(\infty), Float(\infty)]], [0.98, [Float(\infty), Float(\infty)]], [0.99, [Float(\infty), Float(\infty)]], \\
[1.00, [Float(\infty), Float(\infty)]], [1.01, [Float(\infty), Float(\infty)]], [1.02, [Float(\infty), \\
Float(\infty)]], [1.03, [Float(\infty), Float(\infty)]], [1.04, [Float(\infty), Float(\infty)]], [1.05, [ \\
Float(\infty), Float(\infty)]], [1.06, [Float(\infty), Float(\infty)]], [1.07, [Float(\infty), Float(\infty)]], \\
[1.08, [Float(\infty), Float(\infty)]], [1.09, [Float(\infty), Float(\infty)]], [1.10, [Float(\infty), \\
Float(\infty)]], [1.11, [Float(\infty), Float(\infty)]], [1.12, [Float(\infty), Float(\infty)]], [1.13, [ \\
Float(\infty), Float(\infty)]], [1.14, [Float(\infty), Float(\infty)]], [1.15, [Float(\infty), Float(\infty)]], \\
[1.16, [Float(\infty), Float(\infty)]], [1.17, [Float(\infty), Float(\infty)]], [1.18, [Float(\infty), \\
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Float(\infty), Float(\infty)]], [1.22, [Float(\infty), Float(\infty)]], [1.23, [Float(\infty), Float(\infty)]], \\
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\end{aligned}$$

















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$$\text{for unstable equilibrium point, } \left[ \frac{2}{11}, \frac{6}{11} \right]$$

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[8.040149217, 0.2036302380]], [10.00, [15.87043487, 0.2726018257]], [10.01,
[49.01316792, 1.582406386]]]
```

Analyzing F3:

```
> #Stable equilibrium of f3
if nops(s3)=0 then print(`no stable equilibra`);
end if;
for i in s3 do:
print(`for stable equilibrium point`, i);
print(Dis2(F3,x,y,i+[0.01,0.01],0.01,10));
od:
```

$$for stable equilibrium point, \left[ \frac{1}{18}, \frac{7}{18} \right]$$

(13)

$$[[0.01, [0.0655555556, 0.3988888889]], [0.02, [0.0659522223, 0.3964755556]], [0.03, [0.06626726348, 0.3943544354]], [0.04, [0.06651211765, 0.3924951533]], [0.05, [0.06669662342, 0.3908698545]], [0.06, [0.06682924961, 0.3894531294]], [0.07,$$

[0.06691729222, 0.3882219080]], [0.08, [0.06696704292, 0.3871553314]], [0.09, [0.06698393282, 0.3862346097]], [0.10, [0.06697265497, 0.3854428723]], [0.11, [0.06693726878, 0.3847650158]], [0.12, [0.06688128886, 0.3841875535]], [0.13, [0.06680776085, 0.3836984702]], [0.14, [0.06671932608, 0.3832870827]], [0.15, [0.06661827681, 0.3829439095]], [0.16, [0.06650660349, 0.3826605488]], [0.17, [0.06638603525, 0.3824295663]], [0.18, [0.06625807471, 0.3822443918]], [0.19, [0.06612402785, 0.3820992255]], [0.20, [0.06598502978, 0.3819889526]], [0.21, [0.06584206699, 0.3819090668]], [0.22, [0.06569599655, 0.3818556009]], [0.23, [0.06554756274, 0.3818250653]], [0.24, [0.06539741151, 0.3818143923]], [0.25, [0.06524610298, 0.3818208871]], [0.26, [0.06509412232, 0.3818421839]], [0.27, [0.06494188924, 0.3818762070]], [0.28, [0.06478976625, 0.3819211361]], [0.29, [0.06463806585, 0.3819753761]], [0.30, [0.06448705682, 0.3820375298]], [0.31, [0.06433696971, 0.3821063743]], [0.32, [0.06418800164, 0.3821808396]], [0.33, [0.06404032046, 0.3822599905]], [0.34, [0.06389406848, 0.3823430098]], [0.35, [0.06374936564, 0.3824291843]], [0.36, [0.06360631235, 0.3825178919]], [0.37, [0.06346499191, 0.3826085904]], [0.38, [0.06332547274, 0.3827008079]], [0.39, [0.06318781023, 0.3827941340]], [0.40, [0.06305204838, 0.3828882124]], [0.41, [0.06291822131, 0.3829827340]], [0.42, [0.06278635450, 0.3830774312]], [0.43, [0.06265646591, 0.3831720730]], [0.44, [0.06252856699, 0.3832664600]], [0.45, [0.06240266350, 0.3833604208]], [0.46, [0.06227875629, 0.3834538085]], [0.47, [0.06215684194, 0.3835464976]], [0.48, [0.06203691340, 0.3836383811]], [0.49, [0.06191896042, 0.3837293687]], [0.50, [0.06180297006, 0.3838193841]], [0.51, [0.06168892703, 0.3839083638]], [0.52, [0.06157681407, 0.3839962549]], [0.53, [0.06146661224, 0.3840830144]], [0.54, [0.06135830119, 0.3841686073]], [0.55, [0.06125185936, 0.3842530061]], [0.56, [0.06114726422, 0.3843361894]], [0.57, [0.06104449243, 0.3844181415]], [0.58, [0.06094352000, 0.3844988513]], [0.59, [0.06084432239, 0.3845783120]], [0.60, [0.06074687470, 0.3846565202]], [0.61, [0.06065115170, 0.3847334758]], [0.62, [0.06055712796, 0.3848091814]], [0.63, [0.06046477791, 0.3848836417]], [0.64, [0.06037407593, 0.3849568636]], [0.65, [0.06028499638, 0.3850288556]], [0.66, [0.06019751368, 0.3850996276]], [0.67, [0.06011160233, 0.3851691909]], [0.68, [0.06002723696, 0.3852375577]], [0.69, [0.05994439237, 0.3853047412]], [0.70, [0.05986304353, 0.3853707552]], [0.71, [0.05978316565, 0.3854356142]], [0.72, [0.05970473415, 0.3854993331]], [0.73, [0.05962772471, 0.3855619273]], [0.74, [0.05955211327, 0.3856234125]], [0.75, [0.05947787606, 0.3856838045]], [0.76, [0.05940498959, 0.3857431195]], [0.77, [0.05933343069, 0.3858013736]], [0.78, [0.05926317645, 0.3858585831]], [0.79, [0.05919420430, 0.3859147642]], [0.80, [0.05912649197, 0.3859699333]], [0.81, [0.05906001752, 0.3860241065]], [0.82, [0.05899475931, 0.3860773001]], [0.83,

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[0.05555555507, 0.3888888890]]]
```

```
> #unstable equilibrium points of f3:
for i in alleged_unstable3 do:
print(`for unstable equilibrium point`, i);
print(Dis2(F3,x,y,i+[0.01,0.01],0.01,10));
od:
```

$$\text{for unstable equilibrium point, } \left[ \frac{3}{5}, \frac{1}{10} \right]$$

```
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& \times 10^{353907499469227828}], [2.77, [6.324690356 \times 10^{707814998938455655}, 1.547627077 \\
& \times 10^{707814998938455656}], [2.78, [5.711244432 \times 10^{1415629997876911311}, 1.397519251 \\
& \times 10^{1415629997876911312}], [2.79, [4.657080090 \times 10^{2831259995753822623}, 1.139569345 \\
& \times 10^{2831259995753822624}], [2.80, [3.096560893 \times 10^{5662519991507645247}, 7.577163806 \\
& \times 10^{5662519991507645247}], [2.81, [Float(\infty), Float(\infty)]], [2.82, [Float(\infty), Float(\infty)]], \\
& [2.83, [Float(\infty), Float(\infty)]], [2.84, [Float(\infty), Float(\infty)]], [2.85, [Float(\infty), \\
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& \text{Float}(\infty), \text{Float}(\infty)]], [2.89, [Float(\infty), \text{Float}(\infty)]], [2.90, [Float(\infty), \text{Float}(\infty)]], \\
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& \text{Float}(\infty)]], [3.02, [Float(\infty), \text{Float}(\infty)]], [3.03, [Float(\infty), \text{Float}(\infty)]], [3.04, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [3.05, [Float(\infty), \text{Float}(\infty)]], [3.06, [Float(\infty), \text{Float}(\infty)]], \\
& [3.07, [Float(\infty), \text{Float}(\infty)]], [3.08, [Float(\infty), \text{Float}(\infty)]], [3.09, [Float(\infty), \\
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& \text{Float}(\infty), \text{Float}(\infty)]], [3.13, [Float(\infty), \text{Float}(\infty)]], [3.14, [Float(\infty), \text{Float}(\infty)]], \\
& [3.15, [Float(\infty), \text{Float}(\infty)]], [3.16, [Float(\infty), \text{Float}(\infty)]], [3.17, [Float(\infty), \\
& \text{Float}(\infty)]], [3.18, [Float(\infty), \text{Float}(\infty)]], [3.19, [Float(\infty), \text{Float}(\infty)]], [3.20, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [3.21, [Float(\infty), \text{Float}(\infty)]], [3.22, [Float(\infty), \text{Float}(\infty)]], \\
& [3.23, [Float(\infty), \text{Float}(\infty)]], [3.24, [Float(\infty), \text{Float}(\infty)]], [3.25, [Float(\infty), \\
& \text{Float}(\infty)]], [3.26, [Float(\infty), \text{Float}(\infty)]], [3.27, [Float(\infty), \text{Float}(\infty)]], [3.28, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [3.29, [Float(\infty), \text{Float}(\infty)]], [3.30, [Float(\infty), \text{Float}(\infty)]], \\
& [3.31, [Float(\infty), \text{Float}(\infty)]], [3.32, [Float(\infty), \text{Float}(\infty)]], [3.33, [Float(\infty), \\
& \text{Float}(\infty)]], [3.34, [Float(\infty), \text{Float}(\infty)]], [3.35, [Float(\infty), \text{Float}(\infty)]], [3.36, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [3.37, [Float(\infty), \text{Float}(\infty)]], [3.38, [Float(\infty), \text{Float}(\infty)]], \\
& [3.39, [Float(\infty), \text{Float}(\infty)]], [3.40, [Float(\infty), \text{Float}(\infty)]], [3.41, [Float(\infty), \\
& \text{Float}(\infty)]], [3.42, [Float(\infty), \text{Float}(\infty)]], [3.43, [Float(\infty), \text{Float}(\infty)]], [3.44, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [3.45, [Float(\infty), \text{Float}(\infty)]], [3.46, [Float(\infty), \text{Float}(\infty)]], \\
& [3.47, [Float(\infty), \text{Float}(\infty)]], [3.48, [Float(\infty), \text{Float}(\infty)]], [3.49, [Float(\infty), \\
& \text{Float}(\infty)]], [3.50, [Float(\infty), \text{Float}(\infty)]], [3.51, [Float(\infty), \text{Float}(\infty)]], [3.52, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [3.53, [Float(\infty), \text{Float}(\infty)]], [3.54, [Float(\infty), \text{Float}(\infty)]], \\
& [3.55, [Float(\infty), \text{Float}(\infty)]], [3.56, [Float(\infty), \text{Float}(\infty)]], [3.57, [Float(\infty), \\
& \text{Float}(\infty)]], [3.58, [Float(\infty), \text{Float}(\infty)]], [3.59, [Float(\infty), \text{Float}(\infty)]], [3.60, [ \\
& \text{Float}(\infty), \text{Float}(\infty)]], [3.61, [Float(\infty), \text{Float}(\infty)]], [3.62, [Float(\infty), \text{Float}(\infty)]], \\
& [3.63, [Float(\infty), \text{Float}(\infty)]], [3.64, [Float(\infty), \text{Float}(\infty)]], [3.65, [Float(\infty),
\end{aligned}$$













$\text{Float}(\infty)]], [9.74, [\text{Float}(\infty), \text{Float}(\infty)]], [9.75, [\text{Float}(\infty), \text{Float}(\infty)]], [9.76, [\text{Float}(\infty), \text{Float}(\infty)]], [9.77, [\text{Float}(\infty), \text{Float}(\infty)]], [9.78, [\text{Float}(\infty), \text{Float}(\infty)]], [9.79, [\text{Float}(\infty), \text{Float}(\infty)]], [9.80, [\text{Float}(\infty), \text{Float}(\infty)]], [9.81, [\text{Float}(\infty), \text{Float}(\infty)]], [9.82, [\text{Float}(\infty), \text{Float}(\infty)]], [9.83, [\text{Float}(\infty), \text{Float}(\infty)]], [9.84, [\text{Float}(\infty), \text{Float}(\infty)]], [9.85, [\text{Float}(\infty), \text{Float}(\infty)]], [9.86, [\text{Float}(\infty), \text{Float}(\infty)]], [9.87, [\text{Float}(\infty), \text{Float}(\infty)]], [9.88, [\text{Float}(\infty), \text{Float}(\infty)]], [9.89, [\text{Float}(\infty), \text{Float}(\infty)]], [9.90, [\text{Float}(\infty), \text{Float}(\infty)]], [9.91, [\text{Float}(\infty), \text{Float}(\infty)]], [9.92, [\text{Float}(\infty), \text{Float}(\infty)]], [9.93, [\text{Float}(\infty), \text{Float}(\infty)]], [9.94, [\text{Float}(\infty), \text{Float}(\infty)]], [9.95, [\text{Float}(\infty), \text{Float}(\infty)]], [9.96, [\text{Float}(\infty), \text{Float}(\infty)]], [9.97, [\text{Float}(\infty), \text{Float}(\infty)]], [9.98, [\text{Float}(\infty), \text{Float}(\infty)]], [9.99, [\text{Float}(\infty), \text{Float}(\infty)]], [10.00, [\text{Float}(\infty), \text{Float}(\infty)]], [10.01, [\text{Float}(\infty), \text{Float}(\infty)]]]$

$$\text{for unstable equilibrium point, } \left[ \frac{5}{13}, \frac{2}{13} \right]$$

$[[0.01, [0.3946153846, 0.1638461538]], [0.02, [0.3942223077, 0.1626738461]], [0.03, [0.3938663761, 0.1615931661]], [0.04, [0.3935452010, 0.1605979429]], [0.05, [0.3932564600, 0.1596821936]], [0.06, [0.3929979129, 0.1588401608]], [0.07, [0.3927674142, 0.1580663406]], [0.08, [0.3925629212, 0.1573555014]], [0.09, [0.3923824998, 0.1567026959]], [0.10, [0.3922243272, 0.1561032665]], [0.11, [0.3920866928, 0.1555528459]], [0.12, [0.3919679975, 0.1550473538]], [0.13, [0.3918667511, 0.1545829900]], [0.14, [0.3917815696, 0.1541562251]], [0.15, [0.3917111707, 0.1537637898]], [0.16, [0.3916543694, 0.1534026626]], [0.17, [0.3916100731, 0.1530700566]], [0.18, [0.3915772763, 0.1527634060]], [0.19, [0.3915550556, 0.1524803525]], [0.20, [0.3915425641, 0.1522187318]], [0.21, [0.3915390264, 0.1519765602]], [0.22, [0.3915437337, 0.1517520215]], [0.23, [0.3915560388, 0.1515434549]], [0.24, [0.3915753515, 0.1513493429]], [0.25, [0.3916011341, 0.1511683003]], [0.26, [0.3916328975, 0.1509990634]], [0.27, [0.3916701971, 0.1508404802]], [0.28, [0.3917126291, 0.1506915011]], [0.29, [0.3917598274, 0.1505511704]], [0.30, [0.3918114601, 0.1504186182]], [0.31, [0.3918672267, 0.1502930530]], [0.32, [0.3919268556, 0.1501737547]], [0.33, [0.3919901012, 0.1500600686]], [0.34, [0.3920567420, 0.1499513994]], [0.35, [0.3921265783, 0.1498472060]], [0.36, [0.3921994302, 0.1497469964]], [0.37, [0.3922751361, 0.1496503236]], [0.38, [0.3923535507, 0.1495567812]], [0.39, [0.3924345439, 0.1494659999]], [0.40, [0.3925179993, 0.1493776438]], [0.41, [0.3926038128, 0.1492914076]], [0.42, [0.3926918917, 0.1492070137]], [0.43,$

[0.3927821536, 0.1491242095]], [0.44, [0.3928745255, 0.1490427652]], [0.45, [0.3929689429, 0.1489624716]], [0.46, [0.3930653490, 0.1488831382]], [0.47, [0.3931636943, 0.1488045914]], [0.48, [0.3932639354, 0.1487266729]], [0.49, [0.3933660350, 0.1486492384]], [0.50, [0.3934699611, 0.1485721560]], [0.51, [0.3935756864, 0.1484953053]], [0.52, [0.3936831882, 0.1484185761]], [0.53, [0.3937924478, 0.1483418675]], [0.54, [0.3939034501, 0.1482650870]], [0.55, [0.3940161834, 0.1481881498]], [0.56, [0.3941306391, 0.1481109779]], [0.57, [0.3942468115, 0.1480334995]], [0.58, [0.3943646973, 0.1479556484]], [0.59, [0.3944842956, 0.1478773635]], [0.60, [0.3946056078, 0.1477985882]], [0.61, [0.3947286371, 0.1477192701]], [0.62, [0.3948533887, 0.1476393604]], [0.63, [0.3949798695, 0.1475588138]], [0.64, [0.3951080878, 0.1474775879]], [0.65, [0.3952380534, 0.1473956430]], [0.66, [0.3953697775, 0.1473129419]], [0.67, [0.3955032726, 0.1472294495]], [0.68, [0.3956385522, 0.1471451328]], [0.69, [0.3957756309, 0.1470599604]], [0.70, [0.3959145244, 0.1469739026]], [0.71, [0.3960552493, 0.1468869310]], [0.72, [0.3961978231, 0.1467990186]], [0.73, [0.3963422642, 0.1467101394]], [0.74, [0.3964885917, 0.1466202684]], [0.75, [0.3966368254, 0.1465293816]], [0.76, [0.3967869861, 0.1464374556]], [0.77, [0.3969390950, 0.1463444678]], [0.78, [0.3970931741, 0.1462503962]], [0.79, [0.3972492460, 0.1461552193]], [0.80, [0.3974073339, 0.1460589160]], [0.81, [0.3975674617, 0.1459614657]], [0.82, [0.3977296537, 0.1458628481]], [0.83, [0.3978939349, 0.1457630431]], [0.84, [0.3980603308, 0.1456620308]], [0.85, [0.3982288674, 0.1455597917]], [0.86, [0.3983995713, 0.1454563063]], [0.87, [0.3985724696, 0.1453515552]], [0.88, [0.3987475899, 0.1452455192]], [0.89, [0.3989249603, 0.1451381790]], [0.90, [0.3991046095, 0.1450295154]], [0.91, [0.3992865665, 0.1449195091]], [0.92, [0.3994708610, 0.1448081410]], [0.93, [0.3996575230, 0.1446953917]], [0.94, [0.3998465832, 0.1445812419]], [0.95, [0.4000380727, 0.1444656722]], [0.96, [0.4002320230, 0.1443486629]], [0.97, [0.4004284663, 0.1442301945]], [0.98, [0.4006274352, 0.1441102471]], [0.99, [0.4008289628, 0.1439888007]], [1.00, [0.4010330827, 0.1438658353]], [1.01, [0.4012398290, 0.1437413306]], [1.02, [0.4014492364, 0.1436152662]], [1.03, [0.4016613400, 0.1434876214]], [1.04, [0.4018761756, 0.1433583753]], [1.05, [0.4020937793, 0.1432275069]], [1.06, [0.4023141879, 0.1430949950]], [1.07,

[0.4025374387, 0.1429608180]], [1.08, [0.4027635695, 0.1428249542]], [1.09, [0.4029926188, 0.1426873817]], [1.10, [0.4032246254, 0.1425480782]], [1.11, [0.4034596290, 0.1424070213]], [1.12, [0.4036976696, 0.1422641882]], [1.13, [0.4039387879, 0.1421195560]], [1.14, [0.4041830252, 0.1419731013]], [1.15, [0.4044304233, 0.1418248007]], [1.16, [0.4046810248, 0.1416746303]], [1.17, [0.4049348727, 0.1415225660]], [1.18, [0.4051920108, 0.1413685834]], [1.19, [0.4054524834, 0.1412126578]], [1.20, [0.4057163355, 0.1410547641]], [1.21, [0.4059836128, 0.1408948771]], [1.22, [0.4062543616, 0.1407329711]], [1.23, [0.4065286289, 0.1405690202]], [1.24, [0.4068064624, 0.1404029981]], [1.25, [0.4070879104, 0.1402348781]], [1.26, [0.4073730219, 0.1400646334]], [1.27, [0.4076618468, 0.1398922367]], [1.28, [0.4079544355, 0.1397176603]], [1.29, [0.4082508393, 0.1395408763]], [1.30, [0.4085511101, 0.1393618564]], [1.31, [0.4088553007, 0.1391805719]], [1.32, [0.4091634645, 0.1389969938]], [1.33, [0.4094756559, 0.1388110927]], [1.34, [0.4097919299, 0.1386228389]], [1.35, [0.4101123424, 0.1384322021]], [1.36, [0.4104369500, 0.1382391519]], [1.37, [0.4107658103, 0.1380436574]], [1.38, [0.4110989816, 0.1378456873]], [1.39, [0.4114365232, 0.1376452100]], [1.40, [0.4117784951, 0.1374421934]], [1.41, [0.4121249583, 0.1372366050]], [1.42, [0.4124759746, 0.1370284119]], [1.43, [0.4128316067, 0.1368175809]], [1.44, [0.4131919184, 0.1366040782]], [1.45, [0.4135569742, 0.1363878698]], [1.46, [0.4139268397, 0.1361689212]], [1.47, [0.4143015815, 0.1359471974]], [1.48, [0.4146812670, 0.1357226630]], [1.49, [0.4150659647, 0.1354952823]], [1.50, [0.4154557441, 0.1352650190]], [1.51, [0.4158506758, 0.1350318364]], [1.52, [0.4162508312, 0.1347956974]], [1.53, [0.4166562831, 0.1345565644]], [1.54, [0.4170671050, 0.1343143994]], [1.55, [0.4174833718, 0.1340691640]], [1.56, [0.4179051593, 0.1338208192]], [1.57, [0.4183325445, 0.1335693256]], [1.58, [0.4187656056, 0.1333146433]], [1.59, [0.4192044218, 0.1330567321]], [1.60, [0.4196490736, 0.1327955511]], [1.61, [0.4200996426, 0.1325310591]], [1.62, [0.4205562116, 0.1322632144]], [1.63, [0.4210188647, 0.1319919747]], [1.64, [0.4214876872, 0.1317172974]], [1.65, [0.4219627656, 0.1314391393]], [1.66, [0.4224441878, 0.1311574567]], [1.67, [0.4229320429, 0.1308722054]], [1.68, [0.4234264213, 0.1305833409]], [1.69, [0.4239274148, 0.1302908180]], [1.70, [0.4244351165, 0.1299945911]], [1.71,

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$$\begin{aligned}
& \times 10^{67773875340}, 6.375494071 \times 10^{67773875340}], [4.16, [9.692276635 \times 10^{135547750680}, \\
& 2.371662313 \times 10^{135547750681}], [4.17, [1.341231713 \times 10^{271095501362}, 3.281941722 \\
& \times 10^{271095501362}], [4.18, [2.568383306 \times 10^{542191002724}, 6.284733841 \times 10^{542191002724}]], \\
& [4.19, [9.418286311 \times 10^{1084382005448}, 2.304617949 \times 10^{1084382005449}]], [4.20, [1.266473155 \\
& \times 10^{2168764010898}, 3.099010444 \times 10^{2168764010898}]], [4.21, [2.290045909 \times 10^{4337528021796}, \\
& 5.603653073 \times 10^{4337528021796}]], [4.22, [7.487564705 \times 10^{8675056043592}, 1.832177898 \\
& \times 10^{8675056043593}]], [4.23, [8.004484875 \times 10^{17350112087185}, 1.958666249 \\
& \times 10^{17350112087186}]], [4.24, [9.147849019 \times 10^{34700224174371}, 2.238442998 \\
& \times 10^{34700224174372}]], [4.25, [1.194786172 \times 10^{69400448348744}, 2.923595193 \\
& \times 10^{69400448348744}]], [4.26, [2.038133309 \times 10^{138800896697488}, 4.987232764 \\
& \times 10^{138800896697488}]], [4.27, [5.930856073 \times 10^{277601793394976}, 1.451257363 \\
& \times 10^{277601793394977}]], [4.28, [5.022118790 \times 10^{555203586789953}, 1.228892893 \\
& \times 10^{555203586789954}]], [4.29, [3.601025310 \times 10^{1110407173579907}, 8.811568571 \\
& \times 10^{1110407173579907}]], [4.30, [1.851418330 \times 10^{2220814347159815}, 4.530348487 \\
& \times 10^{2220814347159815}]], [4.31, [4.893970303 \times 10^{4441628694319630}, 1.197535457 \\
& \times 10^{4441628694319631}]], [4.32, [3.419596553 \times 10^{8883257388639261}, 8.367619475 \\
& \times 10^{8883257388639261}]], [4.33, [1.669559699 \times 10^{17766514777278523}, 4.085347504 \\
& \times 10^{17766514777278523}]], [4.34, [3.979752982 \times 10^{35533029554557046}, 9.738300420 \\
& \times 10^{35533029554557046}]], [4.35, [2.261332606 \times 10^{71066059109114093}, 5.533392744 \\
& \times 10^{71066059109114093}]], [4.36, [7.300979036 \times 10^{142132118218228186}, 1.786521111 \\
& \times 10^{142132118218228187}]], [4.37, [7.610521442 \times 10^{284264236436456373}, 1.862264933 \\
& \times 10^{284264236436456374}]], [4.38, [8.269534047 \times 10^{568528472872912747}, 2.023522747 \\
& \times 10^{568528472872912748}]], [4.39, [9.763696932 \times 10^{1137056945745825495}, 2.389138582 \\
& \times 10^{1137056945745825496}]], [4.40, [1.361071035 \times 10^{2274113891491650992}, 3.330487773 \\
& \times 10^{2274113891491650992}]], [4.41, [2.644927643 \times 10^{4548227782983301984}, 6.472034845 \\
& \times 10^{4548227782983301984}]], [4.42, [9.988029174 \times 10^{9096455565966603968}, 2.444031808 \\
& \times 10^{9096455565966603969}]], [4.43, [Float( $\infty$ ), Float( $\infty$ )]], [4.44, [Float( $\infty$ ), Float( $\infty$ )]], \\
& [4.45, [Float( $\infty$ ), Float( $\infty$ )]], [4.46, [Float( $\infty$ ), Float( $\infty$ )]], [4.47, [Float( $\infty$ ), \\
& Float( $\infty$ )]], [4.48, [Float( $\infty$ ), Float( $\infty$ )]], [4.49, [Float( $\infty$ ), Float( $\infty$ )]], [4.50, [ \\
& Float( $\infty$ ), Float( $\infty$ )]], [4.51, [Float( $\infty$ ), Float( $\infty$ )]], [4.52, [Float( $\infty$ ), Float( $\infty$ )]], \\
& [4.53, [Float( $\infty$ ), Float( $\infty$ )]], [4.54, [Float( $\infty$ ), Float( $\infty$ )]], [4.55, [Float( $\infty$ ), \\
& Float( $\infty$ )]], [4.56, [Float( $\infty$ ), Float( $\infty$ )]], [4.57, [Float( $\infty$ ), Float( $\infty$ )]], [4.58, [ \\
& Float( $\infty$ ), Float( $\infty$ )]], [4.59, [Float( $\infty$ ), Float( $\infty$ )]], [4.60, [Float( $\infty$ ), Float( $\infty$ )]]]
\end{aligned}$$











$\text{Float}(\infty)]], [9.68, [\text{Float}(\infty), \text{Float}(\infty)]], [9.69, [\text{Float}(\infty), \text{Float}(\infty)]], [9.70, [\text{Float}(\infty), \text{Float}(\infty)]], [9.71, [\text{Float}(\infty), \text{Float}(\infty)]], [9.72, [\text{Float}(\infty), \text{Float}(\infty)]], [9.73, [\text{Float}(\infty), \text{Float}(\infty)]], [9.74, [\text{Float}(\infty), \text{Float}(\infty)]], [9.75, [\text{Float}(\infty), \text{Float}(\infty)]], [9.76, [\text{Float}(\infty), \text{Float}(\infty)]], [9.77, [\text{Float}(\infty), \text{Float}(\infty)]], [9.78, [\text{Float}(\infty), \text{Float}(\infty)]], [9.79, [\text{Float}(\infty), \text{Float}(\infty)]], [9.80, [\text{Float}(\infty), \text{Float}(\infty)]], [9.81, [\text{Float}(\infty), \text{Float}(\infty)]], [9.82, [\text{Float}(\infty), \text{Float}(\infty)]], [9.83, [\text{Float}(\infty), \text{Float}(\infty)]], [9.84, [\text{Float}(\infty), \text{Float}(\infty)]], [9.85, [\text{Float}(\infty), \text{Float}(\infty)]], [9.86, [\text{Float}(\infty), \text{Float}(\infty)]], [9.87, [\text{Float}(\infty), \text{Float}(\infty)]], [9.88, [\text{Float}(\infty), \text{Float}(\infty)]], [9.89, [\text{Float}(\infty), \text{Float}(\infty)]], [9.90, [\text{Float}(\infty), \text{Float}(\infty)]], [9.91, [\text{Float}(\infty), \text{Float}(\infty)]], [9.92, [\text{Float}(\infty), \text{Float}(\infty)]], [9.93, [\text{Float}(\infty), \text{Float}(\infty)]], [9.94, [\text{Float}(\infty), \text{Float}(\infty)]], [9.95, [\text{Float}(\infty), \text{Float}(\infty)]], [9.96, [\text{Float}(\infty), \text{Float}(\infty)]], [9.97, [\text{Float}(\infty), \text{Float}(\infty)]], [9.98, [\text{Float}(\infty), \text{Float}(\infty)]], [9.99, [\text{Float}(\infty), \text{Float}(\infty)]], [10.00, [\text{Float}(\infty), \text{Float}(\infty)]], [10.01, [\text{Float}(\infty), \text{Float}(\infty)]]]$

*for unstable equilibrium point,  $\left[ \frac{6}{13}, \frac{4}{13} \right]$*

$\left[ [0.01, [0.4715384615, 0.3176923077]], [0.02, [0.4719838461, 0.3192738462]], [0.03, [0.4724958648, 0.3210121931]], [0.04, [0.4730826168, 0.3229279607]], [0.05, [0.4737535130, 0.3250450166]], [0.06, [0.4745195416, 0.3273911414]], [0.07, [0.4753936013, 0.3299988528]], [0.08, [0.4763909226, 0.3329064467]], [0.09, [0.4775296053, 0.3361593252]], [0.10, [0.4788313112, 0.3398117066]], [0.11, [0.4803221671, 0.3439288527]], [0.12, [0.4820339549, 0.3485900032]], [0.13, [0.4840057009, 0.3538922915]], [0.14, [0.4862858278, 0.3599560449]], [0.15, [0.4889351141, 0.3669320679]], [0.16, [0.4920308333, 0.3750118240]], [0.17, [0.4956726524, 0.3844419389]], [0.18, [0.4999912174, 0.3955452986]], [0.19, [0.5051609467, 0.4087524738]], [0.20, [0.5114196103, 0.4246497906]], [0.21, [0.5190992191, 0.4440551352]], [0.22, [0.5286764882, 0.4681417452]], [0.23, [0.5408586917, 0.4986487355]], [0.24, [0.5567368541, 0.5382566046]], [0.25, [0.5780750396, 0.5912961029]], [0.26, [0.6078954354, 0.6651814561]], [0.27, [0.6517660949, 0.7735639277]], [0.28, [0.7209544686, 0.9440525743]], [0.29, [0.8412995090, 1.239931056]], [0.30, [1.083316945, 1.833835507]], [0.31, [1.695541367, 3.334047842]], [0.32, [3.991943959, 8.955896088]], [0.33, [22.14651944, 53.38143473]], [0.34, [695.7819033, 1701.727450]], [0.35, [691032.8960, 1.690935186  $\times 10^6$ ]], [0.36, [6.817923412  $\times 10^{11}$ , 1.668316936  $\times 10^{12}$ ]], [0.37, [6.636748016  $\times 10^{23}$ , 1.623987371  $\times 10^{24}$ ]], [0.38, [6.288735934  $\times 10^{47}$ , 1.538828755  $\times 10^{48}$ ]], [0.39, [5.646491965  $\times 10^{95}$ , 1.381674738  $\times 10^{96}$ ]], [0.40, [4.552078412  $\times 10^{191}$ , 1.113875787  $\times 10^{192}$ ]], [0.41,$

$[2.958500449 \times 10^{383}, 7.239335445 \times 10^{383}]]$ , [0.42,  $[1.249670473 \times 10^{767}, 3.057894906 \times 10^{767}]$ ], [0.43,  $[2.229683500 \times 10^{1534}, 5.455948641 \times 10^{1534}]$ ], [0.44,  $[7.098043477 \times 10^{3068}, 1.736863568 \times 10^{3069}]$ ], [0.45,  $[7.193322310 \times 10^{6137}, 1.760177933 \times 10^{6138}]$ ], [0.46,  $[7.387734045 \times 10^{12275}, 1.807749723 \times 10^{12276}]$ ], [0.47,  $[7.792462412 \times 10^{24551}, 1.906785179 \times 10^{24552}]$ ], [0.48,  $[8.669651576 \times 10^{49103}, 2.121429946 \times 10^{49104}]$ ], [0.49,  $[1.073137816 \times 10^{98208}, 2.625926405 \times 10^{98208}]$ ], [0.50,  $[1.644232429 \times 10^{196416}, 4.023372664 \times 10^{196416}]$ ], [0.51,  $[3.859922905 \times 10^{392832}, 9.445080893 \times 10^{392832}]$ ], [0.52,  $[2.127205623 \times 10^{785665}, 5.205189243 \times 10^{785665}]$ ], [0.53,  $[6.460574752 \times 10^{1571330}, 1.580877460 \times 10^{1571331}]$ ], [0.54,  $[5.959290043 \times 10^{3142661}, 1.458215045 \times 10^{3142662}]$ ], [0.55,  $[5.070388748 \times 10^{6285323}, 1.240704363 \times 10^{6285324}]$ ], [0.56,  $[3.670580285 \times 10^{12570647}, 8.981766886 \times 10^{12570647}]$ ], [0.57,  $[1.923630555 \times 10^{25141295}, 4.707048987 \times 10^{25141295}]$ ], [0.58,  $[5.283181673 \times 10^{50282590}, 1.292773962 \times 10^{50282591}]$ ], [0.59,  $[3.985137415 \times 10^{100565181}, 9.751475921 \times 10^{100565181}]$ ], [0.60,  $[2.267455717 \times 10^{201130363}, 5.548375756 \times 10^{201130363}]$ ], [0.61,  $[7.340570930 \times 10^{402260726}, 1.796209093 \times 10^{402260727}]$ ], [0.62,  $[7.693286216 \times 10^{804521453}, 1.882517150 \times 10^{804521454}]$ ], [0.63,  $[8.450375184 \times 10^{1609042907}, 2.067773869 \times 10^{1609042908}]$ ], [0.64,  $[1.019539823 \times 10^{3218085816}, 2.494774208 \times 10^{3218085816}]$ ], [0.65,  $[1.484091234 \times 10^{6436171632}, 3.631513400 \times 10^{6436171632}]$ ], [0.66,  $[3.144657930 \times 10^{12872343264}, 7.694855383 \times 10^{12872343264}]$ ], [0.67,  $[1.411884053 \times 10^{25744686529}, 3.454825243 \times 10^{25744686529}]$ ], [0.68,  $[2.846100797 \times 10^{51489373058}, 6.964297714 \times 10^{51489373058}]$ ], [0.69,  $[1.156518983 \times 10^{102978746117}, 2.829956870 \times 10^{102978746117}]$ ], [0.70,  $[1.909667434 \times 10^{205957492234}, 4.672881777 \times 10^{205957492234}]$ ], [0.71,  $[5.206761629 \times 10^{411914984468}, 1.274074276 \times 10^{411914984469}]$ ], [0.72,  $[3.870682983 \times 10^{823829968937}, 9.471410385 \times 10^{823829968937}]$ ], [0.73,  $[2.139081923 \times 10^{1647659937875}, 5.234250089 \times 10^{1647659937875}]$ ], [0.74,  $[6.532915589 \times 10^{3295319875750}, 1.598578981 \times 10^{3295319875751}]$ ], [0.75,  $[6.093492842 \times 10^{6590639751501}, 1.491053947 \times 10^{6590639751502}]$ ], [0.76,  $[5.301329790 \times 10^{13181279503003}, 1.297214736 \times 10^{13181279503004}]$ ], [0.77,  $[4.012562921 \times 10^{26362559006007}, 9.818585065 \times 10^{26362559006007}]$ ], [0.78,  $[2.298772128 \times 10^{52725118012015}, 5.625005794 \times 10^{52725118012015}]$ ], [0.79,  $[7.544736160 \times 10^{105450236024030}, 1.846167530 \times 10^{105450236024031}]$ ], [0.80,  $[8.127188364 \times 10^{210900472048061}, 1.988691315 \times 10^{210900472048062}]$ ], [0.81,  $[9.430459684 \times 10^{421800944096123}, 2.307596725 \times 10^{421800944096124}]$ ], [0.82,  $[1.269749167 \times 10^{843601888192248}, 3.107026719$ ]

$$\begin{aligned}
& \times 10^{843601888192248}]], [0.83, [2.301908651 \times 10^{1687203776384496}, 5.632680737 \\
& \times 10^{1687203776384496}]], [0.84, [7.565338777 \times 10^{3374407552768992}, 1.851208912 \\
& \times 10^{3374407552768993}]], [0.85, [8.171635256 \times 10^{6748815105537985}, 1.999567293 \\
& \times 10^{6748815105537986}]], [0.86, [9.533890454 \times 10^{13497630211075971}, 2.332905834 \\
& \times 10^{13497630211075972}]], [0.87, [1.297754451 \times 10^{26995260422151944}, 3.175554556 \\
& \times 10^{26995260422151944}]], [0.88, [2.404569118 \times 10^{53990520844303888}, 5.883886907 \\
& \times 10^{53990520844303888}]], [0.89, [8.255183704 \times 10^{107981041688607776}, 2.020011274 \\
& \times 10^{107981041688607777}]], [0.90, [9.729839925 \times 10^{215962083377215553}, 2.380853905 \\
& \times 10^{215962083377215554}]], [0.91, [1.351647987 \times 10^{431924166754431108}, 3.307429943 \\
& \times 10^{431924166754431108}]], [0.92, [2.608431382 \times 10^{863848333508862216}, 6.382729911 \\
& \times 10^{863848333508862216}]], [0.93, [9.714289535 \times 10^{1727696667017724432}, 2.377048785 \\
& \times 10^{1727696667017724433}]], [0.94, [1.347330987 \times 10^{3455393334035448866}, 3.296866412 \\
& \times 10^{3455393334035448866}]], [0.95, [2.591795962 \times 10^{6910786668070897732}, 6.342023687 \\
& \times 10^{6910786668070897732}]], [0.96, [Float(\infty), Float(\infty)]], [0.97, [Float(\infty), Float(\infty)]], \\
[0.98, [Float(\infty), Float(\infty)]], [0.99, [Float(\infty), Float(\infty)]], [1.00, [Float(\infty), \\
Float(\infty)]], [1.01, [Float(\infty), Float(\infty)]], [1.02, [Float(\infty), Float(\infty)]], [1.03, [ \\
Float(\infty), Float(\infty)]], [1.04, [Float(\infty), Float(\infty)]], [1.05, [Float(\infty), Float(\infty)]], \\
[1.06, [Float(\infty), Float(\infty)]], [1.07, [Float(\infty), Float(\infty)]], [1.08, [Float(\infty), \\
Float(\infty)]], [1.09, [Float(\infty), Float(\infty)]], [1.10, [Float(\infty), Float(\infty)]], [1.11, [ \\
Float(\infty), Float(\infty)]], [1.12, [Float(\infty), Float(\infty)]], [1.13, [Float(\infty), Float(\infty)]], \\
[1.14, [Float(\infty), Float(\infty)]], [1.15, [Float(\infty), Float(\infty)]], [1.16, [Float(\infty), \\
Float(\infty)]], [1.17, [Float(\infty), Float(\infty)]], [1.18, [Float(\infty), Float(\infty)]], [1.19, [ \\
Float(\infty), Float(\infty)]], [1.20, [Float(\infty), Float(\infty)]], [1.21, [Float(\infty), Float(\infty)]], \\
[1.22, [Float(\infty), Float(\infty)]], [1.23, [Float(\infty), Float(\infty)]], [1.24, [Float(\infty), \\
Float(\infty)]], [1.25, [Float(\infty), Float(\infty)]], [1.26, [Float(\infty), Float(\infty)]], [1.27, [ \\
Float(\infty), Float(\infty)]], [1.28, [Float(\infty), Float(\infty)]], [1.29, [Float(\infty), Float(\infty)]], \\
[1.30, [Float(\infty), Float(\infty)]], [1.31, [Float(\infty), Float(\infty)]], [1.32, [Float(\infty), \\
Float(\infty)]], [1.33, [Float(\infty), Float(\infty)]], [1.34, [Float(\infty), Float(\infty)]], [1.35, [ \\
Float(\infty), Float(\infty)]], [1.36, [Float(\infty), Float(\infty)]], [1.37, [Float(\infty), Float(\infty)]], \\
[1.38, [Float(\infty), Float(\infty)]], [1.39, [Float(\infty), Float(\infty)]], [1.40, [Float(\infty), \\
Float(\infty)]], [1.41, [Float(\infty), Float(\infty)]], [1.42, [Float(\infty), Float(\infty)]], [1.43, [ \\
Float(\infty), Float(\infty)]], [1.44, [Float(\infty), Float(\infty)]], [1.45, [Float(\infty), Float(\infty)]], \\
[1.46, [Float(\infty), Float(\infty)]], [1.47, [Float(\infty), Float(\infty)]], [1.48, [Float(\infty), \\
Float(\infty)]], [1.49, [Float(\infty), Float(\infty)]], [1.50, [Float(\infty), Float(\infty)]], [1.51, [ \\
Float(\infty), Float(\infty)]], [1.52, [Float(\infty), Float(\infty)]], [1.53, [Float(\infty), Float(\infty)]]]
\end{aligned}$$

















```

Float(∞)], [9.65, [Float(∞), Float(∞)]], [9.66, [Float(∞), Float(∞)]], [9.67, [
Float(∞), Float(∞)]], [9.68, [Float(∞), Float(∞)]], [9.69, [Float(∞), Float(∞)]],
[9.70, [Float(∞), Float(∞)]], [9.71, [Float(∞), Float(∞)]], [9.72, [Float(∞),
Float(∞)]], [9.73, [Float(∞), Float(∞)]], [9.74, [Float(∞), Float(∞)]], [9.75, [
Float(∞), Float(∞)]], [9.76, [Float(∞), Float(∞)]], [9.77, [Float(∞), Float(∞)]],
[9.78, [Float(∞), Float(∞)]], [9.79, [Float(∞), Float(∞)]], [9.80, [Float(∞),
Float(∞)]], [9.81, [Float(∞), Float(∞)]], [9.82, [Float(∞), Float(∞)]], [9.83, [
Float(∞), Float(∞)]], [9.84, [Float(∞), Float(∞)]], [9.85, [Float(∞), Float(∞)]],
[9.86, [Float(∞), Float(∞)]], [9.87, [Float(∞), Float(∞)]], [9.88, [Float(∞),
Float(∞)]], [9.89, [Float(∞), Float(∞)]], [9.90, [Float(∞), Float(∞)]], [9.91, [
Float(∞), Float(∞)]], [9.92, [Float(∞), Float(∞)]], [9.93, [Float(∞), Float(∞)]],
[9.94, [Float(∞), Float(∞)]], [9.95, [Float(∞), Float(∞)]], [9.96, [Float(∞),
Float(∞)]], [9.97, [Float(∞), Float(∞)]], [9.98, [Float(∞), Float(∞)]], [9.99, [
Float(∞), Float(∞)]], [10.00, [Float(∞), Float(∞)]], [10.01, [Float(∞), Float(∞)]]]

```

### PROBLEM 3:

Use EquPts(F,var) together with SIRS to find all the equilibrium points of the SIRS model,  
confirming Equations

### Problems 4:

Write a Maple code Chemostat(N,C,a1,a2) (analogous to SIRS) giving the underlying transformation

#Chemostat info is on page 126 of the book

#Parameters:

#

```

> print(SIRS);
proc(s, i, β, γ, v, N) [-β*s*i + γ*(N - s - i), β*s*i - v*i] end proc

```

(15)

```

> Chemostat := proc(N, C, a1, a2);
[a1*C/(1+C)* N - N, -C/(1+C)*N+a2];
end;

```

#Writing the underlying transformation is done

```
> Chemostat(N,C,a1,a2);
```

$$= \left[ \frac{a1 C N}{C + 1} - N, -\frac{C N}{C + 1} + a2 \right] \quad (16)$$

$$= \left[ 1, \frac{10}{3} \right] \quad (17)$$

NOW FIND THE EQUILIBRIUM POINTS of chemostat

#In the chemostat model, the "N" and "C" are the "x" and "y"

```
> EquPts(Chemostat(y,x,y,x), [x,y]);
{[0,0], [1,2]}
```

(18)

Problem 5 (10 brownie points) Write a Dis3(x

```
> print(Dis2);
proc(F,x,y,pt,h,A)
```

```
local L, i;
L := Orb2([x + h * F[1], y + h * F[2]], x, y, pt, 0, trunc(A/h));
L := [seq([i * h, [L[i][1], L[i][2]]], i = 1 .. nops(L))]
```

end proc

```
> print(Orbk);
proc(k,z,f,INI,K1,K2)
```

```
local L, i, newguy;
L := INI;
if not (type(k, integer) and type(z, symbol) and type(INI, list) and nops(INI) = k and
type(K1, integer) and type(K2, integer) and 0 < K1 and K1 < K2) then
    print(bad input); RETURN(FAIL)
end if;
```

while nops(L) < K2 do

```
    newguy := subs({seq(z[i] = L[-i], i = 1 .. k)}, f);
    L := [op(L), newguy]
```

end do;

[op(K1 .. K2, L)]

end proc

Code for dis3

```
> Dis3 := proc(F,x,y,z,pt,h,A) local L;
L := Orbk(3,g,g[1]+h*F[1]+g[2]+h*F[2]+g[3]+h*F[3],10,100);
print(L);
end;
```

```
Dis3 := proc(F,x,y,z,pt,h,A)
```

(21)

```

local L;
L := Orbk(3,g,g[1]+h*F[1]+g[2]+h*F[2]+g[3]+h*F[3],10,100); print(L)
end proc

```

```

> dF1 := RandNice([x,y,z],10);
print(Dis3(dF1,x,y,z,[1,1,1],0.01,100));
dF2 := RandNice([x,y,z],10);
dF1 := [(2 - 2 x - y - 3 z) (5 - 4 x - 3 y - 10 z), (1 - 8 x - 3 y - 8 z) (8 - 7 x - 5 y
- 6 z), (7 - x - 5 y - 6 z) (6 - 6 x - 4 y - 10 z)]
                                bad input
                                FAIL

dF2 := [(10 - 5 x - 9 y - 9 z) (5 - 10 x - 9 y - 5 z), (5 - 2 x - 4 y - 9 z) (10 - 3 x - 7 y   (22
- z), (4 - 9 x - 5 y - 9 z) (10 - 7 x - 9 y - 6 z)]

```