

#OK to post

Anusha Nagar, Homework 19, 11.06.2021

MAPLE CODE is  
after handwritten portion

$$(1) (i) \beta = 0.3 \frac{V}{N} \Rightarrow R = N - IN - S$$

$$R @ t = 10 \Rightarrow 1000 - 996.7 - 2.979$$

$$R = 6.279$$

$$\beta = 0.9 \frac{V}{N} \Rightarrow R = 1000 - 988.3315 - 8.91$$

$$R = 2.678$$

$$\beta = 3.9 \frac{V}{N} \Rightarrow R = 1000 - 914.6283 - 40.00$$

$$R = 45.372$$

$$(ii) \beta = 0.3 \frac{V}{N} \Rightarrow R = 1000 - 996.402 - 2.958$$

$$R = 0.64$$

$$\beta = 0.9 \frac{V}{N} \Rightarrow R = 1000 - 985.6773 - 8.9797$$

$$R = 5.343$$

$$\beta = 3.9 \frac{V}{N} \Rightarrow R = 1000 - 872.5259 - 40.8742$$

$$R = 86.60$$

$$(iii) \beta = 0.3 \frac{V}{N} \Rightarrow 1000 - 996.62 - 2.94$$

$$R = 0.44$$

$$\beta = 0.9 \frac{V}{N} \Rightarrow 1000 - 987.57 - 8.97$$

$$R = 3.46$$

$$\beta = 3.9 \frac{V}{N} \Rightarrow 1000 - 902.19 - 41.95$$

$$R = 55.86$$

(2) ✓

(See maple code)

(3) ✓

(4) Chemostat (N, C, a1, a2)

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> #OKay to Post
> #Anusha Nagar, Homework 19, 11.06.2021
> read "C://Users/an646/Documents/M19.txt"
> #Problem 1
> #N = 1000, I0 = 200, R0 = 0. (Susceptible0 = 800)
> #I Think there's a typo - I'm going to be using beta = 0.3*nu div N, 0.9*nu div N, 3.9*nu div N (I
  think nu and N are switched in the homework problem)
> #(i) Where nu = 1, gamma = 3
> SIRSdemo(1000, 200, 3, 1, 0.01, 10)

```

*This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, 10*

*with population size, 1000, and fixed parameters nu=, 1, and gamma=, 3  
where we change beta from 0.2\*nu/N to 4\*nu/N*

*Recall that the epidemic will persist if beta exceeds nu/N, that in this case is,  $\frac{1}{1000}$*

*We start with , 200, infected individuals, 0 removed and hence, 800, susceptible  
We will show what happens once time is close to, 10*

*beta is,  $\frac{1}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [998.9666995, 0.9909989667]], [9.99, [998.9666995, 0.9909989667]], [10.00, [998.9666995, 0.9909989667]], [10.01, [998.9666995, 0.9909989667]]]*

*beta is,  $\frac{3}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [996.7009881, 2.978970309]], [9.99, [996.7009881, 2.978970309]], [10.00, [996.7009881, 2.978970309]], [10.01, [996.7009881, 2.978970309]]]*

*beta is,  $\frac{1}{2}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [994.1715221, 4.974854288]], [9.99, [994.1715221, 4.974854288]], [10.00, [994.1715221, 4.974854288]], [10.01, [994.1715221, 4.974854288]]]*

*beta is,  $\frac{7}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [991.3807432, 6.978577656]], [9.99, [991.3807432, 6.978577656]], [10.00, [991.3807432, 6.978577656]], [10.01, [991.3807432, 6.978577656]]]*

*beta is,  $\frac{9}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [988.3315033, 8.990054852]], [9.99, [988.3315033, 8.990054852]], [10.00, [988.3315033, 8.990054852]], [10.01, [988.3315033, 8.990054852]]]

*beta is,  $\frac{11}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [985.0270559, 11.00918827]], [9.99, [985.0270559, 11.00918827]], [10.00, [985.0270559, 11.00918827]], [10.01, [985.0270559, 11.00918827]]]

*beta is,  $\frac{13}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [981.4710448, 13.03586861]], [9.99, [981.4710448, 13.03586861]], [10.00, [981.4710448, 13.03586861]], [10.01, [981.4710448, 13.03586861]]]

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [977.6674922, 15.06997519]], [9.99, [977.6674922, 15.06997519]], [10.00, [977.6674922, 15.06997519]], [10.01, [977.6674922, 15.06997519]]]

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [973.6207848, 17.11137641]], [9.99, [973.6207848, 17.11137641]], [10.00, [973.6207848, 17.11137641]], [10.01, [973.6207848, 17.11137641]]]

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [969.3356593, 19.15993017]], [9.99, [969.3356593, 19.15993017]], [10.00, [969.3356593, 19.15993017]], [10.01, [969.3356593, 19.15993017]]]

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [964.8171858, 21.21548438]], [9.99, [964.8171858, 21.21548438]], [10.00, [964.8171858, 21.21548438]], [10.01, [964.8171858, 21.21548438]]]

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [960.0707508, 23.27787743]], [9.99, [960.0707508, 23.27787743]], [10.00, [960.0707508, 23.27787743]], [10.01, [960.0707508, 23.27787743]]]

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [955.1020392, 25.34693877]], [9.99, [955.1020392, 25.34693877]], [10.00, [955.1020392, 25.34693877]], [10.01, [955.1020392, 25.34693877]]]

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [949.9170149, 27.42248950]], [9.99, [949.9170149, 27.42248950]], [10.00, [949.9170149, 27.42248950]], [10.01, [949.9170149, 27.42248950]]]

*beta is,  $\frac{29}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [944.5219011, 29.50434292]], [9.99, [944.5219011, 29.50434292]], [10.00, [944.5219011, 29.50434292]], [10.01, [944.5219011, 29.50434292]]]

*beta is,  $\frac{31}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [938.9231598, 31.59230516]], [9.99, [938.9231598, 31.59230516]], [10.00, [938.9231598, 31.59230516]], [10.01, [938.9231598, 31.59230516]]]

*beta is,  $\frac{33}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [933.1274712, 33.68617582]], [9.99, [933.1274712, 33.68617582]], [10.00, [933.1274712, 33.68617582]], [10.01, [933.1274712, 33.68617582]]]

*beta is,  $\frac{7}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [927.1417118, 35.78574860]], [9.99, [927.1417118, 35.78574860]], [10.00, [927.1417118, 35.78574860]], [10.01, [927.1417118, 35.78574860]]]

*beta is,  $\frac{37}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [920.9729335, 37.89081195]], [9.99, [920.9729335, 37.89081195]], [10.00, [920.9729335, 37.89081195]], [10.01, [920.9729335, 37.89081195]]]

*beta is,  $\frac{39}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [914.6283415, 40.00114971]], [9.99, [914.6283415, 40.00114971]], [10.00, [914.6283415, 40.00114971]], [10.01, [914.6283415, 40.00114971]]]

**(1)**

> *SIRSdemo(1000, 200, 3, 2, 0.01, 10)*

*This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, 10*

*with population size, 1000, and fixed parameters nu=, 2, and gamma=, 3*

*where we change beta from 0.2\*nu/N to 4\*nu/N*

*Recall that the epidemic will persist if beta exceeds nu/N, that in this case is,  $\frac{1}{500}$*

*We start with , 200, infected individuals, 0 removed and hence, 800, susceptible*

*We will show what happens once time is close to, 10*

*beta is,  $\frac{1}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [998.9334028, 0.9819978668]], [9.99, [998.9334028, 0.9819978668]], [10.00, [998.9334028, 0.9819978668]], [10.01, [998.9334028, 0.9819978668]]]*

*beta is,  $\frac{3}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [996.4021571, 2.957935239]], [9.99, [996.4021571, 2.957935239]], [10.00, [996.4021571, 2.957935239]], [10.01, [996.4021571, 2.957935239]]]*

*beta is,  $\frac{1}{2}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [993.3444243, 4.949667221]], [9.99, [993.3444243, 4.949667221]], [10.00, [993.3444243, 4.949667221]], [10.01, [993.3444243, 4.949667221]]]*

*beta is,  $\frac{7}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [989.7667603, 6.956997143]], [9.99, [989.7667603, 6.956997143]], [10.00, [989.7667603, 6.956997143]], [10.01, [989.7667603, 6.956997143]]]*

*beta is,  $\frac{9}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [985.6773407, 8.979679729]], [9.99, [985.6773407, 8.979679729]], [10.00, [985.6773407, 8.979679729]], [10.01, [985.6773407, 8.979679729]]]*

*beta is,  $\frac{11}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [981.0859054, 11.01742279]], [9.99, [981.0859054, 11.01742279]], [10.00, [981.0859054, 11.01742279]], [10.01, [981.0859054, 11.01742279]]]*

*beta is,  $\frac{13}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [976.0036901, 13.06988925]], [9.99, [976.0036901, 13.06988925]], [10.00, [976.0036901, 13.06988925]], [10.01, [976.0036901, 13.06988925]]]

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [970.4433482, 15.13669951]], [9.99, [970.4433482, 15.13669951]], [10.00, [970.4433482, 15.13669951]], [10.01, [970.4433482, 15.13669951]]]

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [964.4188616, 17.21743410]], [9.99, [964.4188616, 17.21743410]], [10.00, [964.4188616, 17.21743410]], [10.01, [964.4188616, 17.21743410]]]

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [957.9454447, 19.31163661]], [9.99, [957.9454447, 19.31163661]], [10.00, [957.9454447, 19.31163661]], [10.01, [957.9454447, 19.31163661]]]

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [951.0394389, 21.41881679]], [9.99, [951.0394389, 21.41881679]], [10.00, [951.0394389, 21.41881679]], [10.01, [951.0394389, 21.41881679]]]

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [943.7182031, 23.53845386]], [9.99, [943.7182031, 23.53845386]], [10.00, [943.7182031, 23.53845386]], [10.01, [943.7182031, 23.53845386]]]

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [935.9999984, 25.67000000]], [9.99, [935.9999984, 25.67000000]], [10.00, [935.9999984, 25.67000000]], [10.01, [935.9999984, 25.67000000]]]

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [927.9038703, 27.81288384]], [9.99, [927.9038703, 27.81288384]], [10.00,

[927.9038703, 27.81288384]], [10.01, [927.9038703, 27.81288384]]]

*beta is,  $\frac{29}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [919.4495282, 29.96651411]], [9.99, [919.4495282, 29.96651411]], [10.00, [919.4495282, 29.96651411]], [10.01, [919.4495282, 29.96651411]]]

*beta is,  $\frac{31}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [910.6572255, 32.13028319]], [9.99, [910.6572255, 32.13028319]], [10.00, [910.6572255, 32.13028319]], [10.01, [910.6572255, 32.13028319]]]

*beta is,  $\frac{33}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [901.5476397, 34.30357076]], [9.99, [901.5476397, 34.30357076]], [10.00, [901.5476397, 34.30357076]], [10.01, [901.5476397, 34.30357076]]]

*beta is,  $\frac{7}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [892.1417551, 36.48574730]], [9.99, [892.1417551, 36.48574730]], [10.00, [892.1417551, 36.48574730]], [10.01, [892.1417551, 36.48574730]]]

*beta is,  $\frac{37}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [882.4607475, 38.67617753]], [9.99, [882.4607475, 38.67617753]], [10.00, [882.4607475, 38.67617753]], [10.01, [882.4607475, 38.67617753]]]

*beta is,  $\frac{39}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [872.5258747, 40.87422371]], [9.99, [872.5258747, 40.87422371]], [10.00, [872.5258747, 40.87422371]], [10.01, [872.5258747, 40.87422371]]]

(2)

> *SIRSDemo(1000, 200, 7, 3, 0.01, 10)*

*This is a numerical demonstration of the R0 phenomenon in the SIRS model using discretization with mesh size=, 0.01, and letting it run until time t=, 10*

*with population size, 1000, and fixed parameters nu=, 3, and gamma=, 7*

*where we change beta from  $0.2 \cdot \text{nu}/N$  to  $4 \cdot \text{nu}/N$*

*Recall that the epidemic will persist if beta exceeds  $\text{nu}/N$ , that in this case is,  $\frac{3}{1000}$*

*We start with , 200, infected individuals, 0 removed and hence, 800, susceptible*

*We will show what happens once time is close to, 10*

*beta is,  $\frac{1}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [998.9571869, 0.9729968716]], [9.99, [998.9571869, 0.9729968716]], [10.00, [998.9571869, 0.9729968716]], [10.01, [998.9571869, 0.9729968716]]]*

*beta is,  $\frac{3}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [996.6155905, 2.936908621]], [9.99, [996.6155905, 2.936908621]], [10.00, [996.6155905, 2.936908621]], [10.01, [996.6155905, 2.936908621]]]*

*beta is,  $\frac{1}{2}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [993.9350689, 4.924545130]], [9.99, [993.9350689, 4.924545130]], [10.00, [993.9350689, 4.924545130]], [10.01, [993.9350689, 4.924545130]]]*

*beta is,  $\frac{7}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [990.9190693, 6.935665103]], [9.99, [990.9190693, 6.935665103]], [10.00, [990.9190693, 6.935665103]], [10.01, [990.9190693, 6.935665103]]]*

*beta is,  $\frac{9}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [987.5717147, 8.969979927]], [9.99, [987.5717147, 8.969979927]], [10.00, [987.5717147, 8.969979927]], [10.01, [987.5717147, 8.969979927]]]*

*beta is,  $\frac{11}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [983.8977865, 11.02715490]], [9.99, [983.8977865, 11.02715490]], [10.00, [983.8977865, 11.02715490]], [10.01, [983.8977865, 11.02715490]]]*

*beta is,  $\frac{13}{10}$ , times the threshold value*

*the long-term behavior is*

*[[9.98, [979.9027040, 13.10681067]], [9.99, [979.9027040, 13.10681067]], [10.00, [979.9027040, 13.10681067]], [10.01, [979.9027040, 13.10681067]]]*

*beta is,  $\frac{3}{2}$ , times the threshold value*

*the long-term behavior is*



[[9.98, [975.5925002, 15.20852494]], [9.99, [975.5925002, 15.20852494]], [10.00, [975.5925002, 15.20852494]], [10.01, [975.5925002, 15.20852494]]]

*beta is,  $\frac{17}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [970.9737953, 17.33183428]], [9.99, [970.9737953, 17.33183428]], [10.00, [970.9737953, 17.33183428]], [10.01, [970.9737953, 17.33183428]]]

*beta is,  $\frac{19}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [966.0537675, 19.47623623]], [9.99, [966.0537675, 19.47623623]], [10.00, [966.0537675, 19.47623623]], [10.01, [966.0537675, 19.47623623]]]

*beta is,  $\frac{21}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [960.8401210, 21.64119148]], [9.99, [960.8401210, 21.64119148]], [10.00, [960.8401210, 21.64119148]], [10.01, [960.8401210, 21.64119148]]]

*beta is,  $\frac{23}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [955.3410529, 23.82612625]], [9.99, [955.3410529, 23.82612625]], [10.00, [955.3410529, 23.82612625]], [10.01, [955.3410529, 23.82612625]]]

*beta is,  $\frac{5}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [949.5652167, 26.03043478]], [9.99, [949.5652167, 26.03043478]], [10.00, [949.5652167, 26.03043478]], [10.01, [949.5652167, 26.03043478]]]

*beta is,  $\frac{27}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [943.5216861, 28.25348193]], [9.99, [943.5216861, 28.25348193]], [10.00, [943.5216861, 28.25348193]], [10.01, [943.5216861, 28.25348193]]]

*beta is,  $\frac{29}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [937.2199158, 30.49460585]], [9.99, [937.2199158, 30.49460585]], [10.00, [937.2199158, 30.49460585]], [10.01, [937.2199158, 30.49460585]]]

*beta is,  $\frac{31}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [930.6697029, 32.75312075]], [9.99, [930.6697029, 32.75312075]], [10.00, [930.6697029, 32.75312075]], [10.01, [930.6697029, 32.75312075]]]

*beta is,  $\frac{33}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [923.8811464, 35.02831970]], [9.99, [923.8811464, 35.02831970]], [10.00, [923.8811464, 35.02831970]], [10.01, [923.8811464, 35.02831970]]]

*beta is,  $\frac{7}{2}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [916.8646074, 37.31947743]], [9.99, [916.8646074, 37.31947743]], [10.00, [916.8646074, 37.31947743]], [10.01, [916.8646074, 37.31947743]]]

*beta is,  $\frac{37}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [909.6306685, 39.62585316]], [9.99, [909.6306685, 39.62585316]], [10.00, [909.6306685, 39.62585316]], [10.01, [909.6306685, 39.62585316]]]

*beta is,  $\frac{39}{10}$ , times the threshold value*

*the long-term behavior is*

[[9.98, [902.1900937, 41.94669340]], [9.99, [902.1900937, 41.94669340]], [10.00, [902.1900937, 41.94669340]], [10.01, [902.1900937, 41.94669340]]]

(3)

> #Problem 2

> f1 := RandNice([x, y], 8)

f1 := [(5 - 7x - 7y) (2 - 5x - 8y), (6 - 2x - 3y) (4 - 4x - 6y)]

(4)

> f2 := RandNice([x, y], 8)

f2 := [(5 - 3x - 8y) (1 - 8x - 5y), (2 - 3x - 2y) (2 - 4x - 8y)]

(5)

> f3 := RandNice([x, y], 8)

f3 := [(3 - 3x - y) (2 - 5x - 4y), (5 - 6x - 2y) (3 - 7x - 8y)]

(6)

> EquPts(f1, [x, y])

{[10, -6], [42, -26], [- $\frac{27}{7}$ ,  $\frac{32}{7}$ ], [ $\frac{1}{7}$ ,  $\frac{4}{7}$ ]}

(7)

> StEquPts(f1, [x, y])

$\emptyset$

(8)

> L1 := Dis2(f1, x, y, [10, -6] + [0.1, 0.1], 0.01, 10) : print([op(nops(L1) - 3 .. nops(L1), L1)]) :

[[9.98, [Float( $\infty$ ), Float( $\infty$ )]], [9.99, [Float( $\infty$ ), Float( $\infty$ )]], [10.00, [Float( $\infty$ ), Float( $\infty$ )]], [10.01, [Float( $\infty$ ), Float( $\infty$ )]]]

(9)

>  $L2 := \text{Dis2}(f1, x, y, [42, -26] + [0.1, 0.1], 0.01, 10) : \text{print}([\text{op}(\text{nops}(L2)) - 3 .. \text{nops}(L2),$   
 $L2]) :$   
 $[[9.98, [\text{Float}(\infty), \text{Float}(\infty)]], [9.99, [\text{Float}(\infty), \text{Float}(\infty)]], [10.00, [\text{Float}(\infty),$  **(10)**  
 $\text{Float}(\infty)]], [10.01, [\text{Float}(\infty), \text{Float}(\infty)]]]$

>  $L3 := \text{Dis2}\left(f1, x, y, \left[-\frac{27}{7}, \frac{32}{7}\right] + [0.1, 0.1], 0.01, 10\right) : \text{print}([\text{op}(\text{nops}(L3)) - 3 .. \text{nops}(L3),$   
 $L3]) :$   
 $[[9.98, [\text{Float}(\infty), \text{Float}(\infty)]], [9.99, [\text{Float}(\infty), \text{Float}(\infty)]], [10.00, [\text{Float}(\infty),$  **(11)**  
 $\text{Float}(\infty)]], [10.01, [\text{Float}(\infty), \text{Float}(\infty)]]]$

>  $L4 := \text{Dis2}\left(f1, x, y, \left[\frac{1}{7}, \frac{4}{7}\right] + [0.1, 0.1], 0.01, 10\right) : \text{print}([\text{op}(\text{nops}(L4)) - 3 .. \text{nops}(L4),$   
 $L4]) :$   
 $[[9.98, [\text{Float}(\infty), \text{Float}(\infty)]], [9.99, [\text{Float}(\infty), \text{Float}(\infty)]], [10.00, [\text{Float}(\infty),$  **(12)**  
 $\text{Float}(\infty)]], [10.01, [\text{Float}(\infty), \text{Float}(\infty)]]]$

> *#f1 does not have stable equilibrium points*

>  $\text{EquPts}(f2, [x, y])$   
 $\left\{[-8, 13], \left[-3, \frac{7}{4}\right], \left[-\frac{1}{22}, \frac{3}{11}\right], \left[\frac{1}{3}, \frac{1}{2}\right]\right\}$  **(13)**

>  $\text{StEquPts}(f2, [x, y])$   
 $\left\{\left[-\frac{1}{22}, \frac{3}{11}\right]\right\}$  **(14)**

>  $L5 := \text{Dis2}\left(f2, x, y, \left[-\frac{1}{22}, \frac{3}{11}\right] + [0.1, 0.1], 0.01, 10\right) : \text{print}([\text{op}(\text{nops}(L5)) - 3 .. \text{nops}(L5),$   
 $L5]) :$   
 $[[9.98, [-0.04545454593, 0.2727272734]], [9.99, [-0.04545454593, 0.2727272734]],$  **(15)**  
 $[10.00, [-0.04545454593, 0.2727272734]], [10.01, [-0.04545454593, 0.2727272734]]]$

> *#Stable!*

>  $L6 := \text{Dis2}(f2, x, y, [-8, 13] + [0.1, 0.1], 0.01, 10) : \text{print}([\text{op}(\text{nops}(L6)) - 3 .. \text{nops}(L6),$   
 $L6]) :$   
 $[[9.98, [\text{Float}(\infty), \text{Float}(\infty)]], [9.99, [\text{Float}(\infty), \text{Float}(\infty)]], [10.00, [\text{Float}(\infty),$  **(16)**  
 $\text{Float}(\infty)]], [10.01, [\text{Float}(\infty), \text{Float}(\infty)]]]$

>  $L7 := \text{Dis2}\left(f2, x, y, \left[-3, \frac{7}{4}\right] + [0.1, 0.1], 0.01, 10\right) : \text{print}([\text{op}(\text{nops}(L7)) - 3 .. \text{nops}(L7),$   
 $L7]) :$   
 $[[9.98, [\text{Float}(\infty), \text{Float}(\infty)]], [9.99, [\text{Float}(\infty), \text{Float}(\infty)]], [10.00, [\text{Float}(\infty),$  **(17)**  
 $\text{Float}(\infty)]], [10.01, [\text{Float}(\infty), \text{Float}(\infty)]]]$

>  $L8 := \text{Dis2}\left(f2, x, y, \left[\frac{1}{3}, \frac{1}{2}\right] + [0.1, 0.1], 0.01, 10\right) : \text{print}([\text{op}(\text{nops}(L8)) - 3 .. \text{nops}(L8),$   
 $L8]) :$   
 $[[9.98, [\text{Float}(\infty), \text{Float}(\infty)]], [9.99, [\text{Float}(\infty), \text{Float}(\infty)]], [10.00, [\text{Float}(\infty),$  **(18)**  
 $\text{Float}(\infty)]], [10.01, [\text{Float}(\infty), \text{Float}(\infty)]]]$

```

> #Rest are unstable
> EquPts(f3, [x, y])

$$\left\{ \left[ \frac{1}{3}, \frac{1}{12} \right], \left[ \frac{8}{7}, -\frac{13}{14} \right], \left[ \frac{21}{17}, -\frac{12}{17} \right] \right\}$$


```

(19)

```

> StEquPts(f3, [x, y])

$$\left\{ \left[ \frac{1}{3}, \frac{1}{12} \right] \right\}$$


```

(20)

```

> L9 := Dis2(f3, x, y, [1/3, 1/12] + [0.1, 0.1], 0.01, 10) : print([op(nops(L9)-3 ..nops(L9),
L9) ]) :
[[9.98, [0.3333333353, 0.08333333161]], [9.99, [0.3333333353, 0.08333333161]], [10.00,
[0.3333333353, 0.08333333161]], [10.01, [0.3333333353, 0.08333333161]]]

```

(21)

```

> #Stable!
> L10 := Dis2(f3, x, y, [8/7, -13/14] + [0.1, 0.1], 0.01, 10) : print([op(nops(L10)-3
..nops(L10), L10) ]) :
[[9.98, [Float(∞), Float(∞)]], [9.99, [Float(∞), Float(∞)]], [10.00, [Float(∞),
Float(∞)]], [10.01, [Float(∞), Float(∞)]]]

```

(22)

```

> L11 := Dis2(f3, x, y, [21/17, -12/17] + [0.1, 0.1], 0.01, 10) : print([op(nops(L11)-3
..nops(L11), L11) ]) :
[[9.98, [Float(∞), Float(∞)]], [9.99, [Float(∞), Float(∞)]], [10.00, [Float(∞),
Float(∞)]], [10.01, [Float(∞), Float(∞)]]]

```

(23)

```

> #Unstable for the rest

```

```

> #Problem 3

```

```

> EquPts(SIRS(s, i, beta, gamma, nu, N), [s, i])

$$\left\{ [N, 0], \left[ \frac{\nu}{\beta}, \frac{\gamma(N\beta - \nu)}{\beta(\gamma + \nu)} \right] \right\}$$


```

(24)

```

> #We see that values for steady state susceptible and infected align. Since removed is N-S-I, these
also align

```

```

>

```

```

> #Problem 4

```

```

> Chemostat := proc(N, C, a1, a2) :
[a1 * (C / (1 + C) * N) - N, -C / (1 + C) * N - C + a2] :
end:

```

```

> EquPts(Chemostat(N, C, a1, a2), [N, C])

$$\left\{ [0, a2], \left[ \frac{a1(a2 a1 - a2 - 1)}{a1 - 1}, \frac{1}{a1 - 1} \right] \right\}$$


```

(25)

```

>

```