

```
> #Nikita John, Assignment 18
  #Okay to Post; November 8th 2021
> #Maple code for Lecture 18
```

```
Help18 :=proc ( ) :print( ` Dis2(F,x,y,pt,h,A), SIRS(s,i,beta,gamma,nu,N) ` ) :end:
```

```
#SIRS(s,i,beta,gamma,nu,N): The SIRS dynamical model with parameters beta,gamma, nu,N
(see section 6.6 of Edelstein-Keshet), s is the number of
```

```
#Susceptibles, i is the number of infected, (the number of removed is given by N-s-i). N is the
total population
```

```
SIRS :=proc(s, i, beta, gamma, nu, N) : [-beta*s*i + gamma*(N-s-i), beta*s*i-nu*i] :
end:
```

```
#Dis2(F,x,y,pt,h,A): The approximate orbit of the Dynamical system approximating the 2D
for the autonomous continuous dynamical process
```

```
#dx/dt=F[1](x(t),y(t))
```

```
#dy/dt=F[2](x(t),y(t)) , x(0)=pt[1], y(0)=pt[2] with mesh size h from t=0 to t=A
```

```
Dis2 :=proc(F, x, y, pt, h, A) local L, i :
```

```
L := Orb2([x + h * F[1], y + h * F[2]], x, y, pt, 0, trunc(A/h)) :
```

```
L := [seq([i * h, [L[i][1], L[i][2]]], i = 1 ..nops(L)) ] :
```

```
end:
```

```
#OLD STUFF
```

```
Help17 :=proc ( ) :print( ` HW3g(u,v,w,M), HW2g(u,v,M) ` ) :end:
```

```
#HW3g(u,v,w,M): The Hardy-Weinberg unerlying transformation with (u,v,w),
```

```
GENERALIZED Eqs. with the 3 by 3 matrix M (53a,53b,53c) in Edelestein-Keshet Ch. 3
```

```
#Based on Anne Somalwar's solution of the bonus problem from hw15, see the end of
```

```
#from https://sites.math.rutgers.edu/~zeilberg/Bio21/HW15posted/hw15AnneSomalwar.pdf
```

```
HW3g :=proc(u, v, w, M) local tot, LI :
```

```
LI := [
```

```
M[1][1]*u^2 + (M[1][2] + M[2][1])/2 * u * v + M[2][2] * (1/4) * v^2,
```

```
(M[1][2] + M[2][1])/2 * u * v + (M[1][3] + M[3][1]) * u * w + M[2][2]/2 * v^2
+ (M[2][3] + M[3][2])/2 * v * w,
```

```
M[2][2] * 1/4 * v^2 + (M[2][3] + M[3][2])/2 * v * w + M[3][3] * w^2 ] :
```

```

tot := LI[1] + LI[2] + LI[3] :
[LI[1]/tot, LI[2]/tot, LI[3]/tot] :
end:

```

#HW2g(u,v,M): The Generalized Hardy-Weinberg underlying transformation with (u,v), M is the survival matrix. Based on Ann Somalwar's HW3g(u,v,w) (only retain the first two components and replace w by 1-u-v)

```

HW2g := proc(u, v, M) local LI, w :
LI := HW3g(u, v, w, M) :
normal(subs(w = 1 - u - v, [LI[1], LI[2]])) :
end:

```

#OLD STUFF

```

Help15 := proc( ) : print( ` HW3(u,v,w), HW2(u,v) , Dis1(F,x,x0,h,A), ToSys(k,z,f,INI) ` ) :end:

```

#ToSys(k,z,f,INI): converts the kth order difference equation $x(n)=f(x[n-1],x[n-2],\dots,x[n-k])$ to a first-order system

```

#x1(n)=F(x1(n-1),x2(n-1), ...,xk(n-1))
#x2(n)=x1(n-1)
#...

```

#xk(n)=x[k-1](n-1). It gives the underlying transformation phrased in terms of $z[1],\dots,z[k]$, followed by the initial conditions. Try:

```

#ToSys:=proc(2,z,z[1]+z[2],[1,1])
ToSys := proc(k, z, f, INI) local i :
[f, seq(z[i-1], i = 2 ..k)], INI :
end:

```

#HW3(u,v,w): The Hardy-Weinberg underlying transformation with (u,v,w), Eqs. (53a,53b, 53c) in Edelestein-Keshet Ch. 3

```

HW3 := proc(u, v, w) : [u^2 + u*v + (1/4)*v^2, u*v + 2*u*w + 1/2*v^2 + v*w, 1/4
*v^2 + v*w + w^2] :end:

```

#HW2(u,v): The Hardy-Weinberg underlying transformation with (u,v,w), Eqs. (53a,53b,53c) in Edelestein-Keshet Ch. 3 using the fact that $u+v+w=1$

```

HW2 := proc(u, v) : expand([u^2 + u*v + (1/4)*v^2, u*v + 2*u*(1-u-v) + 1/2*v^2
+ v*(1-u-v)]) :end:

```

```

#Dis1(F,x,x0,h,A): The approximate orbit of the Dynamical system approximating the 1D for
the autonomous continuous dynamical process  $dy/dt=F(y(t))$ ,  $y(0)=y_0$  with mesh size  $h$ 
from  $t=0$  to  $t=A$ 
Dis1 :=proc(F, x, x0, h, A) local L, i :
L := Orb(x + h * F, x, x0, 0, trunc(A/h)) :

L := [seq([i * h, L[i]], i = 1 ..nops(L))] :
end:

##old stuff

#M13.txt: Maple code for Lecture 13 of Dynamical Modesl in Biology, Fall 2021 (taught by
Dr. Z.)
Help13 :=proc( ) :
print(`RT2(x,y,d,K), Orb2(F,x,y,pt0,K1,K2), FP2(F,x,y), SFP2(F,x,y), PlotOrb2(L), FP2drz
(F,x,y), SFP2drz(F,x,y)`) end:

with(LinearAlgebra) :

#RT2(x,y,d,K): A random rational transformation of degree  $d$  from  $R^2$  to  $R^2$  with postiiive
integer coefficients from 1 to  $K$  The inputs are variables  $x$  and  $y$  and
#the output is a pair of expressions of  $(x,y)$  representing functions. It is for generating examples
#Try:
#RT2(x,y,2,10);
RT2 :=proc(x, y, d, K) local ra, i, j, f, g :
ra := rand(1 ..K) : #random integer from  $-K$  to  $K$ 
f := add(add(ra( ) * x^i * y^j, j = 0 ..d-i), i = 0 ..d) / add(add(ra( ) * x^i * y^j, j = 0 ..d-i), i = 0
..d) :
g := add(add(ra( ) * x^i * y^j, j = 0 ..d-i), i = 0 ..d) / add(add(ra( ) * x^i * y^j, j = 0 ..d-i), i = 0
..d) :
[f, g] :
end:

#Orb2(F,x,y,pt,K1,K2): Inputs a mapping  $F=[f,g]$  from  $R^2$  to  $R^2$  where  $f$  and  $g$  describe
functions of  $x$  and  $y$ , an initial point  $pt0=[x0,y0]$ 
#outputs the orbit starting at discrete time  $K1$  and ending in discrete time  $K2$ . Try
#F:=RT2(x,y,2,10);
#Orb2(F,x,y,[1.1,1.2],1000,1010);
Orb2 :=proc(F, x, y, pt0, K1, K2) local pt, L, i :
pt := pt0 :

for i from 1 to K1-1 do
pt := subs( {x = pt[1], y = pt[2]}, F) :
od:

```

```

L := [ ]:
for i from K1 to K2 do
  L := [op(L), pt]:
  pt := normal(subs( {x=pt[1], y=pt[2]}, F) ):

od:
L:
end:

#FP2(F,x,y): The list of fixed points of the transformation [x,y]->F. Try
#FP2([x-y,x=y],x,y);
FP2 := proc(F, x, y) local L, i:
L := [solve( {F[1]=x, F[2]=y}, {x, y} )]:

[seq(subs(L[i], [x, y]), i = 1 ..nops(L) )]:
end:

#SFP2(F,x,y): The list of Stable fixed points of the transformation [x,y]->F. Try
#SFP2([(1+x)/(1+y), (1+7*y)/(4+x)],x,y);
SFP2 := proc(F, x, y) local L, J, S, J0, i, pt, EV:

L := evalf(FP2(F, x, y) ):
  #F is the list of ALL fixed points of the transformation [x,y]->F using the previous procedure
  #FP2(F,x,y), but since we are interested in numbers we take the floating point version using
  #evalf

J := Matrix(normal( [ [diff(F[1], x), diff(F[1], y)], [diff(F[2], x), diff(F[2], y)] ] )):
  #J is the Jacobian matrix in general (in terms of the variables x and y). Note that J is a
  #SYMBOLIC matrix featuring variables x and y

S := [ ]: #S is the list of stable fixed points that starts out empty

for i from 1 to nops(L) do #we examine it case by case
  pt := L[i]: #pt is the current fixed point to be examined

  J0 := subs( {x=pt[1], y=pt[2]}, J) :
    #J0 is the NUMERICAL matrix obtained by plugging-in the examined fixed pt

  EV := Eigenvalues(J0) :
    # We used Maple's command Eigenvalues to find the eigenvalues of this 2 by 2 matrix

  if abs(EV[1]) < 1 and abs(EV[2]) < 1 then
    S := [op(S), pt]:
    #If both eigenvalues have absolute value less than 1 it means that they are stable, so we
    #append the examined fixed point, pt, to the list of fixed points
  fi:

od:

```

S : #the output is *S*

end:

###added Oct. 17, 20221

with(*plots*) :

PlotOrb1 :=**proc**(*L*) **local** *i*, *d* :

d := *textplot*([*L*[1], 0, 0]) :

for *i* **from** 2 **to** *nops*(*L*) **do**

d := *d*, *textplot*([*L*[*i*], 0, *i*-1]) :

od:

display(*d*) :

end:

PlotOrb2 :=**proc**(*L*) **local** *i*, *d* :

d := *textplot*([*op*(*L*[1]), 0]) :

for *i* **from** 2 **to** *nops*(*L*) **do**

d := *d*, *textplot*([*op*(*L*[*i*]), *i*-1]) :

od:

display(*d*) :

end:

###End added Oct. 17, 20221

###old stuff

#M11.txt: Maple code for Lecture 11 of Dynamical Models in Biology taught by Dr. Z.

Help11 :=**proc**() :*print*(` *SFPe*(*f*,*x*), *Orbk*(*k*,*z*,*f*,*INI*,*K1*,*K2*) `) :**end:**

SFPe(*f*,*x*): The set of fixed points of $x \rightarrow f(x)$ done exactly (and allowing symbolic parameters), followed by the condition of stability (if it is between -1 and 1 it is stable)

#Try: *FPe*($k*x*(1-x)$,*x*);

#VERSION OF Oct. 12, 2021 (avoiding division by 0)

SFPe :=**proc**(*f*, *x*) **local** *f1*, *L*, *i*, *M* :

f1 := *normal*(*diff*(*f*, *x*)) :

L := [*solve*(*numer*(*f*-*x*), *x*)] :

M := [] :

for *i* **from** 1 **to** *nops*(*L*) **do**

if *subs*(*x*=*L*[*i*], *denom*(*f1*)) \neq 0 **then**

M := [*op*(*M*), [*L*[*i*], *normal*(*subs*(*x*=*L*[*i*], *f1*))]] :

fi:

od:

M:

end:

#Added after class

#Orbk(k,z,f,INI,K1,K2): Given a positive integer k, a letter (symbol), z, an expression f of z [1], ..., z[k] (representing a multi-variable function of the variables z[1],...,z[k]

#a vector INI representing the initial values [x[1],..., x[k]], and (in applications) positive integres K1 and K2, outputs the

#values of the sequence starting at n=K1 and ending at n=K2. of the sequence satisfying the difference equation

##x[n]=f(x[n-1],x[n-2],..., x[n-k+1]):

#This is a generalization to higher-order difference equation of procedure Orb(f,x,x0,K1,K2) . For example

*#Orbk(1,z,5/2*z[1]*(1-z[1]),[0.5],1000,1010); should be the same as*

*#Orb(5/2*z[1]*(1-z[1]),z[1],[0,5],1000,1010);*

#Try:

*#Orbk(2,z,(5/4)*z[1]-(3/8)*z[2],[1,2],1000,1010);*

Orbk := proc (k, z, f, INI, K1, K2) local L, i, newguy :

L := INI: #We start out with the list of initial values

if not (type(k, integer) **and** type(z, symbol) **and** type(INI, list) **and** nops(INI) = k **and** type(K1, integer) **and** type(K2, integer) **and** K1 > 0 **and** K2 > K1) **then**

#checking that the input is OK

print(`bad input`) :

RETURN(FAIL) :

fi:

while nops(L) < K2 **do**

newguy := subs({seq(z[i]=L[-i], i=1 ..k) }, f) :

#Using what we know about the value yesterday, the day before yesterday, ... up to k days before yesterday we find the value of the sequence today

L := [op(L), newguy] : #we append the new value to the running list of values of our sequence

od:

[op(K1 ..K2, L)] :

end:

#####STAFT FROM M9.txt

#M9.txt: Maple Code for "Dynamical models in Biology" (Math 336) taught by Dr. Z., Lecture 9

```

Help9 :=proc( ) :
  print( ` Orb(f,x,x0,K1,K2), Orb2D(f,x,x0,K) , FP(f,x) , SFP(f,x) , Comp(f,x) ` ) :end:

#Orb(f,x,x0,K1,K2): Inputs an expression f in x (describing) a function of x, an initial point,
x0, and a positive integer K, outputs
#the values of x[n] from n=K1 to n=K2. Try: where x[n]=f(x[n-1]), . Try:
#Orb(2*x*(1-x),x,0.4,1000,2000);
Orb :=proc(f, x, x0, K1, K2) local x1, i, L :
x1 := x0 :

for i from 1 to K1 do
x1 := subs(x=x1, f) :
#we don't record the first values of K1, since we are interested in the long-time behavior of
the orbit
od:

L := [x1] :

for i from K1 to K2 do
x1 := subs(x=x1, f) : #we compute the next member of the orbit
L := [op(L), x1] : #we append it to the list
od:

L : #that's the output

end:

#Orb2D(f,x,x0,K): 2D version of Orb(f,x,x0,0,K), just for illustration
Orb2D :=proc(f, x, x0, K) local L, L1, i :
L := Orb(f, x, x0, 0, K) :
L1 := [[L[1], 0], [L[1], L[2]], [L[2], L[2]]] :
for i from 3 to nops(L) do
L1 := [op(L1), [L[i-1], L[i]], [L[i], L[i]]] :
od:
L1 :
end:

#FP(f,x): The list of fixed points of the map x->f where f is an expression in x. Try:
#FP(2*x*(1-x),x);
FP :=proc(f, x)
evalf([solve(f=x, x)]) :
end:

#SFP(f,x): The list of stable fixed points of the map x->f where f is an expression in x. Try:
#SFP(2*x*(1-x),x);
SFP :=proc(f, x) local L, i, fl, pt, Ls :

```

$L := FP(f, x) : \#The\ list\ of\ fixed\ points\ (including\ complex\ ones)$

$Ls := [] : \#Ls\ is\ the\ list\ of\ stable\ fixed\ points,\ that\ starts\ out\ as\ the\ empty\ list$

$f1 := diff(f, x) : \#The\ derivative\ of\ the\ function\ f\ w.r.t.\ x$

for i **from** 1 **to** $nops(L)$ **do**

$pt := L[i] :$

if $abs(subs(x = pt, f1)) < 1$ **then**

$Ls := [op(Ls), pt] : \# if\ pt,\ is\ stable\ we\ add\ it\ to\ the\ list\ of\ stable\ points$

fi:

od:

$Ls : \#The\ last\ line\ is\ the\ output$

end:

$\#Comp(f,x): f(f(x))$

$Comp := \mathbf{proc}(f, x) : normal(subs(x = f, f)) : \mathbf{end:}$

##added Oct. 17, 2021

$\#FP2drz(F,x,y): The\ list\ of\ fixed\ points\ of\ the\ transformation\ [x,y] \rightarrow F.$ Dr. Z.'s way

$\#FP2([x-y, x+y], x, y);$

$FP2drz := \mathbf{proc}(F, x, y) \mathbf{local} eq, i, L, SI :$

$eq := [numer(F[1]-x), numer(F[2]-y)] :$

$L := Groebner[Basis](eq, plex(x, y)) :$

$SI := evalf([solve(L[1], y)]) :$

$[seq([solve(subs(y = SI[i], L[2]), x), SI[i]], i = 1 .. nops(SI))]$] :

end:

$\#SFP2drz(F,x,y): The\ list\ of\ Stable\ fixed\ points\ of\ the\ transformation\ [x,y] \rightarrow F.$ Try

$\#SFP2drz([(1+x)/(1+y), (1+7*y)/(4+x)], x, y);$

$SFP2drz := \mathbf{proc}(F, x, y) \mathbf{local} L, J, S, J0, i, pt, EV :$

$L := FP2drz(F, x, y) :$

$\#F$ is the list of ALL fixed points of the transformation $[x,y] \rightarrow F$ using the previous procedure $FP2(F,x,y)$, but since we are interested in numbers we take the floating point version using $evalf$

$J := Matrix(normal([[diff(F[1], x), diff(F[2], x)], [diff(F[1], y), diff(F[2], y)]])) :$

#J is the Jacobian matrix in general (in terms of the variables x and y). Note that J is a SYMBOLIC matrix featuring variables x and y

S := []: #S is the list of stable fixed points that starts out empty

for *i* **from** 1 **to** nops(L) **do** *#we examine it case by case*

pt := L[i]: #pt is the current fixed point to be examined

J0 := subs({x=pt[1], y=pt[2]}, J):

#J0 is the NUMERICAL matrix obtained by plugging-in the examined fixed pt

EV := Eigenvalues(J0) :

We used Maple's command Eigenvalues to find the eigenvalues of this 2 by 2 matrix

if abs(EV[1]) < 1 **and** abs(EV[2]) < 1 **then**

S := [op(S), pt] :

#If both eigenvalues have absolute value less than 1 it means that they are stable, so we append the examined fixed point, pt, to the list of fixed points

fi:

od:

S : #the output is S

end:

> #1

C := proc(a, b, c, d, e) local numEggPerChicken, numEggPerDay, numEgg, numEggTot :

numEggPerChicken := $\frac{a}{b}$:

numEggPerDay := $\frac{\text{numEggPerChicken}}{c}$:

numEgg := numEggPerDay · d :

numEggTot := numEgg · e :

numEggTot :

end:

> $C\left(\frac{3}{2}, \frac{3}{2}, \frac{3}{2}, 3, 3\right);$

6

(1)

> #2

W := proc(a, b, k) local eqSys, x, y, K, c :

eqSys := $\left\{ \frac{1}{x} + \frac{1}{y} = \frac{1}{a}, \frac{1}{x} + \frac{1}{k \cdot y} = \frac{1}{b} \right\}$:

K := solve(eqSys, {x, y}) :

c := k · K[2] :

c :

end:

> $W(4, 5, 2);$

2 y = 20

(2)

> #3

```
with(LinearAlgebra) :
M1 := Matrix([[2, 0], [4, 0]]) :
Eigenvalues(M1);
```

$$\begin{bmatrix} 0 \\ 2 \end{bmatrix}$$

(3)

```
> M2 := Matrix([[ -2, -2], [ -4, -2]]) :
Eigenvalues(M2);
```

$$\begin{bmatrix} -2 + 2\sqrt{2} \\ -2 - 2\sqrt{2} \end{bmatrix}$$

(4)

```
> #4
```

```
Dis2([x*(1-x-y), x*(3-2*x-y)], x, y, [0.01, -1.01], 0.01, 10);
[[0.01, [0.01, -1.01]], [0.02, [0.010200, -1.009601]], [0.03, [0.01040393890,
```

(5)

```
-1.009194101]], [0.04, [0.01061189181, -1.008779152]], [0.05, [0.01082393516,
-1.008355997]], [0.06, [0.01104014674, -1.007924478]], [0.07, [0.01126060570,
-1.007484435]], [0.08, [0.01148539259, -1.007035704]], [0.09, [0.01171458938,
-1.006578119]], [0.10, [0.01194827945, -1.006111509]], [0.11, [0.01218654765,
-1.005635703]], [0.12, [0.01242948028, -1.005150525]], [0.13, [0.01267716515,
-1.004655795]], [0.14, [0.01292969157, -1.004151332]], [0.15, [0.01318715039,
-1.003636951]], [0.16, [0.01344963400, -1.003112463]], [0.17, [0.01371723637,
-1.002577677]], [0.18, [0.01399005306, -1.002032397]], [0.19, [0.01426818124,
-1.001476425]], [0.20, [0.01455171971, -1.000909559]], [0.21, [0.01484076894,
-1.000331593]], [0.22, [0.01513543105, -0.9997423180]], [0.23, [0.01543580986,
-0.9991415214]], [0.24, [0.01574201090, -0.9985289868]], [0.25, [0.01605414144,
-0.9979044941]], [0.26, [0.01637231050, -0.9972678196]], [0.27, [0.01669662886,
-0.9966187356]], [0.28, [0.01702720911, -0.9959570106]], [0.29, [0.01736416563,
-0.9952824092]], [0.30, [0.01770761463, -0.9945946920]], [0.31, [0.01805767418,
-0.9938936158]], [0.32, [0.01841446420, -0.9931789331]], [0.33, [0.01877810650,
-0.9924503924]], [0.34, [0.01914872478, -0.9917077382]], [0.35, [0.01952644468,
-0.9909507105]], [0.36, [0.01991139375, -0.9901790454]], [0.37, [0.02030370150,
-0.9893924744]], [0.38, [0.02070349941, -0.9885907249]], [0.39, [0.02111092093,
-0.9877735197]], [0.40, [0.02152610152, -0.9869405774]], [0.41, [0.02194917864,
-0.9860916120]], [0.42, [0.02238029177, -0.9852263330]], [0.43, [0.02281958244,
-0.9843444453]], [0.44, [0.02326719422, -0.9834456492]], [0.45, [0.02372327275,
-0.9825296404]], [0.46, [0.02418796573, -0.9815961099]], [0.47, [0.02466142294,
-0.9806447440]], [0.48, [0.02514379626, -0.9796752241]], [0.49, [0.02563523966,
-0.9786872269]], [0.50, [0.02613590922, -0.9776804242]], [0.51, [0.02664596312,
-0.9766544830]], [0.52, [0.02716556167, -0.9756090653]], [0.53, [0.02769486729,
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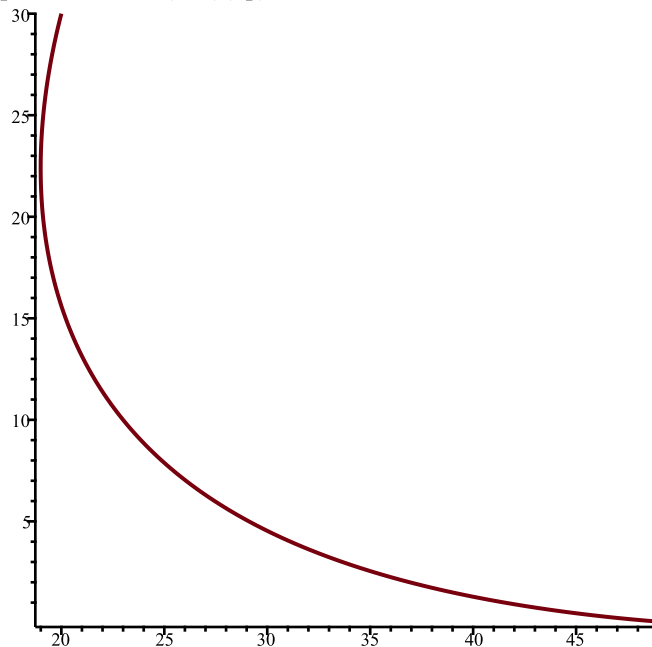
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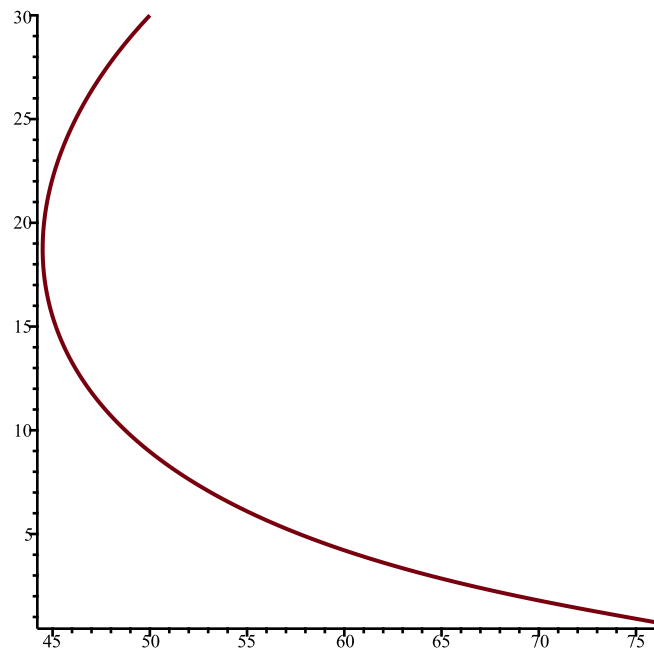
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> #5

```
L1 := Dis2(SIRS(s, i, 0.01, 0.5, 1, 50), s, i, [20, 30], 0.01, 10) :
plot([seq(L1[i][2], i = 1 ..nops(L1))]);
```



```
> L2 := Dis2(SIRS(s, i, 0.01, 0.5, 1, 80), s, i, [50, 30], 0.01, 10) :
plot([seq(L2[i][2], i = 1 ..nops(L2))]);
```



```

> L3 := Dis2(SIRS(s, i, 0.01, 0.5, 1, 120), s, i, [90, 30], 0.01, 10);
plot([seq(L3[i][2], i = 1 ..nops(L3))]);
L3 := [[0.01, [90, 30]], [0.02, [89.7300, 29.9700]], [0.03, [89.46257919, 29.93922081]],
[0.04, [89.19772620, 29.90767259]], [0.05, [88.93542957, 29.87536550]], [0.06,
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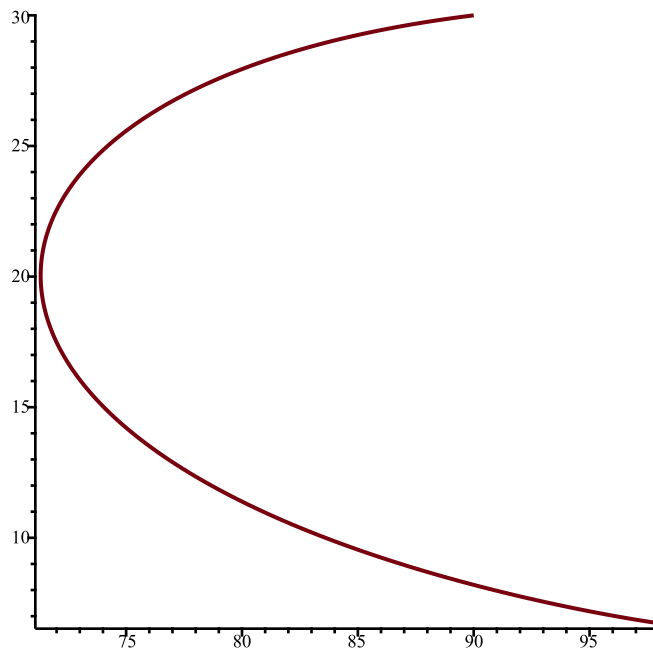
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> #In the long run, if $N=120$, then 98 individuals will be infected

Dynamic Modeling HW 18

3) $x'(t) = x(t)(1-x(t)-y(t))$

$y'(t) = x(t)(3-2x(t)-y(t))$

$F(x,y) = x(1-x-y)$

$G(x,y) = x(3-2x-y)$

$0 = x(1-x-y)$

$x=0, x+y=1$

$0 = x(3-2x-y)$

$x=0, 2x+y=3$

$(x+y=1) \cdot -1$

$+ 2x+y=3$

$x=2$

$2+y=1 \Rightarrow y=-1$

Equilibrium points: $(0,-1), (2,-1)$

Jacobian: $\begin{bmatrix} 1-2x-y & -x \\ 3-4x-y & -x \end{bmatrix}$

$F(x,y) = x - x^2 - xy$

$G(x,y) = 3x - 2x^2 - xy$

* $(0,-1)$

$\begin{bmatrix} 2 & 0 \\ 4 & 0 \end{bmatrix}$

\Rightarrow Eigenvalues: $\lambda = 0, 2$
(on Maple)

Both eigenvalues > 0 ,
 $(0,-1)$ is unstable

* $(2,-1)$

$\begin{bmatrix} -2 & -2 \\ -4 & -2 \end{bmatrix}$

\Rightarrow Eigenvalues: $\lambda = -2 \pm 2\sqrt{2}$
(on Maple)

At least one
eigenvalue > 0 ,
 $(2,-1)$ is unstable