

```
> #Hrudai Battini Hw 18
read "/Users/hb334/Documents/M18.txt";
with(LinearAlgebra):
```

```
> #1
C := proc(a,b,c,d,e) local r,f:
r := a/(b/c):
f := d/r*e:

end:

C(3/2,3/2,3/2,3,3);
```

6

(1)

```
> #2
W := proc(a,b,k) local va,vb,vc:

vc = 1/(1/a-1/b)/(k-1):
end:
W(4,5,2);
```

vc=20

(2)

```
> #3
#i
#F(x,y) = 0 = (x*(1-x-y) = (0,0) , (2,-1)
#G(x,y) = 0 = x(3-2x-y)-> (x,y) = (0,0), (2,-1)
J = [[1-x-y, x], [3-2*x-y,x]];
#(0,0)
J1 := Matrix([[1,0], [3,0]]); #Unstable
Eigenvalues(J1);
#(2,-1)
J2 := Matrix([[0,2], [0,2]]);
Eigenvalues(J2); #Unstable
```

$$J = \begin{bmatrix} 1-x-y & x \\ 3-2x-y & x \end{bmatrix}$$

$$J1 := \begin{bmatrix} 1 & 0 \\ 3 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$J2 := \begin{bmatrix} 0 & 2 \\ 0 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 0 \\ 2 \end{bmatrix}$$

(3)

```
> #4
F := [x*(1-x-y), x*(3-2*x-y)];
Dis2(F,x,y,[2.1,-0.9],0.1,10);
Dis2(F,x,y,[0.1,0.1],0.1,10);
```

$$F := [x(1 - x - y), x(3 - 2x - y)]$$

[[0.1, [2.1, -0.9]], [0.2, [2.058, -0.963]], [0.3, [2.0384490, -0.9944874]], [0.4, [2.029487652, -1.011286381]], [0.5, [2.025793727, -1.020964789]], [0.6, [2.024815484, -1.027168309]], [0.7, [2.025291888, -1.031716583]], [0.8, [2.026593076, -1.035537740]], [0.9, [2.028405795, -1.039114355]], [1.0, [2.030577926, -1.042704072]], [1.1, [2.033040234, -1.046450850]], [1.2, [2.035766666, -1.050441630]], [1.3, [2.038754146, -1.054735408]], [1.4, [2.042012332, -1.059378239]], [1.5, [2.045558472, -1.064411069]], [1.6, [2.049414881, -1.069873912]], [1.7, [2.053607785, -1.075808167]], [1.8, [2.058166873, -1.082258016]], [1.9, [2.063125232, -1.089271370]], [2.0, [2.068519508, -1.096900620]], [2.1, [2.074390196, -1.105203326]], [2.2, [2.080782041, -1.114242910]], [2.3, [2.087744519, -1.124089414]], [2.4, [2.095332405, -1.134820342]], [2.5, [2.103606440, -1.146521614]], [2.6, [2.112634104, -1.159288668]], [2.7, [2.122490506, -1.173227731]], [2.8, [2.133259434, -1.188457297]], [2.9, [2.145034570, -1.205109855]], [3.0, [2.157920926, -1.223333915]], [3.1, [2.172036532, -1.243296396]], [3.2, [2.187514435, -1.265185456]], [3.3, [2.204505083, -1.289213861]], [3.4, [2.223179176, -1.315623017]], [3.5, [2.243731098, -1.344687824]], [3.6, [2.266383073, -1.376722554]], [3.7, [2.291390226, -1.412088010]], [3.8, [2.319046798, -1.451200309]], [3.9, [2.349693816, -1.494541737]], [4.0, [2.383728642, -1.542674250]], [4.1, [2.421616962, -1.596256426]], [4.2, [2.463907951, -1.656064916]], [4.3, [2.511253658, -1.723021858]], [4.4, [2.564434025, -1.798230253]], [4.5, [2.624389525, -1.883020135]], [4.6, [2.692264271, -1.979009522]], [4.7, [2.769463670, -2.088185959]], [4.8, [2.857732650, -2.213017147]], [4.9, [2.959263461, -2.356603396]], [5.0, [3.076846816, -2.522891372]], [5.1, [3.214087893, -2.716979564]], [5.2, [3.375721696, -2.945564281]], [5.3, [3.568084694, -3.217606641]], [5.4, [3.799839626, -3.545357609]], [5.5, [4.083124503, -3.945982925]], [5.6, [4.435440340, -4.444232759]], [5.7, [4.882884199, -5.077013933]], [5.8, [5.465963920, -5.901613182]], [5.9, [6.250684627, -7.011375849]], [6.0, [7.351237182, -8.567792196]], [6.1, [8.980679345, -10.87217140]], [6.2, [11.57743564, -14.54453938]], [6.3, [16.17032446, -21.03986503]], [6.4,

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 × 10¹⁷⁵¹⁵⁷⁷]], [8.8, [-4.959530493 × 10³⁵⁰³¹⁵⁴, -7.013835372 × 10³⁵⁰³¹⁵⁴]], [8.9,
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(4)

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```
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[0.002761081822, 1.647561621]], [10.1, [0.002581522403, 1.647933516]]]
```

```
> #5
N := 50;
Dis2(SIRS(x,y,0.01,0.01,1,N),x,y,[N-30,30],0.1,10);
N2 := 80;
Dis2(SIRS(x,y,0.01,0.01,1,N2),x,y,[N2-50,50],0.1,10);

N3 := 120;
Dis2(SIRS(x,y,0.01,0.01,1,N3),x,y,[N3-110,110],0.1,10); #It
looks as if no one is infected given enough time.
#  $N\beta/v$  is the famous R0-factor, aka infectuous contact number.
```

$N := 50$

```
[[0.1, [20, 30]], [0.2, [19.400, 27.600]], [0.3, [18.86756000, 25.37544000]], [0.4,
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$N2 := 80$

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[3.0, [17.48629189, 4.569496308]], [3.1, [17.46433255, 4.192450223]], [3.2, [17.44945743, 3.846423546]], [3.3, [17.44104355, 3.528899195]], [3.4, [17.43852593, 3.237556961]], [3.5, [17.44139162, 2.970259486]], [3.6, [17.44917451, 2.725038996]], [3.7, [17.46145062, 2.500084777]], [3.8, [17.47783398, 2.293731406]], [3.9, [17.49797296, 2.104447722]], [4.0, [17.52154697, 1.930826519]], [4.1, [17.54826352, 1.771574935]], [4.2, [17.57785563, 1.625505506]], [4.3, [17.61007936, 1.491527856]], [4.4, [17.64471183, 1.368640994]], [4.5, [17.68154920, 1.255926171]], [4.6, [17.72040500, 1.152540274]], [4.7, [17.76110858, 1.057709727]], [4.8, [17.80350366, 0.9707248516]], [4.9, [17.84744714, 0.8909346698]], [5.0, [17.89280785, 0.8177421122]], [5.1, [17.93946560, 0.7505996035]], [5.2, [17.98731017, 0.6890049990]], [5.3, [18.03624051, 0.6324978457]], [5.4, [18.08616389, 0.5806559444]], [5.5, [18.13699523, 0.5330921886]], [5.6, [18.18865645, 0.4894516602]], [5.7, [18.24107587, 0.4494089623]], [5.8, [18.29418768, 0.4126657691]], [5.9, [18.34793143, 0.3789485772]], [6.0, [18.40225163, 0.3480066420]], [6.1, [18.45709726, 0.3196100836]], [6.2, [18.51242148, 0.2935481496]], [6.3, [18.56818122, 0.2696276217]], [6.4, [18.62433692, 0.2476713540]], [6.5, [18.68085220, 0.2275169333]], [6.6, [18.73769362, 0.2090154502]], [6.7, [18.79483044, 0.1920303727]], [6.8, [18.85223440, 0.1764365137]], [6.9, [18.90987951, 0.1621190848]], [7.0, [18.96774186, 0.1489728287]], [7.1, [19.02579947, 0.1369012240]], [7.2, [19.08403211, 0.1258157568]], [7.3, [19.14242119, 0.1156352530]], [7.4, [19.20094959, 0.1062852664]], [7.5, [19.25960157, 0.09769751780]], [7.6, [19.31836265, 0.08980938129]], [7.7, [19.37721951, 0.08256341336]], [7.8, [19.43615988, 0.07590692140]], [7.9, [19.49517247, 0.06979156832]], [8.0, [19.55424691, 0.06417301015]], [8.1, [19.61337364, 0.05901056402]], [8.2, [19.67254386, 0.05426690386]], [8.3, [19.73174948, 0.04990778152]], [8.4, [19.79098305, 0.04590177121]], [8.5, [19.85023773, 0.04222003527]], [8.6, [19.90950719, 0.03883610948]], [8.7, [19.96878563, 0.03572570633]], [8.8, [20.02806771, 0.03286653467]], [8.9, [20.08734852, 0.03023813438]], [9.0, [20.14662353, 0.02782172488]], [9.1, [20.20588858, 0.02560006621]], [9.2, [20.26513982, 0.02355733168]], [9.3, [20.32437373, 0.02167899113]], [9.4, [20.38358707, 0.01995170394]], [9.5, [20.44277684, 0.01836322084]], [9.6, [20.50194030, 0.01690229399]], [9.7, [20.56107493, 0.01555859441]], [9.8, [20.62017840, 0.01432263640]], [9.9, [20.67924856, 0.01318570808]], [10.0, [20.73828345, 0.01213980780]], [10.1, [20.79728127, 0.01117758580]]]

$N3 := 120$

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(5)

67.96473139]], [0.7, [5.890361588, 61.59445078]], [0.8, [5.580063188, 55.79781929]], [0.9, [5.327329949, 50.52939272]], [1.0, [5.122286479, 45.74564020]], [1.1, [4.957096279, 41.40539845]], [1.2, [4.825483238, 37.47010915]], [1.3, [4.722376262, 33.90390962]], [1.4, [4.643642958, 30.67362568]], [1.5, [4.585888323, 27.74870048]], [1.6, [4.546301294, 25.10108287]], [1.7, [4.522536825, 22.70509167]], [1.8, [4.512624583, 20.53726711]], [1.9, [4.514897715, 18.57621738]], [2.0, [4.527936879, 16.80246536]], [2.1, [4.550525974, 15.19829932]], [2.2, [4.581616893, 13.74762965]], [2.3, [4.620301274, 12.43585305]], [2.4, [4.665787732, 11.24972513]], [2.5, [4.717383389, 10.17724145]], [2.6, [4.774478815, 9.207527255]], [2.7, [4.836535665, 8.330735674]], [2.8, [4.903076493, 7.537954007]], [2.9, [4.973676298, 6.821117771]], [3.0, [5.047955472, 6.172932026]], [3.1, [5.125573899, 5.586799509]], [3.2, [5.206225971, 5.056755112]], [3.3, [5.289636380, 4.577406211]], [3.4, [5.375556524, 4.143878404]], [3.5, [5.463761436, 3.751766217]], [3.6, [5.554047153, 3.397088351]], [3.7, [5.646228429, 3.076247105]], [3.8, [5.740136760, 2.785991588]], [3.9, [5.835618658, 2.523384402]], [4.0, [5.932534146, 2.285771471]], [4.1, [6.030755424, 2.070754741]], [4.2, [6.130165699, 1.876167482]], [4.3, [6.230658148, 1.700051952]], [4.4, [6.332134995, 1.540639200]], [4.5, [6.434506686, 1.396330815]], [4.6, [6.537691148, 1.265682434]], [4.7, [6.641613134, 1.147388832]], [4.8, [6.746203619, 1.040270462]], [4.9, [6.851399269, 0.9432612922]], [5.0, [6.957141949, 0.8553978227]], [5.1, [7.063378285, 0.7758091645]], [5.2, [7.170059264, 0.7037080816]], [5.3, [7.277139868, 0.6383829020]], [5.4, [7.384578743, 0.5791902135]], [5.5, [7.492337898, 0.5255482679]], [5.6, [7.600382427, 0.4769310263]], [5.7, [7.708680256, 0.4328627819]], [5.8, [7.817201912, 0.3929133045]], [5.9, [7.925920314, 0.3566934566]], [6.0, [8.034810577, 0.3238512348]], [6.1, [8.143849832, 0.2940681946]], [6.2, [8.253017067, 0.2670562223]], [6.3, [8.362292974, 0.2425546197]], [6.4, [8.471659813, 0.2203274705]], [6.5, [8.581101287, 0.2001612628]], [6.6, [8.690602421, 0.1818627406]], [6.7, [8.800149459, 0.1652569633]], [6.8, [8.909729767, 0.1501855530]], [6.9, [9.019331738, 0.1365051104]], [7.0, [9.128944716, 0.1240857843]], [7.1, [9.238558913, 0.1128099782]], [7.2, [9.348165342, 0.1025711820]], [7.3, [9.457755754, 0.09327291617]], [7.4, [9.567322573, 0.08482777701]], [7.5, [9.676858847, 0.07715657402]], [7.6, [9.786358198, 0.07018754990]], [7.7, [9.895814771, 0.06385567541]], [7.8, [10.00522319, 0.05810201181]], [7.9, [10.11457854, 0.05287313423]], [8.0, [10.22387630, 0.04812061028]], [8.1, [10.33311232, 0.04380052842]], [8.2, [10.44228281, 0.03987307136]], [8.3, [10.55138429, 0.03630213011]], [8.4, [10.66041357, 0.03305495483]], [8.5, [10.76936773, 0.03010183884]], [8.6, [10.87824408, 0.02741583273]], [8.7, [10.98704018, 0.02497248558]], [8.8, [11.09575380,

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