

> #Please do not post homework
#Shreya Ghosh, 10-11-2021, Assignment 10

> #1.

$$\#x = \frac{x}{x+c} \rightarrow x^2 + x(c-1) = 0 \rightarrow x(x+c-1) = 0$$

$$\#x+c-1=0 \rightarrow x=1-c$$

$x=0, 1-c \rightarrow 0$ is always a fixed point because if $x[n-1]$ is 0 then, $x[n]$ is always 0 since $x[n-1]$ is in the numerator

$$\#f(x) = \frac{(x+c)-x}{(x+c)^2} = \frac{c}{(x+c)^2}$$

$$\#f(0) = \frac{c}{c^2} = \frac{1}{c} \rightarrow 0 \text{ is a fixed point for any value of } c \text{ except } c=0$$

$$\#f(1-c) = \frac{c}{(1-c+c)^2} = c \rightarrow 1-c \text{ is a fixed point for } -1 < c < 1$$

> #2i. $(x, y) \rightarrow \left(\frac{-16}{3}x + 5y, -7x + \frac{13}{2}y \right)$

$$\# \left(\frac{-16}{3} - l \right) \left(\frac{13}{2} - l \right) + 35 = 0$$

$$\#l^2 - \frac{7}{6}l + \frac{1}{3} = 0 \rightarrow l = \frac{2}{3}, \frac{1}{2} < 1 \rightarrow \text{stable fixed point}$$

> #2ii. $(x, y) \rightarrow \left(\frac{92}{3}x - 25y, 35x - \frac{57}{2}y \right)$

$$\# \left(\frac{92}{3} - l \right) \left(-\frac{57}{2} - l \right) + 875 = 0$$

$$\#l^2 - \frac{13}{6}l + 1 = 0 \rightarrow l = \frac{3}{2}, \frac{2}{3} \rightarrow \frac{3}{2} > 1 \rightarrow \text{not a stable fixed point}$$

> #2iii. $(x, y) \rightarrow \left(\frac{-177}{4}x + \frac{75}{2}y, \frac{-105}{2}x + \frac{89}{2}y \right)$

$$\# \left(\frac{-177}{4} - l \right) \left(\frac{89}{2} - l \right) + \frac{7875}{4} = 0$$

$$\#l^2 - \frac{1}{4}l - \frac{3}{8} = 0 \rightarrow l = \frac{3}{4}, -\frac{1}{2} \rightarrow -1 < \frac{3}{4}, -\frac{1}{2} < 1 \rightarrow \text{stable fixed point}$$

> with (Linear Algebra)

[&x, Add, Adjoint, BackwardSubstitute, BandMatrix, Basis, BezoutMatrix, BidiagonalForm, BilinearForm, CARE, CharacteristicMatrix, CharacteristicPolynomial, Column, ColumnDimension, ColumnOperation, ColumnSpace, CompanionMatrix, CompressedSparseForm, ConditionNumber, ConstantMatrix, ConstantVector, Copy, CreatePermutation, CrossProduct, DARE, DeleteColumn, DeleteRow, Determinant, Diagonal, DiagonalMatrix, Dimension, Dimensions, DotProduct, EigenConditionNumbers, Eigenvalues,

(1)

Eigenvectors, Equal, ForwardSubstitute, FrobeniusForm, FromCompressedSparseForm, FromSplitForm, GaussianElimination, GenerateEquations, GenerateMatrix, Generic, GetResultDataType, GetResultShape, GivensRotationMatrix, GramSchmidt, HankelMatrix, HermiteForm, HermitianTranspose, HessenbergForm, HilbertMatrix, HouseholderMatrix, IdentityMatrix, IntersectionBasis, IsDefinite, IsOrthogonal, IsSimilar, IsUnitary, JordanBlockMatrix, JordanForm, KroneckerProduct, LA_Main, LUDecomposition, LeastSquares, LinearSolve, LyapunovSolve, Map, Map2, MatrixAdd, MatrixExponential, MatrixFunction, MatrixInverse, MatrixMatrixMultiply, MatrixNorm, MatrixPower, MatrixScalarMultiply, MatrixVectorMultiply, MinimalPolynomial, Minor, Modular, Multiply, NoUserValue, Norm, Normalize, NullSpace, OuterProductMatrix, Permanent, Pivot, PopovForm, ProjectionMatrix, QRDecomposition, RandomMatrix, RandomVector, Rank, RationalCanonicalForm, ReducedRowEchelonForm, Row, RowDimension, RowOperation, RowSpace, ScalarMatrix, ScalarMultiply, ScalarVector, SchurForm, SingularValues, SmithForm, SplitForm, StronglyConnectedBlocks, SubMatrix, SubVector, SumBasis, SylvesterMatrix, SylvesterSolve, ToeplitzMatrix, Trace, Transpose, TridiagonalForm, UnitVector, VandermondeMatrix, VectorAdd, VectorAngle, VectorMatrixMultiply, VectorNorm, VectorScalarMultiply, ZeroMatrix, ZeroVector, Zip]

$$\begin{aligned} > m1 := \left[\left[-\frac{16}{3} \cdot 0.3, 5 \cdot 0.6 \right], \left[-7 \cdot 0.3, \frac{13}{2} \cdot 0.6 \right] \right] \\ m1 := \left[\left[-1.600000000, 3.0 \right], \left[-2.1, 3.900000000 \right] \right] \end{aligned} \quad (2)$$

$$\begin{aligned} > evalm(m1^{1000}) \\ \left[\begin{array}{cc} -3.763553199 \times 10^{356} & 6.942161054 \times 10^{356} \\ -4.859512771 \times 10^{356} & 8.963742121 \times 10^{356} \end{array} \right] \end{aligned} \quad (3)$$

$$\begin{aligned} > m2 := \left[\left[-\frac{92}{3} \cdot 0.3, -25 \cdot 0.6 \right], \left[35 \cdot 0.3, -\frac{57}{2} \cdot 0.6 \right] \right] \\ m2 := \left[\left[-9.200000000, -15.0 \right], \left[10.5, -17.10000000 \right] \right] \end{aligned} \quad (4)$$

$$\begin{aligned} > evalm(m2^{1000}) \\ \left[\begin{array}{cc} 3.768602543 \times 10^{1248} & 1.069093184 \times 10^{1249} \\ -7.483652276 \times 10^{1248} & 9.399159968 \times 10^{1248} \end{array} \right] \end{aligned} \quad (5)$$

$$\begin{aligned} > m3 := \left[\left[-\frac{177}{4} \cdot 0.3, \frac{75}{2} \cdot 0.6 \right], \left[-\frac{105}{2} \cdot 0.3, \frac{89}{2} \cdot 0.6 \right] \right] \\ m3 := \left[\left[-13.27500000, 22.50000000 \right], \left[-15.75000000, 26.70000000 \right] \right] \end{aligned} \quad (6)$$

$$\begin{aligned} > evalm(m3^{1000}) \\ \left[\begin{array}{cc} -1.178923817 \times 10^{1128} & 1.998932780 \times 10^{1128} \\ -1.399252944 \times 10^{1128} & 2.372513420 \times 10^{1128} \end{array} \right] \end{aligned} \quad (7)$$

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