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> #1;
#The number of females born at n=4 =>  $p1 \cdot c2 + p2 \cdot c1 + p3 \cdot c0 + p2 \cdot c2 + p3 \cdot c1$ ;
> #2;
R3 := proc(n, p1, p2, p3, c0, c1, c2) option remember:
  if n = 0 then
    c0;
  elif n = 1 then
    c1;
  elif n = 2 then
    c2;
  else
    expand(p1 · R3(n - 1, p1, p2, p3, c0, c1, c2) + p2 · R3(n - 2, p1, p2, p3, c0, c1, c2) + p3 · R3(n
      - 3, p1, p2, p3, c0, c1, c2)) :
  fi;
  end;
seq(R3(n, 1, 1, 1, 1, 1, 1), n = 1 .. 4); # output for n=4;

#3
#Extinction: When total probability:  $p1 + p2 + p3 < 1$ :
seq(R3(n, 0.3, 0.3, 0.3, 1, 1, 1), n = 1000);

#Stable Population: When probability:  $p1 + p2 + p3 = 1$ :
seq(R3(n, 0.4, 0.3, 0.3, 1, 1, 1), n = 1000);

#Population Explosion: When probability:  $p1 + p2 + p3 > 1$ :
seq(R3(n, 0.5, 0.5, 0.5, 1, 1, 1), n = 1000);

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$$\begin{aligned}
& 1, 1, 3, 5 \\
& 2.232967122 \cdot 10^{-23} \\
& 1.000000000 \\
& 1.276032977 \cdot 10^{91}
\end{aligned} \tag{1}$$