

$$\#R3(4) = (p1 * R3(3, p1, p2, p3, c0, c1, c2) + p2 * R3(2, p1, p2, p3, c0, c1, c2) + p3 * R3(1, p1, p2, p3, c0, c1, c2))$$

$$\#R(0) = c0, R(1) = c1, R(2) = c2$$

#expected number of females born at time n

```
> R3 := proc(n, p1, p2, p3, c0, c1, c2) option remember:
  if n = 0 then
    c0:
  elif n = 1 then
    c1:
  elif n = 2 then
    c2:
  else
    expand(p1 * R3(n - 1, p1, p2, p3, c0, c1, c2) + p2 * R3(n - 2, p1, p2, p3, c0, c1, c2) + p3
      * R3(n - 3, p1, p2, p3, c0, c1, c2));
  fi:
end:
```

seq(R3(i, 1, 1, 1, 1, 1, 1), i=0..4);

1, 1, 1, 3, 5

(1)

```
=
>
>
```

```
> seq(R3(i, 0.01, 0.01, 0.01, 1, 1, 1), i=1000)
  #using values that are very small will lead to population extinction
```

1.161296512 10⁻⁶²⁹

(2)

```
> seq(R3(i, .99, .99, .99, 1, 1, 1), i=1000)
  #using values that are large will lead to population explosion
```

3.944437002 10²⁶¹

(3)

```
> seq(R3(i, .5, .5, .5, 1, 1, 1), i=990..1010)
  #using values around 0.5 will lead to stable population
```

1.561649093 10⁹⁰, 1.926687580 10⁹⁰, 2.377054517 10⁹⁰, 2.932695594 10⁹⁰,

(4)

3.618218845 10⁹⁰, 4.463984477 10⁹⁰, 5.507449457 10⁹⁰, 6.794826388 10⁹⁰,
 8.383130160 10⁹⁰, 1.034270300 10⁹¹, 1.276032977 10⁹¹, 1.574308146 10⁹¹,
 1.942305712 10⁹¹, 2.396323418 10⁹¹, 2.956468638 10⁹¹, 3.647548884 10⁹¹,
 4.500170470 10⁹¹, 5.552093996 10⁹¹, 6.849906675 10⁹¹, 8.451085571 10⁹¹,
 1.042654312 10⁹²