$$\begin{split} \sin(0) &= 0 \; ; \quad \sin(\pi/6) = 1/2 \; ; \quad \sin(\pi/4) = \sqrt{2}/2 \; ; \quad \sin(\pi/3) = \sqrt{3}/2 \; ; \quad \sin(\pi/2) = 1 \\ \cos(0) &= 1 \; ; \quad \cos(\pi/6) = \sqrt{3}/2 \; ; \quad \cos(\pi/4) = \sqrt{2}/2 \; ; \quad \cos(\pi/3) = 1/2 \; ; \quad \cos(\pi/2) = 0 \\ \cos^2 x + \sin^2 x = 1 \; ; \quad 1 + \tan^2 x = \sec^2 x \; ; \quad 1 + \cot^2 x = \csc^2 x \\ \sin(2x) &= 2 \sin x \cos x \; ; \quad \cos(2x) = \cos^2 x - \sin^2 x \\ \cos^2 x &= \frac{1}{2} \left(1 + \cos(2x) \right) \; ; \quad \sin^2 x = \frac{1}{2} \left(1 - \cos(2x) \right) \\ \sin A \cos B &= \frac{1}{2} [\sin(A - B) + \sin(A + B)] \\ \sin A \sin B &= \frac{1}{2} [\cos(A - B) - \cos(A + B)] \\ \cos A \cos B &= \frac{1}{2} [\cos(A - B) + \cos(A + B)] \\ \int \sec x \, dx &= \ln|\sec x + \tan x| + C \; ; \quad \int \csc x \, dx = \ln|\csc x - \cot x| + C \end{split}$$

If T_N , M_N , S_N are the Trapezoidal, Midpoint and Simpson's approximations, then

$$T_N = \frac{\Delta x}{2} [f(x_0) + 2f(x_1) + 2f(x_2) + \dots + 2f(x_{N-2}) + 2f(x_{N-1}) + f(x_N)];$$

$$M_N = \Delta x [f(c_1) + f(c_2) + \dots + f(c_N)] \text{ where } c_j = (x_{j-1} + x_j)/2;$$

$$S_N = \frac{\Delta x}{3} [f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + \dots + 2f(x_{N-2}) + 4f(x_{N-1}) + f(x_N)].$$

If $I = \int_a^b f(x) dx$ then

$$|T_N - I| \le \frac{K_2(b-a)^3}{12N^2}$$
, $|M_N - I| \le \frac{K_2(b-a)^3}{24N^2}$, $|S_N - I| \le \frac{K_4(b-a)^5}{180N^4}$.

The length of the curve y = f(x), $a \le x \le b$ is equal to $\int_a^b \sqrt{1 + (f'(x))^2} dx$. The area of the surface obtained by rotating the curve y = f(x), $a \le x \le b$ about the x-axis is equal to $\int_a^b 2\pi f(x) \sqrt{1 + (f'(x))^2} dx$.

The length of the parametric curve (x(t), y(t)), $a \le t \le b$ equals $\int_a^b \sqrt{(x'(t))^2 + (y'(t))^2} dt$. If a curve is given in polar form by $r = f(\theta)$ then the area bounded by $r = f(\theta)$, $\theta = \alpha$ and $\theta = \beta$ is $\int_{\alpha}^{\beta} \frac{1}{2} r^2 d\theta = \int_{\alpha}^{\beta} \frac{1}{2} (f(\theta))^2 d\theta$. The length of the polar curve $r = f(\theta)$ between $\theta = \alpha$ and $\theta = \beta$ is $\int_{\alpha}^{\beta} \sqrt{r^2 + \left(\frac{dr}{d\theta}\right)^2} d\theta = \int_{\alpha}^{\beta} \sqrt{(f(\theta))^2 + (f'(\theta))^2} d\theta$.

Newton's Law of Cooling is given by $\frac{dT}{dt} = -k(T - T_0)$, where T is the temperature and T_0 is the ambient temperature. The balance P in an annuity is given by $\frac{dP}{dt} = r(P - N/r)$, where r is the interest rate and N is the rate of withdrawal.

The *n*th Taylor polynomial of
$$f(x)$$
 with center a is $T_n(x) = \sum_{k=0}^n \frac{f^{(k)}(a)}{k!} (x-a)^k$
If $|f^{(n+1)}(u)| \le K$ for all u between a and x , then $|f(x) - T_n(x)| \le K \frac{|x-a|^{n+1}}{(n+1)!}$
 $(1+x)^a = 1 + ax + \frac{a(a-1)}{2!}x^2 + \frac{a(a-1)(a-2)}{3!}x^3 + \cdots$ if $|x| < 1$