

Exam 2 prob 5 Find abs max/min of $f(t) = 2t^3 + 3t^2 - 12t$
on $[-3, 3]$. Diff everywhere because polynomial.

$$f'(t) = 6t^2 + 6t - 12 = 6(t^2 + t - 2) = 6(t+2)(t-1)$$

Crit #s: $t = -2, 1$

Check:

$$f(-3) = 9$$

$$f(-2) = 20$$

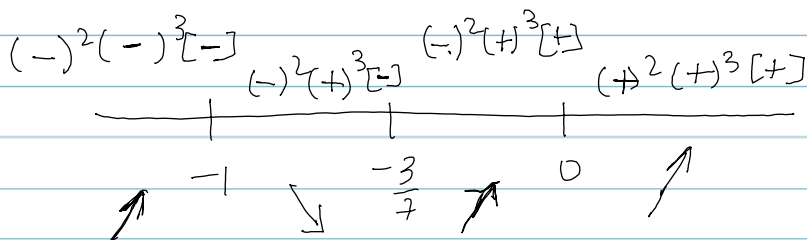
$$f(1) = -7 \leftarrow \text{MIN}$$

$$f(3) = 45 \leftarrow \text{MAX}$$

Prob 6 $f(x) = x^3(x+1)^4$

$$\begin{aligned} f'(x) &= 3x^2(x+1)^4 + x^3 \cdot 4(x+1)^3 = x^2(x+1)^3 [3(x+1) + 4x] \\ &= x^2(x+1)^3 [7x+3] \end{aligned}$$

Crit #s: $x = 0, -1, -\frac{3}{7}$



INC: $(-\infty, -1) \cup (-\frac{3}{7}, \infty)$

DEC: $(-1, -\frac{3}{7})$

REL MAX: $x = -1$

REL MIN: $x = -\frac{3}{7}$