Math 135, Sections 16-18 Review problems for Exam #2 - March 30, 2010

This is the complete list of review problems.

Review sessions will be held on: Wednesday, March 31, 7:00 - 9:00 PM in SEC-117 (BUSCH) and Saturday, April 3, 2:00 - 4:00 PM in HILL-116 (BUSCH)

#1 Find $\frac{dy}{dx}$ and if $2x + e^{xy} = 0$.

#2 Find an equation of the tangent line to the graph of $x^2y - 2xy^3 = 0$ at the point (2, 1).

#3 Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ at the point (2,1) on the graph of $(x-y)^3 + y^2 = 2$.

#4 Find the derivative of the function $(2x+1)^{(3x+1)}$ (where x > 0).

\$5 If $y = 2\sqrt{x} - 9$ and $\frac{dy}{dt} = 5$ find $\frac{dx}{dt}$ when x = 9.

#6 One end of a rope is fastened to a boat and the other end is wound arond a windlass located on a dock at a point 5 feet above the level of the boat. If the boat is drifting away from the dock at the rate of 7 feet/minute, how fast is the rope unwinding at the instant when the lenght of the rope is 13 feet?

#7 A car travels north from the city of Centralia at the rate of 30 miles per hour, starting at 11 AM. A truck travels east from Centralia at the rate of 45 miles per hour, starting at noon. How fast is the distance between the truck and the car changing at 1 PM?

#8 Find $d(x\sqrt{x^2-1})$.

#9 Use differentials to approximate $\sqrt{9.04}$.

#10 The radius of a circle has been measured as 15 inches, but there is a possible error of 0.05 inch in the measurement. Give an approximate value for the error in the computed area.

#11 For each of the following functions:

- (i) find all critical numbers;
- (ii) find the intervals where the function is increasing;
- (iii) find the intervals where the function is decreasing;

(iv) determine whether each critical point is a relative maximum, a relative minimum, or neither;

(v) find the intervals where the graph of the function is concave up and the intervals where the graph of the function is concave down;

(vi) find all points of inflection;

(vii) find all horizontal and vertical asymptotes (realizing that there may be none);

(viii) sketch the graph of the function.

(a)
$$f(x) = x - x^2;$$

(b) $f(x) = x^3 - 3x^2 + 3;$
(c) $f(x) = \frac{1}{3-x};$
(d) $f(x) = \frac{x+1}{2-x};$

#12 Sketch the graph of a function satisfying the following conditions:

$$\begin{split} \lim_{x \to -\infty} f(x) &= 1, \\ \lim_{x \to \infty} f(x) &= -1, \\ \lim_{x \to 1^{-}} f(x) &= -\infty, \\ \lim_{x \to 1^{+}} f(x) &= \infty, \\ f'(x) &> 0 \quad if \quad x < -1, \quad or \quad if \quad 3 < x, \\ f'(x) &< 0 \quad if \quad -1 < x < 1, \quad or \quad if \quad 1 < x < 3, \\ f''(x) &> 0 \quad if \quad x < -3 \quad or \quad if \quad 1 < x < 4, \\ f''(x) &< 0 \quad if \quad -3 < x < 1 \quad or \quad if \quad 4 < x. \end{split}$$

#13 Find the absolute maximum and minimum values of the following functions on the given intervals. Give the values of x for which the absolute maximum and absolute minimum are attained.

(a)
$$f(x) = x^2 - 6x + 1$$
, on [1,4],
(b) $f(x) = \frac{x^3}{3} - x^2 + 1$ on [-3,3],
(c) $f(x) = |2x - 1|$ on $[0, 2\pi]$.
(d) $f(x) = \sin^2(x) + \cos(x)$ on $[0, 2]$.

#14 Find the value of each of the following limits:

(a)
$$\lim_{x\to 0} \frac{\sqrt{1+x}-1}{x}$$
,
(b) $\lim_{x\to 0} \frac{x-\sin(x)}{x^3}$,
(c) $\lim_{x\to 0} x^{-5} \ln(x)$,
(d) $\lim_{x\to \infty} \frac{\ln(\ln(x))}{x}$,
(e) $\lim_{x\to 0} (\frac{1}{\sin(3x)} - \frac{1}{3x})$,
(f) $\lim_{x\to 0^+} (\frac{2\cos(x)}{\sin(2x)} - \frac{1}{x})$.