## MATH 252: Elementary Differential Equations

## Quiz 7

NAME:
Date: November 9, 2017
Solve the following problems on this sheet of paper. Note that there is a problem on the back. No calculators or other electronic devices are permitted.

1. (5 points) Sketch the phase-portrait for the system

$$
\begin{aligned}
& \frac{d x}{d t}=3 x+4 y \\
& \frac{d y}{d t}=x .
\end{aligned}
$$

Note: For full credit, you must have the correct straight-line solutions, if they exist.
2. (5 points) Consider the linear system

$$
\frac{d \mathbf{Y}}{d t}=\left(\begin{array}{cc}
-3 & -5 \\
3 & 1
\end{array}\right) \mathbf{Y}
$$

(a) Find the eigenvalues of the system. Note that they should be complex.
(b) Determine the type of the phase portrait for this system (e.g. center, spiral sink, or spiral source). Provide justification.
(c) Determine the natural period and natural frequency of the oscillations.
(d) Determine the directions of the oscillations in the phase plane.
(e) Using (a)-(d), draw a rough sketch of the phase portrait.

